# Structural and Functional Investigations of Transmembrane Signaling Histidine Kinase Using NMR 

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Seldom, very seldom, does complete truth belong to any human disclosure; seldom can it happen that something is not a little disguised or a little mistaken.
--Jane Austen, Emma

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## RELATED PUBLICATIONS

The work presented in this thesis led to the following publications:

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Kai Xue, Kumar Tekwani Movellan, Xizhou Zhang, Eszter E Najbauer, Marcel C Forster, Stefan Becker, and Loren B Andreas. Towards a native environment: Structure and function of membrane proteins in lipid bilayers by nmr. Chemical Science, 2021.

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## LIST OF ACRONYMS

GPCR G-protein coupled receptor

PDB protein data bank

NMR nuclear magnetic resonance
cryo-EM cryo-electron microscopy

TCST two-component signal transduction
$\mathbf{R R}$ response regulator

HK histidine kinase

TM transmembrane helix

DHp dimerisation and histidine phosphorylation

CA ATP-binding kinase domain

CitA citrate receptor A

PAS Per-ARNT-Sim

PASp periplasmic PAS

PASc cytoplasmic PAS

PASpc periplasmic and cytoplasmic PAS

MAS magic angle spinning
$\mathbf{R F}$ radio frequency

CSA chemical shift anisotropy

REDOR rotational echo double resonance

TEDOR transferred-echo double resonance

## AHT average Hamiltonian theory

CODEX centerband-only detection of exchange

CP cross-polarization

P-helix periplasmic helix

DMPC 1,2-dimyristoyl-sn-glycero-3-phosphocholine

DMPA 1,2-dimyristoyl-sn-glycero-3-phosphatic acid

DMPC 1,2-dimyristoyl-sn-glycero-3-phosphocholine

DMPA 1,2-dimyristoyl-sn-glycero-3-phosphatic acid

CEST chemical exchange saturation transfer
sPRE solvent paramagnetic relaxation enhancement

GT G.thermodenitrificans

WT wild type

COLD cryogenic optical localization

SPA scintillation proximity assay

IMAC immobilized metal affinity chromatography

DLS dynamic light scattering

DM decylmaltoside

TCEP Tris-(2-carboxyethyl)-phosphine hydrochloride

MTSL Methanethiosulfonate

DNP dynamic nuclear polarization

HFA hexafluoroacetone

IPTG isopropyl- $\beta$-D-thiogalactopyranoside

DTT dithiothreitol

LDAO n-dodecyl-N,N-dimethylamine-N-oxide

DEER double electron-electron resonance

TREDOR Transferred-Rotational-Echo DOuble Resonance

CS chemical shift

DSS sodium trimethylsilylpropanesulfonate

ATP adenosine triphosphate


#### Abstract

Membrane proteins play a central role in biology as the gatekeepers of all cellular compartments. And transmembrane signaling through membrane bound kinases is a particularly important process for cellular adaptation to a changing environment. In prokaryotes, the membrane bound HK, which is part of the ubiquitous two-component system, is the most common type of signal transduction employing a protein phosphorylation mechanism. Due to their lipid-bound native environment, structural studies of membrane bound HKs have remained challenging for a spectrum of techniques. The first five chapters of this thesis will be dedicated to the functional and structural studies of a membrane HK CitA, which is activated for cross-phosphorylation upon citrate binding by hydrolysis of ATP molecules, employing NMR spectroscopy. The new regime of ultra-fast MAS NMR has allowed the application of ${ }^{1} \mathrm{H}$-detected experiments to more challenging system. We employed this method for the residue specific assignment of the PASpc construct of CitA and gained chemical shift information of the previously unavailable TM helices, along with their linker regions (Chapter 2). This new piece of information confirms the formation of a P-helix at the end of the PASp domain to further residues downstream, as well as reveals the loosening of a conserved KK linker upon citrate binding between the TM2 helix and the PASc domain.

The role of cytosolic PAS domain in HK activation has remain unsolved since the discovery of HKs over 30 years ago. Based on the functional mutants in the PASc domain of CitA, sPRE profile and NMR visibility, an anti-parallel to parallel dimer rearrangement model for CitA activation in its PASc domain was proposed. However, direct structural evidence and functional data confirming the validity of this structural model is still lacking. We investigated the functional impact of this model on the CitA phosphorylation rate by tracking the ATP hydrolysis using ${ }^{31}$ P NMR (Chapter 3). An attenuation of CitA's kinase activity when the anti-parallel N288D mutant PASc domain, instead of the parallel WT PASc domain, was attached to the DHp domain is observed by us. This confirms the functional relevance of this dimer transition in the activity of CitA. The same ${ }^{31} \mathrm{P}$ NMR method provides a convenient way to test the functionality of CitA with different chemical tags, which is a pre-requisite for site-specific inter-dimer distance measurement. We found that tagging CitA with a small $\mathrm{CF}_{3}$ group of a cysteine mutation site,


N308C, at the end of the PASc domain retains its functionality and responsiveness to citrate binding, while tagging of the same site with MTSL does not. This paves the way for gaining site specific evidence to prove the anti-parallel to parallel transition upon citrate binding using DNP enhanced ${ }^{19}$ F NMR (Chapter 4). From this, we found a large change in inter-N308C distance between the citrate free (more than $20 \AA$ apart) and the citrate bound state ( $11 \AA$ ). This supports the drastic anti-parallel to parallel dimer transition directly. Although our data are collected using a fragment of CitA lacking the DHp domain, they provide key information regarding the structural rearrangement of PASc that lead to HK activation in the context of the TM helices. Combined with the ${ }^{1} \mathrm{H}$-detected MAS NMR assignment, the works presented here suggest that the P-helix formation at the end of PASp, the piston-like upward motion of the TM2 helix, the KK domain loosening at the linker between the TM2 helix and the PASc domain, and the anti-parallel to parallel dimer transition are key events in the activation of CitA with citrate binding.

Internuclear distance determination is the foundation for NMR-based structure calculation. However, high-precision distance measurement is a laborious process requiring lengthy data acquisitions due to the large set of multidimensional spectra needed at different mixing times. This prevents application to large or challenging molecular systems. The last chapter of this thesis will present a new approach, transferred-rotational-echo double resonance (TREDOR), a heteronuclear transfer method in which we simultaneously detect both starting and transferred signals in a single spectrum. This co-acquisition is used to compensate for coherence decay, resulting in accurate and precise distance determination by a single parameter fit using a single spectrum recorded at an ideal mixing time. We showcase TREDOR with the microcrystalline SH3 protein using 3D spectra to resolve resonances. By combining the measured $\mathrm{N}-\mathrm{C}$ and $\mathrm{H}-\mathrm{C}$ distances, we calculate the structure of SH 3 , which converges to the correct fold, with a root-mean-square deviation of $2.1 \AA$ compared to a reference X-ray structure. This demonstrates TREDOR as a fast and straightforward method for determining structures via magic-angle spinning NMR.

## CHAPTER 1

## Introduction

### 1.1 Transmembrane signal transduction through receptor kinases

Membrane proteins, as the gatekeepers of all cellular compartments, play a central role in biology. For cells to perceive and respond to a changing environment, both chemical and physical stimuli need to get transmitted through the membrane in order to initiate the appropriate cellular adaptations. This process, called the transmembrane signal transduction, is most commonly conducted through protein phosphorylation catalyzed by receptor kinases. Receptor kinases are employed in all domains of life and are characterised by a kinase domain that phosphorylates specific amino acid residues (primarily serine/threonine, tyrosine or histidine) either of an effector protein or within the receptor itself [87]. Using protein phosphorylation for signal processing is thermodynamically favorable, as phosphorylation is achieved using a trinucleotide-phosphate molecule, most commonly adenosine triphosphate (ATP), as a high energy phosphate donor. The reverse reaction of dephosphorylation, which restores the system to its original state, can either be done by auto-hydrolysis with the bulk water or by phosphatases, which selectively dephosphorylate the phosphoprotein. The signal network constructed through protein phosphorylation is thus highly tunable, as kinases often act in concert with phosphatases to integrate a multitude of signal inputs. This ensures the intra-cellular crosstalk between different signaling pathways and enables an analog cellular output. Due to their biological importance, these membrane bound receptor kinases represent a major class of drug targets, with G-protein coupled receptors (GPCRs) alone accounting for $11 \%$ of them [144].

Structural determination of the membrane bound receptor kinases has been notoriously challenging. Despite comprising a good $30 \%$ of all proteins, only 4517 membrane protein structures, i.e., $2.5 \%$, are deposited in the protein data bank (PDB) among a total of 182418 entries up till 2021. On top of the usually poor yield upon recombinant production, membrane proteins lose their native structures outside the lipid environment. Solutions to tackle this problem exist across the spectrum of structural biology techniques. Short chain detergents that form micelles are used both in X-ray crystallography and solution state nuclear magnetic resonance (NMR), but are not ideal as they are prone to denature the protein of interest. Recent advances using nanodiscs (discoidal lipid bilayers made soluble by encircling protein belts) in combination with cryo-electron microscopy (cryo-EM) [53] are also proven successful in several cases. But structural techniques in near native lipid environment like liposomes are still desired, due to their resemblance to the protein's natural environment and the relative ease of the sample preparation protocol. For studying transmembrane signaling specifically, the amount of already difficult work is at least doubled, as the signaling proteins usually come in both activated and deactivated states. One gains biological insights into the signaling event from the changes between the two, not from a single state. This is even more crucial in the rational design of drugs, where one state over the other needs to be specifically selected in order to achieve the desired physiological effect.

### 1.2 Membrane bound histidine kinase in the two-component signal transduction mechanism

The two-component signal transduction mechanism (TCST) is the most prevalent mechanism for sensing and responding to environmental changes in prokaryotes [36]. Five percentage of all TCST systems are found in fungi, amoebae and plants [209] but they are absent in animals [39]. Considering the magnitude of their habitats, microbes receive a large variety of environmental signals and must be equipped to respond to a collection of inputs including nutrients, chemoattractants, cell density, osmotic pressure etc. There are tens of thousands of TCST systems present in the currently sequenced genomes and the large repertoire of their input signals makes
them important tools in synthetic biology [109].

TCSTs are named after their two protein signaling components: an often membrane bound dimeric histidine kinase (HK) and a response regulator (RR) (Figure 1.1 [30]). The signal transduction usually starts with a ligand binding event at the sensing domain at the HK N-terminus, and the signal is transmitted through the membrane via a transmembrane helix (TM) bundle and often, cytoplasmic transmitter domains. In the cytoplasm, the signal triggers phosphorylation of the conserved histidine site of the enzymatic transmitter domain at the C-terminus of the HK, catalyzed with the hydrolysis of ATP molecules. A phosphotransfer event then follows, during which the phosphate group on the HK is carried to an aspartate residue in the receiver domain of RR. The phosphorylated RR undergoes extensive structural rearrangement to activate its output domain, which often changes the expression levels of genes relevant for the processing of the diverse input signals received by the HK. This thesis will focus on the investigation of one HK but not RRs, as RRs are often not membrane bound. Extensive review articles are available regarding RRs' structures [225, 63]. To further fine-tune the respective cellular responses and coordinate the various input signals, TCST systems can also be aided by auxiliary proteins, which range from transporters on the membrane to cytosolic binding partners which change the phosphorylation states of HK and RR. They have been summarized by various literature [36, 213, 208].

The first evidence of prokaryote HKs came 30 years ago from the in vitro studies of the HKs NtrB [154] and CheA [90] after the initial findings of protein phosphorylation [32] in the 1960s. Since then, they have emerged as the most common type of signal transduction employing a protein phosphorylation mechanism in microbes, including pathogens. Due to their absence in animals, interfering with the HK signaling important for pathogenicity has been proposed as a potential anti-microbial strategy with the added benefits of fewer side effects and lower likelihood of resistance compared with classical antibiotics [227]. HKs are a diverse group of proteins that do not share domain architecture but are rather characterized by a conserved kinase core consisting of a dimerisation and histidine phosphorylation domain (DHp) and a catalytic, ATP-binding kinase domain (CA). Three classes of HKs are known: Class I HKs are independent sensor proteins that can be either soluble or membrane bound; Class II HKs are soluble kinases that


Figure 1.1: Common signaling mechanism of a TCST system that consists of a Class I histidine kinase (HK) and a response regulator (RR). The HK usually has three domains: the sensor domain (modeled after PDB entry of a citrate binding PAS domain: 3by8 [43]) which responds to the incoming signal (yellow), the transmitter domain(s) which usually spans the bacterial inner membrane and relays the signal to the DHp domain (modeled after PDB entry: 2c2a [139]), which can cross-phosphorylate in between the dimer at a conserved histidine site (upper red). The cross-phosphorylation reaction happens due to the binding and hydrolysis of ATP molecules (upper magenta). A phosphotransfer event then follows so that an aspartate residue (lower magenta) in the response regulator (RR) is phosphorylated (inactive state modeled after PDB entry: 1kgs [35]). This activates the RR and causes it to dimerize and bind to DNA (yellow, lower) for transcription activation of relevant downstream genes (active states modeled after PDB entries: 1gxp [27] and 1zes [14]). The drawings of individual domains are taken from works of the group of D. Goodsell [30]
lack the sensor domain, and need to function with other receptor proteins [88, 159]; Class III HKs are hybrids between Class I and Class II kinases and are characterized by the presence of the sensory domains and the lack of a DHp domain [2]. From here on, HKs will refer solely to Class I HKs. In Class I HKs, the CA domain can phosphorylate the conserved histidine residue in the DHp domain. They have highly modular constructions and often borrow from the same set of signal recognition and signal transduction modules but arrange them in different orders to achieve their diverse functions [81]. Class I HKs can be further divided into subgroups according to their putative sequences and structural motifs [227, 140, 205]. Importantly, almost all HKs characterized structurally function as homo-dimers [39], with the only exceptions being the Pseudomonas aeruginosa GacS-RetS HK hetero-dimers [70] and the monomeric soluble blue light-activated HK from Erythrobacter litoralis HTCC2594, EL346 [170]. Recently, evidence of tetramer organization in the in vivo studies of the CitA/DcuS type of HKs [185] has also been presented. $83 \%$ of all HKs contain transmembrane segments [81], and most of these HKs contain two transmembrane helices. Structural evidence of the transmembrane signal transduction mechanism in these two-pass membrane bound HKs from the periplasmic receiver domain to the cytoplasmic domain is only available from the crystallography data of the TM domain-containing fragment of the nitrate/nitrite sensor NarQ [82]. In it, a piston type upward motion is observed in the TM domains. However, due to the diversity of the domain architecture of HKs, the structural insight from one HK is not nearly enough to cover the canonical signaling mechanism in the TM domains. Studying other types of HKs is therefore necessary.

In the cytoplasm, between the TM domain and the DHp domain, two types of cytoplasmic connector domains can be found: PAS and HAMP. Both domains are often connected to the TM helix by extended $\alpha$-helical stretches such as the signaling helix [6] and other short and long connector $\alpha$-helices [220, 83, 3]. Signaling through the cytoplasmic HAMP domain has been substantially studied, and it is proposed that the HAMP domains serve as converters of the piston-like input in the TM region signal into a helical rotation signal in the DHp domain [82, 81]. The signaling in the cytoplasm through the Per-ARNT-Sim domain (PAS), which can alternatively be found in the periplasm as a ligand receiver domain, is less well studied. The Per-ARNT-Sim domains that form the acronym "PAS" refer to the names of the first three proteins in which


Figure 1.2: The PASp domain from the bacteria G. thermodenitrificans CitA in the citrate free state is shown as the typical PAS fold. The N-terminal helix (grey) is the connector between the core PAS domain and the TM1 helix and does not belong to the core PAS fold. The central $\beta$-scaffold consists of five anti-parallel $\beta$-strand. A major loop between the $\beta 2$ and $\beta 3$ strands hovers over the core $\beta$-scaffold and has a varying number of short $\alpha$-helices. The crystal structure was solved in the group of S.Becker.
its structural motif was recognized: the Drosophila period clock protein (PER), vertebrate aryl hydrocarbon receptor nuclear translocator (ARNT), and Drosophila single-minded protein (SIM). The structure of a typical PAS fold has both $\beta$-strand and $\alpha$-helical components (Figure 1.2). It consists of an N -terminal helix and a core $\beta$-scaffold with five anti-parallel $\beta$-strands facing a large major loop with a varying number of small $\alpha$-helices. Crystal structures have suggested great versatility of the relative position between the N -terminal helix and the PAS domain fold [55, 111]. A dynamic bundle model has been proposed for the PAS domain-mediated cytoplasmic signaling, in which the active, ligand-bound state has an overall higher mobility in the cytoplasmic connector PAS domain [178]. But structural insights of the cytoplasmic connector PAS domain are needed, since there is no evidence that the HAMP domain and PAS domain are interchangeable in their cytoplasmic signal transduction mechanisms. Mutagenesis studies only provided evidence for the existence of dimer rearrangement [55] upon the signaling event, but its interpretation remains ambiguous as to what the structural rearrangements are.

### 1.3 Citrate receptor A (CitA) in the thermophilic bacterium Geobacillus thermodenitrificans

The CitA/DcuS sensor kinase family [72] is a subfamily of Class I HKs, which can bind to citrate (in the case of CitA) and other $\mathrm{C}_{4}$-dicarboxylates (in the case of DcuS). These are key nutrient sources to be degraded in bacterial aerobic growth. The activation of this family of HKs induces the expression of enzymes responsible for catabolizing these $\mathrm{C}_{4}$-dicarboxylates (fumarate reductase, PEP carboxykinase etc.), as well as their respective membrane transporters [213]. CitA is the ideal model protein for studying PAS domain containing HKs, since it is not known so far to require any auxiliary proteins to function, unlike DcuS, which requires the presence of the proteins DctA or DcuB. Otherwise, DcuS remains by itself in a constantly active state [201].

CitA belongs to the class of HKs that contain two PAS domains: the periplasmic PAS domain (PASp) for citrate binding and the cytosolic PAS domain (PASc) as an adaptor between transmembrane helix two (TM2) and the DHp domain. The domain architecture of CitA is shown in Figure 1.3. The ligand binding of CitA is highly selective to citrate. Closely related molecules like isocitrate and tricarballylate does not trigger CitA activation [104]. Depending on whether citrate is bound to the PASp domain, CitA has two functional states: i) the "bound" state in which the kinase is activated and can cross-phosphorylate each monomer by ATP hydrolysis and ii) the "free" state when the PASp domain is in its apo form without citrate, in which the kinase is inactive. The PASp can be studied in isolation without the need for membrane reconstitution, so its structure has been characterized in both signaling states. Structures of the Klebsiella pneumoniae CitA PASp in citrate-free and citrate-bound forms are available both with X-ray crystallography [168, 189] and by solution state NMR [178, 158, 157]. Upon citrate binding, the $\beta$-sheets of PASp tighten to form the binding pocket of CitA; this is accompanied by a rearrangement of the major loop too. The tightening of the $\beta$-sheet core of PASp with ligand binding is compatible with a piston motion of the TM2 first hypothesized based on a cysteine accessibility assay [145]. This was also confirmed with ${ }^{13} \mathrm{C}$-detected solid-state NMR, albeit in only one residue, L154 [178].

The transmembrane signaling mechanism from the TM helices to the PASc domain remains
elusive, mainly because the signaling states cannot be solved in isolation without the sensor domain, PASp. Technical challenges inherent to studying membrane bound kinases cannot be avoided. Crystallography and NMR studies of K. pneumoniae and E. coli CitA PASc domains have thus far remained inconclusive, due to the high mobility of their PASc domains which prevents crystallization and reduces NMR visibility. Fortuitously, a CitA homolog found in the thermophilic bacterium Geobacillus thermodenitrificans (GT CitA) was shown to give NMR spectra of excellent quality both in the PASp and the PASc domains [186] likely owing to reduced PASc dynamics in proteins in thermophilic organisms [166]. GT CitA can be divided into different fragments depending on the purpose of the study. The constructs used in this thesis are presented in Figure 1.3. They are either soluble samples or solid samples embedded in liposomes. The soluble constructs are the isolated periplasmic PAS domain (PASp), the isolated cytoplasmic PAS domain (PASc), and the DHp domain attached with the PASc domain (PASc-kin). The liposome-embedded constructs contain the PASp and PASc domains with the two TM helices (PASpc) alone or including DHp domain as the full length CitA. The dynamic bundle model of cytoplasmic PAS domain [178] mentioned in the previous section was proposed using the GT CitA PASpc construct. In this model, the PASc domain increases its mobility when the citrate is bound to allow CitA activation.

The effects of different point mutations in the PASc domain were tested in E. coli DcuS [145]. A functional mutant N288D in the GT CitA PASc domain can be generated from the constitutively active N304D mutant in E. coli DcuS based on protein sequence alignment results [177] between GT CitA and E. coli DcuS. Another point mutation R289D, also a polar residue, neighbouring the N 288 D mutation was selected as a second possible mutant to rule out potential errors in the sequence alignment. The functionality of both mutants was verified in vivo in the lab of Prof. Unden [177]. A structural model was proposed based on the crystal structures of the N288D mutant and the WT PASc in G. thermodenitrificans solved in the group of Stefan Becker (department of NMR-based Structural Biology, Max-Planck-Institute for Biophysical chemistry )(Figure 3.1). The N288D mutant displayed an anti-parallel dimer form in the crystal structure, which is different from the parallel dimer form observed with the WT PASc, even though the N288D mutant does not disturb the functionality of CitA in G. thermodenitrificans
[186, 177] (Figure A.1). The two dimers differ from one another in the arrangement of the N-terminal helix, but not the central PAS fold. Another difference between the two dimer forms is the inter-dimer distance at the C-terminus, with the anti-parallel dimer having a much larger C-terminal inter-dimer distance than the parallel dimer. M. Salvi et al. proposed that the PASc dimer switches from an anti-parallel to parallel dimer arrangement upon activation by citrate binding, based on chemical exchange saturation transfer (CEST) [214] and solvent paramagnetic relaxation enhancement (sPRE) measurements [236]. The R289D mutant displayed an "open" dimer arrangement, where the two N -terminal helices do not form the dimer interface in the PASc. This dimer form will not be the focus in this thesis, as it is proposed to either be a lowly populated, non-detectable transition state between the anti-parallel and parallel dimers or a dimer form only adopted by isolated PASc domain, since evidence of its existence could not be found through NMR visibility or in the sPRE profile in the membrane bound PASpc construct [177]. More details regarding this structural model of CitA PASc can be found in Chapter 3. However, direct structural and functional evidence in CitA still needs to be found to prove the validity of this model conclusively. This thesis will aim to verify if the anti-parallel dimer form leads to deactivation of the HK activity of GT CitA through a ${ }^{31} \mathrm{P}$ NMR based ATP hydrolysis assay in Chapter 3. In addition, residue specific inter-dimer distance changes that proves this anti-parallel to parallel dimer transition upon CitA activation will be shown in Chapter 4 using a chemically tagged CitA PASpc sample.

### 1.4 MAS NMR spectroscopy

High-resolution magic angle spinning (MAS) NMR is emerging as a powerful tool in giving structural insights in natural materials $[124,125]$, and in determining membrane protein structures. It has no theoretical limit to the size of the molecule of interest. Protein dynamics, particularly important in studying conformational plasticity, can also be readily studied in almost all time scales by NMR [229]. Hardware developments including ultra-fast MAS probes and high field magnets have incrementally contributed to better resolution and sensitivity over the years. Most notably are the recent availability of the high magnetic fields up to 1.2 GHz , which have been reported to increase resolution and sensitivity across a spectrum of membrane proteins


Figure 1.3: Domain architecture of GT CitA and subdivisions of it that form the constructs used in this thesis. The soluble constructs are isolated PASp, isolated PASc and PASc-kin which contains the PASc domain and the DHp domain. The solid constructs are the full length CitA and the PASpc construct which contains the PASp domain, TM1 and TM2 helices, and the PASc domain.
[38, 153]. Application of MAS NMR to biological samples is still in its nascent stage, with earliest membrane protein structures solved only about ten years ago. In the last years, significant contributions of MAS NMR to membrane-associated proteins include [229], i) the transmembrane domain of SARS-CoV-2 envelop protein E from Hong's group [136, 95] ii) the bacterial alkane transporter AlkL [187] from the group of Pintacuda and Andreas, iii) evolution of membrane associated $\alpha$-Synuclein fibrils from the group of Griesinger and Andreas [12], iv) the atomic resolution structure of the HIV capsid tubes by the group of Gronenborn and Polenova [130]. The new regime of ${ }^{1} \mathrm{H}$-detection reduces the requirements for sample quantity and measurement time significantly. With faster spinning, the large proton homonuclear dipolar coupling is reduced under the coherent averaging by MAS, making the ${ }^{1} \mathrm{H}$ linewidth small enough to extract site-specific chemical shift (CS) information in proteins. This additional dimension on top of the four-fold sensitivity gain compared with that of the ${ }^{13} \mathrm{C}$-detection, makes ${ }^{1} \mathrm{H}$-detection suitable for more challenging proteins.

Sequence specific chemical shift assignment is the first step in the investigation of proteins using NMR. Only from this, residue specific chemical shift information can be obtained. Strategies and recent development of sequence specific assignment using ${ }^{1} \mathrm{H}$-detected solid state NMR will be reviewed in Chapter 2. Previously, isolated PASp and PASc constructs from GT CitA have been assigned using solution state NMR [178]. The chemical shift information from them are borrowed for assigning the ${ }^{13} \mathrm{C}$-detected solid state NMR spectra. The drawback is obvious: the TM regions cannot be assigned since they are missing in the isolated domains. All information contained in the chemical shift including the dihedral angles of the peptide bond and local dynamics in the TM domains is missing. This prevents us from detecting any secondary structural or dynamics changes in the regions that connect the PASp and PASc upon citrate binding, which is crucial in understanding the transmembrane signaling mechanism in CitA. With the advantage offered by ${ }^{1} \mathrm{H}$-detection, we performed residue specific assignment experiment in GT CitA PASpc construct including the TM1 and TM2. The dynamic and structural implications from these data in the context of CitA transmembrane signal transduction form the PASp to the PASc domain are discussed in Chapter 2.

The following subsections will introduce the basics of spin physics behind the concepts of the NMR experiments done in this thesis.

### 1.5 Spin Hamiltonians relevant to MAS NMR

The concept of spin was first inferred from the Stern-Gerlach experiment, where the unpaired electron silver atom is observed to interact with an inhomogeneous magnetic field. For NMR experiments, nuclear spin is relevant, which is an intrinsic property of the atom nuclei themselves, rather than originating from rotation in physical space. Its effect is first described by Purcell, Torrey, and Pound [164] in solids. Simultaneously, Bloch, Hansen, and Packard [28] measured the same effect in what they called the "nuclear induction experiment." Its quantum mechanics treatment is analogous to that of angular momentum in classical mechanics and has been formulated extensively in literature $[46,73,176,198]$. The descriptions presented here will follow those from the book Spin Dynamics by M. Levitt [114] and Solid-State NMR Spectroscopy by M. Duer [54]. Without going deeper into spin physics, the spin angular momentum ( $\mu$ ) and the magnetic moment $(S)$ are proportional to each other (the ${ }^{\wedge}$ sign denotes operators), by:

$$
\begin{equation*}
\hat{\mu}=\gamma \hat{S} \tag{1.1}
\end{equation*}
$$

where $\gamma$ is called the gyromagnetic ratio, whose magnitude is an indication of the strength of interaction between the nuclear angular momentum and the magnetic field. It is dependent on the nucleus type. For biological systems, the nuclei of interest are ${ }^{1} \mathrm{H},{ }^{19} \mathrm{~F},{ }^{13} \mathrm{C},{ }^{31} \mathrm{P}$ and ${ }^{15} \mathrm{~N}$, with the size of gyromagnetic ratio in descending order. For this reason, ${ }^{1} \mathrm{H}$-detected NMR experiments have the added advantage of being more sensitive than their ${ }^{13} \mathrm{C}$ detected counterparts. The entire quantum state of a system can be described by the wave function $\mid \Psi_{\text {full }}(t)>$ which obeys the time dependent Schrödinger equation. For our purpose, we will only be concerned with the part, $\mid \Psi(t)>$, that is involved in the spin state:

$$
\begin{equation*}
\frac{d}{d t}|\Psi(t)>\approx-i \hat{\mathcal{H}}| \Psi(t)> \tag{1.2}
\end{equation*}
$$

The Hamiltonian operator $\hat{\mathcal{H}}$ that appears here is called the nuclear spin Hamiltonian, and describes the direction of nuclear spin polarization. An important assumption here is that any rapid influence from the surrounding electrons of the nucleus is treated as an average and has no time dependence. Components that contribute to the nuclear spin Hamiltonians will be discussed.

## External spin Hamiltonians and simple NMR experiments

When a single spin is placed in a large static magnetic field, the interaction of spin angular momentum and a large magnetic field $B_{0}$ is dependent on the minus dot product of their respective operator, and when the field is aligned along the $z$-axis in the laboratory frame, becomes:

$$
\begin{equation*}
\hat{\mathcal{H}}^{\text {static }}=-\hat{\mu} B_{0}=-\gamma \hat{S}_{z} B_{0} \tag{1.3}
\end{equation*}
$$

This part of the spin Hamiltonian (expressed in angular frequency unit) is called the Zeeman interaction. For nuclei with a quantum number $1 / 2$, which account for the most common types of the spins relevant in biological systems, there are two Zeeman eigenstates, $\mid \alpha>$ and $\mid \beta>$ :

$$
\begin{equation*}
\left|\alpha>=\left|\frac{1}{2},+\frac{1}{2}>,|\beta>=| \frac{1}{2},-\frac{1}{2}>\right.\right. \tag{1.4}
\end{equation*}
$$

The matrix representation of the spin angular momentum operator at the $z$ direction $\hat{S}_{z}$ with the above-mentioned $\mid \alpha>$ and $\mid \beta>$ Zeeman eigenbasis is:

$$
\hat{S}_{z}=\frac{1}{2}\left(\begin{array}{cc}
1 & 0  \tag{1.5}\\
0 & -1
\end{array}\right)
$$

which should also satisfy the cyclic commutation relationship with $\hat{S}_{x}$ and $\hat{S}_{y}$. The Zeeman interaction spin Hamiltonian becomes:

$$
\hat{\mathcal{H}}^{\text {static }}=-\frac{\gamma B_{0}}{2}\left(\begin{array}{cc}
1 & 0  \tag{1.6}\\
0 & -1
\end{array}\right)
$$

When plugged into the time dependent Schrödinger equation, one gets the spin precession at the Larmor frequency term $\gamma B_{0}$. This means that the frequency at which a specific spin precesses is
dependent on both the external magnetic field and the gyromagnetic ratio of the spin itself. For a simple NMR experiment, when the sample (essentially a mass of spins) is placed in the coil inside the large magnetic field, an oscillating radio frequency (RF) field $B_{1}$ linearly polarized with phase, $\phi$, is applied near the Larmor frequency $\left(\omega_{r f}\right)$ along the transverse plane. For convenience, it can be decomposed into two rotating components, one in the same sense as the spin precession and one opposite. It can be shown that the non-resonant component (the one opposite in the direction of the spin precession) has negligible effects. So only the resonant component should be considered:

$$
\begin{equation*}
B_{1}^{r e s}(t)=\frac{1}{2} B_{1}\left[\cos \left(\omega_{r f} t+\phi\right) \vec{e}_{x}+\sin \left(\omega_{r f} t+\phi\right) \vec{e}_{y}\right] \tag{1.7}
\end{equation*}
$$

, where $\vec{e}_{x}$ and $\vec{e}_{y}$ are unitary vectors in the $x$ and $y$ directions in the laboratory frame, respectively. The effect of this transverse RF field on the spin Hamiltonian can be approximated:

$$
\begin{equation*}
\hat{\mathcal{H}}^{R F}(t) \approx-\frac{1}{2} \gamma B_{1}\left[\cos \left(\omega_{r f} t+\phi\right) \hat{S}_{x}+\sin \left(\omega_{r f} t+\phi\right) \hat{S}_{y}\right] \tag{1.8}
\end{equation*}
$$

This Hamiltonian, became explicitly time independent when expressed in the rotating frame if the spins are in resonance, i.e., $\omega_{r f}=\gamma B_{0}$.

$$
\begin{equation*}
\hat{\mathcal{H}}_{r}^{R F}(t)=-\frac{1}{2} \gamma B_{1}\left[\cos (\phi) \hat{S}_{x}+\sin (\phi) \hat{S}_{y}\right] \tag{1.9}
\end{equation*}
$$

Effectively, this Hamiltonian is a rotation about the $x$-axis in the rotating frame. The polarization generated by the Zeeman Hamiltonian is "tipped" into the transverse plane by the application of this RF field. This can then be detected by the current induced in the coil. The combination of the Zeeman Hamiltonian and the RF Hamiltonian constitute the external part of the spin Hamiltonian.

## Internal spin Hamiltonians

Influences of the electric and magnetic fields originating from the sample itself constitute the internal spin Hamiltonian. They are important properties of the sample as they encode geometric, distance and dynamic information. In terms of structural biology, the structure and functional dynamics of proteins can be inferred from these parameters. The internal Hamiltonians include the
following terms:

$$
\begin{equation*}
\hat{\mathcal{H}}^{\text {internal }}=\hat{\mathcal{H}}^{C S, \text { iso }}+\hat{\mathcal{H}}^{C S A}+\hat{\mathcal{H}}^{D D}+\hat{\mathcal{H}}^{J}+\hat{\mathcal{H}}^{\text {quadrupole }} \tag{1.10}
\end{equation*}
$$

The quadrupole coupling Hamiltonian $\hat{\mathcal{H}}^{\text {quadrupole }}$ only concerns larger than spin $1 / 2$ nuclei and will not be discussed here. The J-coupling term $\hat{\mathcal{H}}^{J}$ comes from the direct chemical bond between atoms, including hydrogen bonds. Though very important for solution NMR, in biological solid-state NMR, they are usually too weak to be resolved because of the broad spectral lines. However, with the emergence of ultra-fast high resolution MAS NMR, J-coupling has been used to study key features of proteins, like the study of hydrogen bonding in the influenza A protein M2 [146].
$\hat{\mathcal{H}}^{C S, i s o}$ and $\hat{\mathcal{H}}^{C S A}$ are isotropic and anisotropic chemical shift terms, respectively. Physically, they can be described as a "local magnetic field" $\vec{B}^{\text {induced }}$ generated by the electronic environment of the nucleus. Typically, they come from the nearby electron density of the nucleus and therefore are mainly influenced by the type of chemical bonds and the bonded nuclei. This induced field is linearly dependent on the applied magnetic field along the $z$-axis.

$$
\begin{equation*}
\vec{B}^{\text {induced }}=\boldsymbol{\delta} \cdot \vec{B}_{0} \tag{1.11}
\end{equation*}
$$

, where $\boldsymbol{\delta}$ is a $3 \times 3$ matrix and is called the chemical shift tensor. And since $\vec{B}_{0}$ only has the $z$ component, the chemical shift tensor can be reduced to:

$$
\vec{B}^{\text {induced }}=\left(\begin{array}{c}
\delta_{x z} B_{0}  \tag{1.12}\\
\delta_{y z} B_{0} \\
\delta_{z z} B_{0}
\end{array}\right)
$$

And under the secular approximation, the chemical shift Hamiltonian is simplified to:

$$
\begin{equation*}
\hat{\mathcal{H}}^{C S}=-\hat{\mu} \cdot \vec{B}^{\text {induced }} \approx-\gamma \delta_{z z} B_{0} \hat{S}_{z} \tag{1.13}
\end{equation*}
$$

The size of the $\delta_{z z}$ is dependent on the orientation of the molecule with regard to the magnetic field. In an isotropic liquid, the $\delta^{i s o}$ is the average over all possible configurations, and is called the isotropic chemical shift. It is convenient to combine the isotropic chemical shift Hamiltonian with the Zeeman interaction Hamiltonian:

$$
\begin{equation*}
\hat{\mathcal{H}}^{0}=\hat{\mathcal{H}}^{C S, i s o}+\hat{\mathcal{H}}^{\text {static }}=-\gamma\left(1+\delta^{i s o}\right) B_{0} \hat{S}_{z} \tag{1.14}
\end{equation*}
$$

This term will determine the isotropic peak position in an NMR spectrum for a molecule and its prefactor , $-\gamma\left(1+\delta^{i s o}\right) B_{0}$, is called the chemically shifted Larmor frequency. The major influences of its value and dynamic range are the type of nuclei, the electronegativity of the directly bonded chemical group, and other nearby molecular units in space. For proteins, the isotropic chemical shifts of the $C_{\alpha}$ and $C_{\beta}$ atoms are identifying parameters for residue typing during assignment. In solids, where there is no intrinsic motional averaging, the chemical shift is dependent on the relative orientation of the molecule with the external field. This orientation dependent chemical shift Hamiltonian is called the chemical shift anisotropy (CSA) $\hat{\mathcal{H}}^{C S A}$. Without MAS, a solid sample containing a random ensemble of orientations will give the so called powder spectrum, a very broad pattern with some sharp corners. With sufficient MAS frequency, one gets back the isotropic spectrum as spinning about the magic angle averages the chemical shift anisotropy. Note that the chemical shift anisotropy in Hz scale also increases with the external magnetic field.

The dipolar coupling Hamiltonian is maybe the most important interaction in biological solid-state NMR due to its direct dependence on the distance between two spins. The direct dipole-dipole coupling between two spins $i$ and $j$ originates from the interaction of the magnetic fields generated by the spins themselves. It will depend on the relative orientation between the two spins and their internuclear distance. Expressed in angular frequency unit, it is :

$$
\begin{equation*}
\hat{\mathcal{H}}^{D D}=-\frac{\mu_{0}}{4 \pi} \frac{\gamma_{i} \gamma_{j} \hbar}{r_{i j}^{3}}\left[3\left(\hat{S}_{i} \cdot \overrightarrow{e_{i j}}\right)\left(\hat{S}_{j} \cdot \overrightarrow{e_{i j}}\right)-\hat{S}_{i} \cdot \hat{S}_{j}\right] \tag{1.15}
\end{equation*}
$$

, where $\overrightarrow{e_{i j}}$ is a unit vector parallel to the line joining the center of the two nuclei (the internuclear vector), and $\mu_{0}$ the magnetic constant. In spherical coordinates using raising ( $\hat{S_{+}}$) and lowering


Figure 1.4: Powder pattern of CSA which consists of a very broad spectrum with sharp corners. The broadening is caused by the different chemical shifts with different molecular orientations. Different chemical shift tensors give different powder pattern. The powder patterns of a rhombic (upper) and an axially symmetric (middle) CSA tensor are shown. The most probable orientation in the powder arises from the situation when the principal axis is perpendicular to the magnetic field. Under sufficient coherent averaging by MAS, this inhomogeneous interaction is eliminated, leaving a sharp peak at the isotropic chemical shift, which is the numerical average of the three tensor components (lower) described in equation 1.12 [31].
( $\hat{S_{-}}$) operators, the dipolar coupling Hamiltonian is:

$$
\begin{equation*}
\hat{\mathcal{H}}^{D D}=-\frac{\mu_{0}}{4 \pi} \frac{\gamma_{i} \gamma_{j} \hbar}{r_{i j}^{3}}(A+B+C+D+E+F) \tag{1.16}
\end{equation*}
$$

where,

$$
\begin{aligned}
A & =\hat{S_{z}^{i}} \hat{S_{z}^{j}}\left(3 \cos ^{2} \theta-1\right) \\
B & =-\frac{1}{4}\left[\hat{S_{+}^{i}} \hat{S_{-}^{j}}+\hat{S_{-}^{i}} \hat{S_{+}^{j}}\right]\left(3 \cos ^{2} \theta-1\right) \\
C & =\frac{3}{2}\left[\hat{S_{z}^{i}} \hat{S_{+}^{j}}+\hat{S_{+}^{i}} \hat{S_{z}^{j}}\right] \sin \theta \cos \theta e^{-i \phi} \\
D & =\frac{3}{2}\left[\hat{S_{z}^{i}} \hat{S_{-}^{j}}+\hat{S_{-}^{i}} \hat{S_{z}^{j}}\right] \sin \theta \cos \theta e^{+i \phi} \\
E & =\frac{3}{4}\left[\hat{S_{+}^{i}} \hat{S_{+}^{j}}\right] \sin ^{2} \theta e^{-2 i \phi} \\
F & =\frac{3}{4}\left[\hat{S_{-}^{i}} \hat{S_{-}^{j}}\right] \sin ^{2} \theta e^{+2 i \phi}
\end{aligned}
$$

, and the raising $\left(\hat{S_{+}}\right)$and the lowering $\left(\hat{S_{-}}\right)$operators satisfy the relations:

$$
\begin{equation*}
\hat{S_{ \pm}}=\hat{S_{x}} \pm i \hat{S_{y}} \tag{1.17}
\end{equation*}
$$

The spherical coordinates here are defined such that $\theta$ is the tilt angle from the $z$-axis (the direction of the $B_{0}$ field) and $\phi$ as the tilt angle at the transverse plane. In the case of homonuclear dipolar coupling, where spin $i$ and spin $j$ are the same nuclei type, after zero order (or high field) approximation, we get:

$$
\begin{equation*}
\hat{\mathcal{H}}_{\text {homo }}^{D D}=-\frac{\mu_{0}}{4 \pi} \frac{\gamma_{i} \gamma_{j} \hbar}{r_{i j}^{3}}\left(3 \cos ^{2} \theta-1\right)\left[\hat{S}_{z}^{i} \hat{S}_{z}^{j}-\frac{1}{2}\left(\hat{S}_{x}^{i} \hat{S}_{x}^{j}+\hat{S}_{y}^{i} \hat{S}_{y}^{j}\right)\right] \tag{1.18}
\end{equation*}
$$

The first part of the spin operator terms (the ones inside the square bracket) acts as the J-coupling and leads to peak splitting in an NMR spectrum. The second part, however, splits previously degenerate Zeeman levels, and leads to peak splitting in a similar way as in the strong coupling regime, where the coupling constant is not much smaller than the chemical shift separation. This


Figure 1.5: A typical Pake pattern in solid-state NMR [65]. It has the characteristic double corners as the two possible transitions are of the opposite sign, which comes from the dipolar coupling that behaves as two axially symmetric CSA tensors that are mirror images of themselves at the isotropic chemical shift. The separation of the two corners is the strength of the interaction. And just like the CSA powder pattern, the most probable orientation (the sharp corner) corresponds to the situation when the principal axis of the interactions are perpendicular to the magnetic field.
is not the case for heteronuclear dipolar coupling, where the situation is simpler:

$$
\begin{equation*}
\hat{\mathcal{H}}_{\text {hetero }}^{D D}=-\frac{\mu_{0}}{4 \pi} \frac{\gamma_{i} \gamma_{j} \hbar}{r_{i j}^{3}}\left(3 \cos ^{2} \theta-1\right) \hat{S}_{z}^{i} \hat{S}_{z}^{j} \tag{1.19}
\end{equation*}
$$

The effect of heteronuclear dipolar coupling on the NMR spectrum is only splitting of Zeeman energies, so much like the J-coupling, it splits the spectrum, but one transition will be the mirror image of the other with respect to the isotropic chemical shift. And adding the spatial dependencies of the dipolar coupling, one would get something like two mirror image powder spectra (Figure.1.4) added together, this is called a Pake pattern (Figure.1.5). It is worth noting that the quadrupole transitions in nuclei like deuterium results in similar patterns. Just like the chemical shift Hamiltonian, the spatial dependence of the dipolar coupling can be averaged out with spinning the sample sufficiently quickly at an tilt angle from the $B_{0}$ field $\theta_{R}$, if it satisfies the relation:

$$
\begin{equation*}
3 \cos ^{2} \theta_{R}-1=0 \tag{1.20}
\end{equation*}
$$

and one gets $\theta_{R} \approx 54.74^{\circ}$, which is the magic angle.


Figure 1.6: The REDOR pulse sequence for dipolar recoupling under MAS. Two blocks of $\pi$-pulse (filled rectangle) trains applied exactly every half rotor cycle on the $j$ spin is used to recouple the coherently averaged dipolar coupling Hamiltonian under MAS. In between, $\pi$-pulses are applied on the both spins to refocus the isotropic chemical shift. In this version shown, a soft $\pi$-pulse (filled hyperbola) followed by a hard pulse is applied on the $j$ spin to selectively refocus the $j$ spins with isotropic chemical shift of interest.

### 1.6 Heteronuclear dipolar recoupling

Due to the importance of measuring dipolar coupling in structure characterization in an NMR sample, it is of interest to recouple the averaged dipolar coupling Hamiltonian during MAS. Recoupling of heteronuclear dipole interactions in MAS NMR is a well-established method to measure distances $[151,150]$. Due to a favorable scaling factor and relatively low RF power requirement, one of the earlier recoupling sequences, rotational echo double resonance (REDOR) [80, 183] remains widely applied to both materials and biological samples. Since the spin part of the recoupled Hamiltonian is identical to the J-coupling Hamiltonian, a transferred sequence analogous to the solution HSQC sequence was developed soon after, and is referred to as transferred-echo double resonance (TEDOR) [92]. Here we will look at the recoupling block of the REDOR sequence, where a spin I, dipole coupled to another nuclei $S$, is getting dephased.

The recoupling block is such that there is an $\pi$ pulse applied exactly every half rotor period. Another $\pi$ pulse is applied in the middle of the recoupling block on the spin to refocus the dephased chemical shift. In addition, the sequence shown here has a selective $\pi$ pulse on the $i$ spin, followed by a hard $\pi$ pulse, this serves the additional function of selecting only those spins that fall in a
certain chemical shift range. The effect of spinning the sample at the magic angle can be better understood after a frame transformation from the laboratory frame ( $B_{0}$ field as the $z$-axis) into the rotor frame (axis of spinning as the $z$-axis), in which the heteronuclear dipolar Hamiltonian is written as:

$$
\begin{equation*}
\hat{\mathcal{H}}_{\text {hetero }}^{D D}(t)=-\frac{\mu_{0}}{2 \pi} \frac{\gamma_{i} \gamma_{j} \hbar}{r_{i j}^{3}}\left(-\frac{1}{\sqrt{2}} \sin 2 \beta \cos \left(\omega_{R} t+\gamma\right)+\frac{1}{2} \sin ^{2} \beta \cos \left(2 \omega_{R} t+2 \gamma\right)\right) \hat{S}_{z}^{i} \hat{S}_{z}^{j} \tag{1.21}
\end{equation*}
$$

In the rotor frame, the angle $\gamma$ is the initial orientation of the internuclear vector with in the rotor transverse plane, $\beta$ is the angle between the MAS axis and the internuclear vector and $\omega_{R}$ is the spinning speed. As this Hamiltonian has characteristic frequency of $\omega_{R}$ and $2 \omega_{R}$, the spatial part (the terms in brackets from equation1.21) changes sign every half rotor cycle. And integration over one rotor cycle can be shown to result in a zero Hamiltonian. During the REDOR recoupling, the two $\pi$-pulses within a rotor period manipulate the spin part of the dipolar Hamiltonian $\hat{S}_{z}^{i} \hat{S}_{z}^{j}$, changing its signs every half rotor period. This results in a non-zero Hamiltonian at the end, effectively recoupling the dipolar coupling Hamiltonian. A quantitative analysis can be shown using the average Hamiltonian theory (AHT). Such analysis is applicable when several conditions are satisfied by the pulse sequence: i) the total duration for which the sequence is applied $\tau_{c}$ is a multiple of the rotor period $\tau_{R}$ ii) The net rotation produced by each block of RF pulses is zero iii) $\tau_{c}$ is short enough, so that the internal Hamiltonians do not produce a large enough effect to change the state of the system. All are exactly true for REDOR. Importantly for AHT analysis, the Hamiltonian needs to be transformed into the interaction frame, where the RF pulses do not appear directly but rather as the time dependence of the Hamiltonian. This allows a direct observation of the effect of the pulses by integration of the toggling frame Hamiltonian over time. For REDOR, the toggling frame Hamiltonian (the effective Hamiltonian) integrated over one rotor period is:

$$
\begin{equation*}
\overline{\hat{\mathcal{H}}_{R E D O R}^{e f f}}=-\frac{\mu_{0}}{4 \pi^{2}} \frac{\gamma_{i} \gamma_{j} \hbar}{r_{i j}^{3}}(\sqrt{2} \sin 2 \beta \sin \gamma) 2 \hat{S}_{z}^{i} \hat{S}_{z}^{j} \tag{1.22}
\end{equation*}
$$

which is non-zero and results in the loss of magnetization on $i$ spin due to the incomplete refocusing of the dipolar coupling. The amount of dephased $i$ magnetization corresponds to the transverse magnetization that does not lie on the original axis after rotor period. This can be calculated as the phase angle $\Phi$ acquired over one rotor period. For a certain crystalline orientation described by

Euler angles $(\beta, \gamma)$, this phase angle is:

$$
\begin{equation*}
\Phi\left(\beta, \gamma, \tau_{R}\right)= \pm \frac{\mu_{0}}{4 \pi^{2}} \frac{\gamma_{i} \gamma_{j} \hbar}{r_{i j}^{3}} \frac{2 \sqrt{2}}{\omega_{R}} \sin 2 \beta \sin \gamma \tag{1.23}
\end{equation*}
$$

The phase angle acquired after N rotor periods is then simply $N \Phi$. This term is dependent on $\frac{1}{r_{i j}^{3}}$, thus the dephasing rate is an accurate reporter of the internuclear distance and used frequently in structure calculation. In a powder sample, the dephased $i$ spin magnetization $I_{f}$ is found by summing over all possible crystalline orientation. A good approximation based on the expansion of Bessel functions was derived previously [147] to describe the powder averaged dipolar recoupling signal under MAS, and will be discussed more in details in Chapter 5. It is important to note that the equation 1.23 does not take into account the effect of relaxation, while during the actual REDOR experiment, there is significant longitudinal relaxation. Therefore, a separate reference experiment recording the non-dephased magnetization with relaxation is required. The final REDOR parameter is the ratio of the dephased magnetization and reference magnetization. When there is multiple dephasing spins $j$, the related experiment TEDOR [92] is needed to extract the distance information in each individual dipolar coupled spin pair, by recording the chemical shift of not only the dephased $i$ spin but also the dephasing $j$ spins. The detailed analysis of the two experiments, along with an improved, more time saving pulse sequence for measuring dipolar coupling TREDOR [231] will be discussed in Chapter 5.

### 1.7 Chemical shift anisotropy recoupling in the CODEX experiment

Just like dipolar recoupling, RF pulses applied at the correct internals of the rotor period can also recouple the CSA Hamiltonian averaged out by MAS. The one to be introduced in this section is used as CSA encoding in the centerband-only detection of exchange (CODEX) experiment [97]. It is made in the spirit of REDOR, in that the dephasing of the magnetization resulted from the recoupled CSA Hamiltonian is measured. Similarly, a $\pi$-pulse train is applied every half a rotor period (Figure 1.7). At the end of the block (after the pulse train is applied for a duration of N rotor


Figure 1.7: The CODEX pulse sequence for determination of oligomeric state and internuclear distance. The sequence is shown specifically for ${ }^{19} \mathrm{~F}$ CODEX following a ${ }^{1} \mathrm{H}$ to ${ }^{19} \mathrm{~F}$ cross polarization (CP). Decoupling on the proton channel is applied throughout both the CSA recoupling blocks and the acquisition. $\pi$-pulse trains spaced by exactly half a rotor period is applied on the ${ }^{19}$ F channel for CSA encoding (1) and decoding (2). Spin diffusion based exchanged is allowed to happen during the long rotor synchronized mixing period $\tau_{m}$. The two $\pi / 2$ pulses before an after the mixing period has opposite phases so that an incomplete CSA refocusing will lead to loss of the magnetization. To ensure there is no dephasing caused by incomplete rotor cycle, both first and second parts are triggered from the same phase in MAS rotation.
periods), the phase angle acquired is

$$
\begin{equation*}
\Phi=N \int_{0}^{t_{R} / 2} \omega(t) d t \tag{1.24}
\end{equation*}
$$

with $\omega(t)$ being the dephasing frequency that depends on the strength of the CSA. For CODEX specifically, two such CSA recoupling blocks [61, 52, 97] (1 and 2 in Figure 1.7) are applied before and after a rotor synchronized long mixing time $\tau_{m}$. The $\pi / 2$ pulse sandwiching the $\tau_{m}$ has a 180 degree phase inversion. If exchange between those spins with different segmental reorientation could happen (mainly by spin diffusion), meaning that the dephasing frequencies are different between the two CSA recoupling blocks, the magnetization at the end of the pulse sequence cannot be completely refocused and leads to a net loss. The strength of the dephasing will depend on the dipolar coupling (which will affect the spin diffusion rate) during the mixing period. Effectively, this means it is possible to determine distance between spins with even the same isotropic chemical shift, making it useful in measuring inter-oligomer distance. The implication and application of this will be discussed in Chapter 4. Also similar to the analysis of REDOR, a reference spectrum is required to eliminate the effect of the longitudinal relaxation during the mixing period and the dephasing is measured as a ratio $S / S_{0}$ between the leftover magnetization $S$ and the reference magnetization $S_{0}$.

### 1.8 Thesis outline

Chapter 2 of this thesis will demonstrate the application of ${ }^{1} \mathrm{H}$-detected NMR methods in the CitA PASpc construct in both the citrate bound and citrate free state, along with functionally important structural changes upon citrate binding observed in the TM2 helix and its accompanying linker regions. Chapter 3 will introduce the ${ }^{31} \mathrm{P}$ activity assay applied to the soluble PASc-kin constructs to gain insights of the PASc dimer rearrangements on the kinase activity, and the same assay applied to a N308C mutant full length CitA with two different chemical tags for preparation of site-specific distance measurements. Chapter 4 will introduce the application of site-specific interdimer distance measurement using ${ }^{19} \mathrm{~F}$ CODEX and provide direct structural evidence for the dimer rearrangement mechanism of PASc upon citrate binding using the PASpc construct. A structural and dynamics model based on these changes observed by us in the context of CitA transmembrane signal transduction mechanism will be discussed together in Chapter6. Chapter 5 will present a new method to measure the dipolar coupling strength with MAS solid-state NMR, TREDOR.

## CHAPTER 2

## Sequence Specific Resonance Assignment of CitA Reveals a Loosening of a KK Linker with a Piston-like Pulling Motion

### 2.1 Introduction

Sequence specific assignment is the first step in the investigation of proteins with NMR. Previously[186], isolated domains available in solution from CitA (namely the PASp and PASc) have been assigned. The analysis of the chemical shifts, which are sensitive to the dihedral angles of the peptide bonds, shows that the C-terminus of PASp switches from random coil to alpha helical conformation [178] upon citrate binding. This helix is called the periplasmic helix (P-helix) [25]. It is a consensus structural feature in the stimulus transmission of HKs, and its formation is compatible with a piston motion proposed for CitA activation. This process, derived for GT CitA from the structural data of the isolated PASp domain (crystal structure and solution state NMR) and the membrane bound PASpc construct ( ${ }^{13} \mathrm{C}$-detected MAS NMR), is illustrated in Figure 2.1: as the citrate binds to the PASp domain, the $\beta$-strand scaffold "hugs" the citrate molecule and thus leads to a contraction of the C-terminus of PASp. This piston motion is also confirmed in CitA's homologous protein DcuS [145] by cysteine accessibility assay, in which the TM2 helix experiences a rigid body upward motion upon activation by fumarate binding. In addition to revealing functionally relevant structural changes in the PASp domain, the resonances of the isolated domains (both PASp and PASc) have been used solely for the chemical shift assignment of the ${ }^{13} \mathrm{C}$ detected MAS NMR spectra of the PASpc (CitA without the DHp domain)


Figure 2.1: P-helix formation at the C-terminus of PASp with citrate binding, confirmed by secondary chemical shift analysis from ${ }^{13} \mathrm{C}$-detected MAS NMR of the membrane bound PASpc construct, the secondary chemical shift analysis from solution NMR of the isolated PASp domain, and the crystal structure of the PASp domain in both the citrate bound and the citrate free state [178].
construct in liposomes. However, the drawback of "borrowing" the assignments of isolated domains is obvious: whatever is not available in the isolated domains, including the TM helices, cannot be assigned even if it is visible in the solid-state experiments. More importantly, the parts of CitA that interact with lipids might not have the same chemical shifts in the isolated constructs versus the PASpc construct, making us blind to the mechanistic insights only available from the PASpc construct. This includes the structural and dynamic features in the TM helices and their accompanying linker regions, even when these linkers can bear important functions according to mutational analysis and structural studies of PASc in the kinase BvgS [55]. In the crystal structure of the PASc domain monomer from BvgS, the overall arrangement of the N -terminal helix and the $\beta$-scaffold is similar to that observed in the WT PASc domain in CitA (Figure 3.1 B), indicating the similarity between the PASc domain of BvgS and CitA . Moreover, relevant structural changes involving the PASc domain cannot be predicted directly using the isolated PASc construct, as it does not bear an "on" or "off" state by itself. Sequence specific assignment, through which chemical shift information can be acquired $a b$ initio, becomes the prerequisite to studying the transmembrane signaling of CitA in its entirety.

Assignment of protein backbone resonances using NMR is done by a series of experiments with well defined transfers in relation to the primary sequence [10]. Specifically, assignment
strategies using ${ }^{1} \mathrm{H}$ detected MAS NMR have been developed based on the already available experiments in solution NMR [179], which employ magnetization transfers between atoms that are related in a predictable manner according to the primary sequence. The available assignment experiments available have been summarized in various literature [18, 161, 10, 91]. In MAS NMR, short dipolar coupling based transfer, typically cross polarization (CP) transfer, between hetero-nuclei is preferred instead of J-coupling based transfer due to the short $\mathrm{T}_{2}$ time with moderate MAS speed. For homo-nuclear transfers at the MAS frequency of 60 kHz or above, at which the carbon $\mathrm{T}_{2}$ becomes long enough, J-based transfers [18] are more straightforward as the RF power for carbon-carbon dipolar recoupling becomes demanding. With knowledge of the characteristic chemical shifts of $\mathrm{C} \alpha$ and $\mathrm{C} \beta$ of different amino acid and the connectivity pattern of the individual experiment, one could perform a "walk" along the sequence and place stretches of residues in the correct positions in the sequence. This is usually the most time consuming but also an indispensable step in getting atomic resolution information. The recent development in fast MAS probes (up to 100 kHz ) and high magnetic field (up to 1.2 GHz ) have increased the sensitivity and resolution of the spectra to make the assignment process less sample and time demanding. The increase in magnetic field (from 950 MHz to 1.2 GHz ) has been shown to significantly improve the spectral quality of fully protonated CitA PASpc [153] (Figure2.2). At moderate spinning (about 60 kHz ), the dilution of the proton network with sample deuteration can significantly narrow the proton linewidth by reducing the proton coupling network [232, 167]. The backbone resonance assignment presented in this chapter will be solely based on experiments with perdeuterated CitA PASpc samples at 55 kHz MAS.

Despite the technical advances, assignment of the 310 residue CitA PASpc monomer is still challenging. Though there is no theoretical size limit in using MAS NMR, the difficulty of resonance assignment increases with the size of the protein due to increased spectral complexity. In the case of CitA's TM helices, the situation is made worse as $\alpha$-helix and coils have smaller chemical shift dispersion [230], resulting in more severe spectral overlap for individual peaks to be separated. To tackle these issues, both the sequence and the topology of CitA PASpc construct are exploited. In addition to conventional sets of assignment experiments, we measure 3D correlation experiments that link sequential amide nitrogens [11], whose chemical shift dispersion is large even in coils.


Figure 2.2: Resolution and sensitivity of CitA PASpc (H)NH and (H)CH spectra are improved using the 1200 MHz instrument (red) as compared with the 950 MHz (blue). The resulting improvement in peak separation is evident in both the $(\mathrm{H}) \mathrm{NH}(\mathrm{A})$ and $(\mathrm{H}) \mathrm{CH}(\mathrm{B}, \mathrm{C})$ spectra. The expansion of the alpha region is shown side-by-side. This is especially obvious in the glycine region of the (H)NH spectra below 110 ppm . 1D proton traces (inset in A-C) reveal the resolution improvement of various isolated peaks. The aromatic carbon region of the $(\mathrm{H}) \mathrm{CH}$ spectrum (B) has a sensitivity at the 950 MHz magnet, that was too low for reliable linewidth measurement. The insets show the linewidths of selected peaks that are resolved in the 2D spectrum. The peak indicated with a (*) was used to set the base contour level to a consistent fraction of the peak intensity for each set of overlaid spectra. The topology of the protein is shown in (D) with the sensor PASp domain in red, the TM helices (TM1 and TM2) shown in green, and the PASc domain shown in blue. The $\mathrm{T}_{1}$ noise at about 3.3 and 4.7 ppm are from choline and water protons, respectively [153].

For amino acid typing, instead of relying solely on the characteristic carbon chemical shifts, we can reverse lable the amino acids isoleucine (I), value (V), phenylalanine (F) and leucine (L) (IVFL reversed labeled PASpc). To distinguish chemical shifts from the transmembrane regions (i.e TM helices) versus those from water contacting domains (PASp, PASc and water-contacting regions), solvent magnetization transfer experiments can be performed [149]. This combinatorial strategy is used to enable assignment of both the citrate bound and the citrate free state. From the chemical shifts functionally relevant conformational changes accompanying citrate binding can be tracked.

### 2.2 Materials and methods

### 2.2.1 Protein sample preparation

For producing approximately $100 \%$ deuterated, ${ }^{15} \mathrm{~N},{ }^{13} \mathrm{C}$-labeled C12A/R93A CitA PASpc, the plasmid coding for C12A/R93A CitA PASpc (Figure 2.6) was transformed into the strain C43 (DE3) (Imaxio, France). The R93A mutant was previously used in the isolated PASp domain to investigate its structure in both the citrate bound and citrate free form [178]. Without the R93A mutation, the PASp domain in GT CitA binds the citrate molecule too tightly for a citrate free state to be produced. A single colony was transferred into a 2 ml minimal medium shaking culture and step-wise adapted to $100 \% \mathrm{D}_{2} \mathrm{O}$, followed by expression in minimal medium with $100 \%$ $\mathrm{D}_{2} \mathrm{O},{ }^{15} \mathrm{~N}-\mathrm{NH}_{4} \mathrm{Cl}$ as nitrogen source and ${ }^{13} \mathrm{C}_{6}$-D-glucose as carbon source. For additional reverse labeling with isoleucine, valine, phenylalanine and leucine, $150 \mathrm{mg} / \mathrm{L} \mathrm{D}_{1} 0$-L-isoleucine, $100 \mathrm{mg} / \mathrm{L}$ $\mathrm{D}_{8}$-L-valine, $50 \mathrm{mg} / \mathrm{L} \mathrm{D}_{8}$-L-phenylalanine and $150 \mathrm{mg} / \mathrm{L} \mathrm{D}_{1} 0$-L-leucine (CORTECNET) were added to the expression culture shortly before induction. After purification with the established protocol [178] for C12A/R93A CitA PASpc and reconstitution into 1,2-dimyristoyl-sn-glycero-3phosphocholine (DMPC) and 1,2-dimyristoyl-sn-glycero-3-phosphatic acid (DMPA) liposomes (with DMPC to DMPA molar ratio of 9:1) at a lipid:protein ratio of $75: 1(\mathrm{~mol} / \mathrm{mol})$, the liposomes were taken up in 20 mM sodium phosphate, $\mathrm{pH} 6.5,5 \mathrm{mM}$ sodium citrate. The samples were packed in a Bruker 1.3 mm rotor by ultracentrifugation.


Figure 2.3: Citrate unbinds from the CitA PASpc through incubation in citrate free buffer tracked by intensity of H 96 side chain, which hydrogen bonds with citrate at the bound state (E). The loss of this hydrogen bond causes H 96 side chain to become unstructured and thus too dynamic to be detected by CP based (H)NH experiment. The intensity drops to $30 \%$ after 30 hours of incubation ( B to C ). The protein remains functional, as adding citrate to the buffer immediately restores the spectra to the bound state (D). This unbinding protocol is necessary for the residue specific assignment in the citrate free state, as it ( F , red) increases the sensitivity by $30 \%$ compared with the original protocol (F, black), using which the signals become too weak for residue-specific assignment.

The citrate free sample is made by simply incubating the citrate bound CitA PASpc sample with the citrate free buffer ( 20 mM sodium phosphate pH 6.5 ) at $40^{\circ} \mathrm{C}$ for a week. This process is monitored by tracking the intensity of the H96 side chain with 2D (H)NH spectra.

### 2.2.2 NMR spectroscopy

The NMR settings including CP powers, hard pulse powers, sweep width, inter-scan delays etc. of the assignment experiments acquired are summarized in Table 2.1 (triple labeled, perdeuterated PASpc sample in the citrate free state), Table 2.2 (triple labeled, perdeuterated PASpc sample in the citrate bound state), Table 2.3 (IVFL reverse labeled, perdeuterated PASpc sample in the citrate free state) and Table 2.4 (IVFL reverse labeled, perdeuterated PASpc sample in the citrate bound state). The powers for soft pulses are taken at the maximum value. All experiments at the field of 850 MHz were measured with a Bruker $1.3 \mathrm{~mm} \mathrm{H} / \mathrm{C} / \mathrm{D} / \mathrm{N}$ four channel probe. The experiment (H)N(CA)(CO)NH in the bound fully labeled CitA PASpc was acquired at the field of 800 MHz with a Bruker $1.3 \mathrm{~mm} \mathrm{H} / \mathrm{X} / \mathrm{Y}$ three channel probe. The sample temperature was set to 293 K adjusted with the chemical shift of water, using a cooling gas flow of $1350 \mathrm{~L} / \mathrm{h}$. Chemical shifts of ${ }^{13} \mathrm{C}$ are referenced relative to sodium trimethylsilylpropanesulfonate (DSS).

Table 2.1: NMR experiment parameters used in sequence specific assignments in the free state CitA PASpc sample.

| Spectrum | (H)NH | (H)CANH | (H)(CO)CA(CO)NH | (H)CONH | (H)CO(CA)NH |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Scans per point | 8 | 24 | 96 | 8 | 96 |
| Experimental time / h | 0.9 | 112 | 205.3 | 17.2 | 206.4 |
| Signal/noise | 85.99 | 28.22 | 10.29 | 20.85 | 15.06 |
| Field | 850 | 850 | 850 | 850 | 850 |
| Spinning frequency/Hz | 55000 | 55000 | 55000 | 55000 | 55000 |
| interscan delay /s | 1 | 1 | 1 | 1 | 1 |
| Sweep width <br> (t1) / ppm | 160 (N) | 32 (N) | 40 (N) | 40 (N) | 40 (N) |
| Max indirect evolution (t1) / ms | 14.5 (N) | 21.8 (N) | 10.1 (N) | 12.5 (N) | 12.5 (N) |
| Sweep width (t2) / ppm | 40.3 (H) | 32 (C) | 30 (C) | 18.0 (C) | 18.0 (C) |
| Max indirect evolution (t2) / ms | 30.0 (H) | 10.2 (C) | 8.6 (C) | 11.7 (C) | 11.7 (C) |
| Sweep width (t3) / ppm | N/A | 58.8 (H) | 40.3 (H) | 40.3 (H) | 40.3 (H) |
| Max indirect evolution (t3) / ms | N/A | 20.5 (H) | 30.0 (H) | 30.0 (H) | 30.0 (H) |
| Transfer I | HN (dipolar) | HCA (dipolar) | HCO (dipolar) | HCO (dipolar) | HCO (dipolar) |
| ${ }^{1} \mathrm{H}$ field / kHz | 99.4 | 95.1 | 96.3 | 100 | 100 |
| X field / kHz | 38.1 | 40.4 | 40.1 | 40.1 | 40.1 |
| Shape | $\begin{gathered} 100-80 \% \\ \text { ramp }(\mathrm{H}) \end{gathered}$ | $\begin{gathered} 85-100 \% \\ \text { ramp (H) } \end{gathered}$ | 85-100 \% ramp <br> (H) | $\begin{gathered} 85-100 \% \\ \operatorname{ramp}(\mathrm{H}) \end{gathered}$ | $\begin{gathered} 85-100 \% \\ \operatorname{ramp}(\mathrm{H}) \end{gathered}$ |
| Carrier ${ }^{13} \mathrm{C}$ | N/A | 53.7 | 173.3 | 173.8 | 173.8 |
| Time / ms | 1.15 | 6 | 3.5 | 3.5 | 3.5 |
| Transfer II | HN (dipolar) | CAN (dipolar) | COCA (scalar) | CON (dipolar) | $\begin{gathered} \text { COCA (scalar, } \\ \text { SCT) } \end{gathered}$ |
| ${ }^{1} \mathrm{H}$ field / kHz | 95.5 | N/A | N/A | N/A | N/A |
| ${ }^{13} \mathrm{C}$ field / kHz | N/A | 35.5 | N/A | 27.4 | N/A |
| ${ }^{15} \mathrm{~N}$ field / kHz | 38.1 | 29.2 | N/A | 31.6 | N/A |



| Spectrum | (H)(CA)CB(CA)NH | (H)(CA)CB(CA) (CO)NH | (H)N(CA)(CO)NH |
| :---: | :---: | :---: | :---: |
| Max indirect evolution <br> (t2) / ms | 8.8 (C) | 5.6 (C) | 9.6 (N) |
| Sweep width (t3) / <br> ppm | 58.8 (H) | 40.3 (H) | 40.3 (H) |
| Max indirect evolution (t3) / ms | 20.5 (H) | 30.0 (H) | 30.0 (H) |
| Transfer I | HCA (dipolar) | HCA (dipolar) | HN (dipolar) |
| ${ }^{1} \mathrm{H}$ field / kHz | 95.1 | 98.1 | 100 |
| X field / kHz | 40.4 | 40.1 | 38.7 |
| Shape | 85-100 \% ramp <br> (H) | 85-100 \% ramp (H) | 100-80\% ramp (H) |
| Carrier ${ }^{13} \mathrm{C}$ | 53.7 | 53.7 | N/A |
| Time / ms | 7 | 3.5 | 1.15 |
| Transfer II | CACBCA(scalar) | CACBCA(scalar) | NCA (dipolar) |
| ${ }^{1} \mathrm{H}$ field / kHz | N/A | N/A | N/A |
| ${ }^{13} \mathrm{C}$ field / kHz | N/A | N/A | 27.4 |
| ${ }^{15} \mathrm{~N}$ field / kHz | N/A | N/A | 29.4 |
| Carrier ${ }^{13} \mathrm{C}$ | 53.7 and 48 | 53.7 and 48 | 53.3 |
| Shape | N/A | N/A | Tan_ampmod_63_94.land <br> (N) |
| Time / ms | 12 | 12 | 9 |
| Transfer III | CAN (dipolar) | COCA (scalar) | CACO (scalar) |
| ${ }^{1} \mathrm{H}$ field / kHz | N/A | N/A | N/A |
| ${ }^{13} \mathrm{C}$ field / kHz | 35.5 | N/A | N/A |
| ${ }^{15} \mathrm{~N}$ field / kHz | 29.2 | N/A | N/A |
| Carrier ${ }^{13} \mathrm{C}$ | 53.3 | 173.3 and 53.3 | 53.3 and 173.3 |
| Shape | Tan_ampmod | _63_94.land ( N ) | N/A |
| Time / ms | 11 | $\begin{gathered} 6.6 \text { (1st step) } 4.6 \text { (2nd } \\ \text { step) } \end{gathered}$ | 4.6 (1st step) 6.6 (2nd step) |
| Transfer IV | NH (dipolar) | CON (dipolar) | CON (dipolar) |
| ${ }^{1} \mathrm{H}$ field / kHz | 98.1 | N/A | N/A |
| ${ }^{13} \mathrm{C}$ field / kHz | N/A | 27.4 | 27.4 |
| ${ }^{15} \mathrm{~N}$ field / kHz | 38.6 | 28.9 | 30.1 |
| Carrier ${ }^{13} \mathrm{C}$ | N/A | 173.3 | 173.3 |


| Spectrum | $(\mathrm{H})(\mathrm{CA}) \mathrm{CB}(\mathrm{CA}) \mathrm{NH}$ | (H)(CA)CB(CA) (CO)NH | (H)N(CA)(CO)NH |
| :---: | :---: | :---: | :---: |
| Shape | $\begin{gathered} 100-80 \% \text { ramp } \\ \text { (H) } \end{gathered}$ | Tan_ampmod_63_94.I and (N) | Tan_ampmod_63_94.land <br> (N) |
| Time / ms | 0.85 | 9 | 9 |
| Transfer V |  | NH (dipolar) | NH (dipolar) |
| ${ }^{1} \mathrm{H}$ field / kHz | N/A | 100 | 95.1 |
| ${ }^{13} \mathrm{C}$ field / kHz | N/A | N/A | N/A |
| ${ }^{15} \mathrm{~N}$ field / kHz | N/A | 38.1 | 38.7 |
| Carrier ${ }^{13} \mathrm{C}$ | N/A | N/A | N/A |
| Shape | N/A | 100-80\% ramp (H) | 100-80\% ramp (H) |
| Time / ms | N/A | 0.85 | 0.85 |
| Spectrum | (H)N(CO)(CA)NH | (H)COCA(N)H | $\mathrm{H}(\mathrm{H}) \mathrm{NH}$ |
| Scans per point | 128 | 72 | 8 |
| Experimental time / h | 154.9 | 158.1 | 22 |
| Signal/noise | 7.85 | 11.9 | 104.84 |
| Field | 850 | 850 | 850 |
| Spinning frequency/Hz | 55000 | 55000 | 55000 |
| interscan delay /s | 1 | 1 | 1 |
| Sweep width (t1)/ ppm | 40.0 (N) | 18.0 (CO) | 50.0 (N) |
| Max indirect evolution ( t 1 ) / ms | 9.6 (N) | 9.9 (CO) | 12.3 (N) |
| Sweep width (t2) / <br> ppm | 40.0 (N) | 30 (CA) | 15.0 (H) |
| Max indirect evolution ( t 2 ) / ms | 9.6 (N) | 8.1 (CA) | 3.5 (H) |
| Sweep width ( t 3 )/ ppm | 40.3 (H) | 40.3 (H) | 40.3 (H) |
| Max indirect evolution ( t 3 ) / ms | 30.0 (H) | 30.0 (H) | 30.0 (H) |
| Transfer I | HN (dipolar) | HCO (dipolar) | HH (NOE) |
| ${ }^{1} \mathrm{H}$ field / kHz | 100 | 96.1 | N/A |
| X field / kHz | 38.7 | 40.1 | N/A |
| Shape | $100-80 \% \text { ramp }$ <br> (H) | 85-100\% ramp (H) | N/A |
| Carrier ${ }^{13} \mathrm{C}$ | N/A | 173.3 | N/A |
| Time / ms | 1.15 | 3.5 | 100 |


| Spectrum | (H)N(CO)(CA)NH | (H)COCA(N)H | H(H)NH |
| :---: | :---: | :---: | :---: |
| Transfer II | NCO(dipolar) | COCA (scalar, SCT) | HN (dipolar) |
| ${ }^{1} \mathrm{H}$ field / kHz | N/A | N/A | 98.4 |
| ${ }^{13} \mathrm{C}$ field / kHz | 27.4 | N/A | N/A |
| ${ }^{15} \mathrm{~N}$ field / kHz | 30.1 | N/A | 40.5 |
| Carrier ${ }^{13} \mathrm{C}$ | 173.3 | 173.3 then 53.3 | N/A |
| Shape | Tan_ampmod | _63_94.land (N) | 80-100\% ramp (H) |
| Time / ms | 9 | $\begin{gathered} 6.6 \text { (1st step) } 4.6 \text { (2nd } \\ \text { step) } \end{gathered}$ | 1.15 |
| Transfer III | COCA (scalar) | CAN (dipolar) | HN (dipolar) |
| ${ }^{1} \mathrm{H}$ field / kHz | N/A | N/A | 95 |
| ${ }^{13} \mathrm{C}$ field / kHz | N/A | 27.4 | N/A |
| ${ }^{15} \mathrm{~N}$ field / kHz | N/A | 27.8 | 40.5 |
| Carrier ${ }^{13} \mathrm{C}$ | 173.3 and 53.3 | 53.3 | N/A |
| Shape | $\mathrm{N} / \mathrm{A}$ | Tan_ampmod_63_94.I and ( N ) | 100-80\% ramp (H) |
| Time / ms | 6.6 (1st step) 4.6 (2nd step) | 9 | 0.85 |
| Transfer IV | CAN (dipolar) | NH (dipolar) |  |
| ${ }^{1} \mathrm{H}$ field / kHz | N/A | 101.9 | N/A |
| ${ }^{13} \mathrm{C}$ field / kHz | 27.4 | N/A | N/A |
| ${ }^{15} \mathrm{~N}$ field / kHz | 29.4 | 38.1 | N/A |
| Carrier ${ }^{13} \mathrm{C}$ | 53.3 | N/A | N/A |
| Shape | Tan_ampmod_63_9 <br> 4.land (N) | 100-80 \% ramp (H) | N/A |
| Time / ms | 9 | 0.85 | N/A |
| Transfer V | NH (dipolar) |  |  |
| ${ }^{1} \mathrm{H}$ field / kHz | 95.1 | N/A | N/A |
| ${ }^{13} \mathrm{C}$ field / kHz | N/A | $\mathrm{N} / \mathrm{A}$ | N/A |
| ${ }^{15} \mathrm{~N}$ field / kHz | 38.7 | N/A | N/A |
| Carrier ${ }^{13} \mathrm{C}$ | N/A | N/A | N/A |
| Shape | 100-80 \% ramp <br> (H) | N/A | N/A |
| Time / ms | 0.85 | N/A | N/A |

Table 2.2: NMR experiment parameters used in sequence specific assignments in the bound state CitA PASpc sample.

| Spectrum | (H) NH | (H)CANH | $(\mathrm{H})(\mathrm{CO}) \mathrm{CA}(\mathrm{CO}) \mathrm{NH}$ | (H)CONH | (H)CO(CA)NH |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Scans per point | 64 | 8 | 56 | 24 | 64 |
| Experimental time / h | 15.9 | 57.6 | 131.4 | 61.9 | 144.9 |
| Signal/noise | 232 | 20.64 | 12.65 | 22.99 | 8.57 |
| Field | 850 | 850 | 850 | 850 | 850 |
| Spinning frequency/Hz | 55000 | 55000 | 55000 | 55000 | 55000 |
| interscan delay /s | 3.5 | 2.5 | 1 | 1 | 0.74 |
| Sweep width <br> (t1) / ppm | 120.0 (N) | 36 (N) | 36 (N) | 34(N) | 34(N) |
| Max indirect evolution (t1) / ms | 24.8 (N) | 17.4 (N) | 15.5 (N) | 18.4 (N) | 18.4 (N) |
| Sweep width (t2) / ppm | 40.8 (H) | 32 (C) | 32 (C) | 16.0 (C) | 16.0 (C) |
| Max indirect evolution (t2) / ms | 29.5 (H) | 7.0 (C) | 6.4 (C) | 12.6 (C) | 12.6 (C) |
| Sweep width (t3) / ppm | N/A | 58.8 (H) | 58.8 (H) | 58.8 (H) | 58.8 (H) |
| Max indirect evolution (t3) / ms | N/A | 20.5 (H) | 20.5 (H) | 20.5 (H) | 20.5 (H) |
| Transfer I | HN (dipolar) | HCA (dipolar) | HCO (dipolar) | HCO (dipolar) | HCO (dipolar) |
| ${ }^{1} \mathrm{H}$ field / kHz | 96.4 | 94.35 | 93.1 | 91.8 | 94.1 |
| X field / kHz | 70.7 | 40 | 40 | 39.8 | 40.1 |
| Shape | $\begin{gathered} 85-100 \% \\ \text { ramp (H) } \end{gathered}$ | $\begin{gathered} 85-100 \% \\ \text { ramp (H) } \end{gathered}$ | 85-100 \% ramp <br> (H) | $\begin{gathered} 85-100 \% \\ \text { ramp (H) } \end{gathered}$ | $\begin{gathered} 85-100 \% \\ \text { ramp (H) } \end{gathered}$ |
| Carrier ${ }^{13} \mathrm{C}$ |  | 53.7 | 173.3 | 173.8 | 173.8 |
| Time / ms | 1.2 | 4 | 5 | 4 | 4.2 |
| Transfer II | HN (dipolar) | CAN (dipolar) | COCA (scalar) | CON (dipolar) | COCA (scalar) |
| ${ }^{1} \mathrm{H}$ field / kHz | 96.4 | N/A | N/A | N/A | N/A |
| ${ }^{13} \mathrm{C}$ field $/ \mathrm{kHz}$ | N/A | 34.35 | N/A | 34.4 | N/A |
| ${ }^{15} \mathrm{~N}$ field / kHz | 70.7 | 30.61 | N/A | 31.5 | N/A |
| Carrier ${ }^{13} \mathrm{C}$ | N/A | 53.7 | 173.3 and 53.3 | 173.8 | 173.8 and 53.3 |


| Spectrum | (H)NH |  | (H)CANH | (H)(CO)CA(CO)NH | (H)CONH | (H)CO(CA)NH |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Shape | $\begin{gathered} 80-100 \% \\ \text { ramp (H) } \end{gathered}$ |  | Tan_ampmod _63_94.land <br> (N) | N/A | Tan_ampmod_ 63_94.land (N) | N/A |
| Time / ms | 1.2 |  | 13 | 15 | 13 | 7.46 |
| Transfer III | NH (dipolar) |  |  | CON (dipolar) | NH (dipolar) | CAN (dipolar) |
| ${ }^{1} \mathrm{H}$ field / kHz | N/A |  | 96.45 | N/A | 95.1 | N/A |
| ${ }^{13} \mathrm{C}$ field / kHz | N/A |  | N/A | 34.6 | N/A | 34.9 |
| ${ }^{15} \mathrm{~N}$ field / kHz | N/A |  | 39.41 | 32 | 38.7 | 30.1 |
| Carrier ${ }^{13} \mathrm{C}$ | N/A |  | N/A | 173.3 | N/A | 53.3 |
| Shape | N/A |  | $\begin{gathered} 100-80 \% \\ \operatorname{ramp}(\mathrm{H}) \end{gathered}$ | $\begin{gathered} \text { Tan_ampmod_63_ } \\ \text { 94.land (N) } \end{gathered}$ | $\begin{gathered} 100-80 \% \\ \operatorname{ramp}(\mathrm{H}) \end{gathered}$ | Tan_ampmod_ 63_94.land (N) |
| Time / ms | N/A |  | 1.2 | 11.5 | 0.85 | 13 |
| Transfer IV | NH (dipolar) |  |  |  |  | NH (dipolar) |
| ${ }^{1} \mathrm{H}$ field / kHz | N/A |  | N/A | 96.45 | N/A | 99.2 |
| ${ }^{13} \mathrm{C}$ field / kHz | N/A |  | N/A | N/A | N/A | N/A |
| ${ }^{15} \mathrm{~N}$ field / kHz | N/A |  | N/A | 39.41 | N/A | 38.7 |
| Carrier ${ }^{13} \mathrm{C}$ | N/A |  | N/A | N/A | N/A | N/A |
| Shape | N/A |  | N/A | 100-80 \% ramp <br> (H) | N/A | $\begin{gathered} 100-80 \% \\ \operatorname{ramp}(\mathrm{H}) \end{gathered}$ |
| Time / ms | N/A |  | N/A | 1.15 | N/A | 0.7 |
| Spectrum |  | (H)(CA)CB(CA)NH |  | $\begin{gathered} (\mathrm{H})(\mathrm{CA}) \mathrm{CB}(\mathrm{CA}) \\ (\mathrm{CO}) \mathrm{NH} \end{gathered}$ | (H)N(CA)(CO)NH |  |
| Scans per point |  |  | 48 | 48 | 88 |  |
| Experimental time / h |  |  | 296.3 | 269.3 | 262.9 |  |
| Signal/noise |  |  | N/A | N/A |  | 4.81 |
| Field |  |  | 850 | 850 |  | 80 |
| Spinning frequency/Hz |  |  | 55000 | 55000 |  | 000 |
| interscan delay /s |  |  | 1 | 1 |  | 1 |
| Sweep width (t1) / ppm |  |  | 34(N) | 34(N) |  | 0 (N) |
| Max indirect evolution ( t 1 ) / ms |  |  | 18.4 (N) | 17.4 (N) |  | 5 (N) |
| Sweep width (t2) / ppm |  |  | 70.0 (C) | 70.0 (C) |  | 0 (N) |
| Max indirect evolution (t2) / ms |  |  | 6.7 (C) | 6.6 (C) |  | 1 (N) |


| Spectrum | $(\mathrm{H})(\mathrm{CA}) \mathrm{CB}(\mathrm{CA}) \mathrm{NH}$ | (H)(CA)CB(CA) (CO)NH | (H)N(CA)(CO) NH |
| :---: | :---: | :---: | :---: |
| Sweep width (t3) / ppm | 58.8 (H) | 58.8 (H) | 30.1 (H) |
| Max indirect evolution (t3) / ms | 20.5 (H) | 20.5 (H) | 21.3 (H) |
| Transfer I | HCA (dipolar) | HCA (dipolar) | HN (dipolar) |
| ${ }^{1} \mathrm{H}$ field / kHz | 94.7 | 94.4 | 104.2 |
| X field / kHz | 40 | 38.7 | 39.1 |
| Shape | $85-100 \% \text { ramp }$ <br> (H) | 85-100\% ramp (H) | 80-100\% ramp (H) |
| Carrier ${ }^{13} \mathrm{C}$ | 53.7 | 53.7 | N/A |
| Time / ms | 4 | 4 | 1 |
| Transfer II | CACBCA(scalar) | CACBCA(scalar) | NCA (dipolar) |
| ${ }^{1} \mathrm{H}$ field / kHz | N/A | N/A | N/A |
| ${ }^{13} \mathrm{C}$ field / kHz | N/A | N/A | 20.9 |
| ${ }^{15} \mathrm{~N}$ field / kHz | N/A | N/A | 43.7 |
| Carrier ${ }^{13} \mathrm{C}$ | 53.7 and 48 | 53.7 and 48 | 53.3 |
| Shape | N/A | N/A | Tan_ampmod_63_94.land <br> (N) |
| Time / ms | 18.56 | 18.56 | 13 |
| Transfer III | CAN (dipolar) | COCA (scalar) | CACO (scalar) |
| ${ }^{1} \mathrm{H}$ field / kHz | N/A | N/A | N/A |
| ${ }^{13} \mathrm{C}$ field / kHz | 34.8 | N/A | N/A |
| ${ }^{15} \mathrm{~N}$ field / kHz | 30.6 | N/A | N/A |
| Carrier ${ }^{13} \mathrm{C}$ | 53.7 | 173.3 and 53.3 | 53.3 and 173.3 |
| Shape | Tan_ampmod | _63_94.land (N) | N/A |
| Time / ms | 13 | $\begin{aligned} & 7.2 \text { (1st step) } 6.4 \text { (2nd } \\ & \text { step) } \end{aligned}$ | 6.4 (1st step) 7.2 (2nd step) |
| Transfer IV | NH (dipolar) | CON (dipolar) | CON (dipolar) |
| ${ }^{1} \mathrm{H}$ field / kHz | 95.4 | N/A | N/A |
| ${ }^{13} \mathrm{C}$ field / kHz | N/A | 34.4 | 18.4 |
| ${ }^{15} \mathrm{~N}$ field / kHz | 39.4 | 30.6 | 46.5 |
| Carrier ${ }^{13} \mathrm{C}$ | N/A | 173.3 | 173.3 |
| Shape | $100-80 \% \text { ramp }$ <br> (H) | Tan_ampmod_63_94.I and ( N ) | Tan_ampmod_63_94.land <br> (N) |


| Spectrum | (H)(CA)CB(CA)NH | $(\mathrm{H})(\mathrm{CA}) \mathrm{CB}(\mathrm{CA})$ (CO)NH | (H)N(CA)(CO)NH |
| :---: | :---: | :---: | :---: |
| Time / ms | 1.15 | 13 | 13 |
| Transfer V |  | NH (dipolar) | NH (dipolar) |
| ${ }^{1} \mathrm{H}$ field / kHz | N/A | 96.4 | 95.6 |
| ${ }^{13} \mathrm{C}$ field / kHz | N/A | N/A | N/A |
| ${ }^{15} \mathrm{~N}$ field / kHz | N/A | 39.4 | 39.1 |
| Carrier ${ }^{13} \mathrm{C}$ | N/A | N/A | N/A |
| Shape | N/A | 100-80\% ramp (H) | 100-80\% ramp (H) |
| Time / ms | N/A | 1.15 | 0.6 |
| Spectrum | (H)N(CO)(CA)NH | (H)COCA(N)H | $\mathrm{H}(\mathrm{H}) \mathrm{NH}$ |
| Scans per point | 144 | 64 | 16 |
| Experimental time / h | 338.6 | 159 | 102.4 |
| Signal/noise | 11.19 | 13.53 | 66.4 |
| Field | 850 | 850 | 850 |
| Spinning frequency/ Hz | 55000 | 55000 | 55000 |
| interscan delay /s | 1 | 1 | 1 |
| Sweep width (t1)/ <br> ppm | 36.0 (N) | 16.0 (CO) | 60.0 (N) |
| Max indirect evolution <br> (t1)/ms | 14.8 (N) | 12.3 (CO) | 24.8 (N) |
| Sweep width (t2)/ ppm | 36.0 (N) | 32 (CA) | 15.0 (H) |
| Max indirect evolution <br> (t2) / ms | 14.8 (N) | 7.6 (CA) | 3.5 (H) |
| Sweep width (t3)/ ppm | 58.8 (H) | 58.8 (H) | 40.8 (H) |
| Max indirect evolution (t3) / ms | 20.5 (H) | 20.5 (H) | 29.5 (H) |
| Transfer I | HN (dipolar) | HCO (dipolar) | HH (NOE) |
| ${ }^{1} \mathrm{H}$ field / kHz | 96 | 91.5 | N/A |
| X field / kHz | 38.7 | 39.8 | N/A |
| Shape | 100-80 \% ramp <br> (H) | 85-100\% ramp (H) | N/A |
| Carrier ${ }^{13} \mathrm{C}$ | N/A | 173.3 | N/A |
| Time / ms | 1.15 | 4 | 100 |
| Transfer II | NCO(dipolar) | COCA (scalar, SCT) | HN (dipolar) |


| Spectrum | (H)N(CO)(CA)NH | (H)COCA(N)H | H(H)NH |
| :---: | :---: | :---: | :---: |
| ${ }^{1} \mathrm{H}$ field / kHz | N/A | N/A | 93.6 |
| ${ }^{13} \mathrm{C}$ field / kHz | 27.1 | N/A | N/A |
| ${ }^{15} \mathrm{~N}$ field / kHz | 37.7 | N/A | 38.7 |
| Carrier ${ }^{13} \mathrm{C}$ | 173.3 | 173.3 then 53.3 | N/A |
| Shape | Tan_ampmod | _63_94.land (N) | 100-80\% ramp (H) |
| Time / ms | 13 | $\begin{gathered} 7.2 \text { (1st step) } 6.4 \text { (2nd } \\ \text { step) } \end{gathered}$ | 0.7 |
| Transfer III | COCA (scalar) | CAN (dipolar) | HN (dipolar) |
| ${ }^{1} \mathrm{H}$ field / kHz | N/A | N/A | 94.2 |
| ${ }^{13} \mathrm{C}$ field / kHz | N/A | 35 | N/A |
| ${ }^{15} \mathrm{~N}$ field / kHz | N/A | 29.7 | 38.7 |
| Carrier ${ }^{13} \mathrm{C}$ | 173.3 and 53.3 | N/A | N/A |
| Shape | N/A | Tan_ampmod_63_94.I and ( N ) | 100-80\% ramp (H) |
| Time / ms | 7.2 (1st step) 6.4 (2nd step) | $12.5$ | 0.6 |
| Transfer IV | CAN (dipolar) | NH (dipolar) |  |
| ${ }^{1} \mathrm{H}$ field / kHz | N/A | 95.1 | N/A |
| ${ }^{13} \mathrm{C}$ field / kHz | 35.1 | N/A | N/A |
| ${ }^{15} \mathrm{~N}$ field / kHz | 30.1 | 38.7 | N/A |
| Carrier ${ }^{13} \mathrm{C}$ | 53.3 | N/A | N/A |
| Shape | $\begin{array}{\|c} \text { Tan_ampmod_63_9 } \\ \text { 4.land (N) } \end{array}$ | $100-80 \% \text { ramp (H) }$ | N/A |
| Time / ms | 12.5 | $0.85$ | N/A |
| Transfer V | NH (dipolar) |  |  |
| ${ }^{1} \mathrm{H}$ field / kHz | 95.1 | N/A | N/A |
| ${ }^{13} \mathrm{C}$ field / kHz | N/A | N/A | N/A |
| ${ }^{15} \mathrm{~N}$ field / kHz | 38.7 | N/A | N/A |
| Carrier ${ }^{13} \mathrm{C}$ | N/A | N/A | N/A |
| Shape | 100-80 \% ramp <br> (H) | N/A | N/A |
| Time / ms | 0.85 | N/A | N/A |

Table 2.3: NMR experiment parameters used in sequence specific assignments in the free state CitA PASpc sample with IVFL reverse labeling.

| Spectrum | (H) NH | (H)CANH | (H)(CO)CA(CO)NH |
| :---: | :---: | :---: | :---: |
| Scans per point | 136 | 24 | 32 |
| Experimental time / h | 15.1 | 58.8 | 117.3 |
| Signal/noise | 226.17 | 21.43 | N/A |
| Field | 850 | 850 | 850 |
| Spinning frequency/Hz | 55000 | 55000 | 55000 |
| interscan delay /s | 1 | 1 | 1 |
| Sweep width (t1) / ppm | 160 (N) | 40 (N) | 40(N) |
| Max indirect evolution <br> ( t 1 ) / ms | 14.5 (N) | 11.0 (N) | 9.6 (N) |
| Sweep width (t2) / ppm | 40.3 (H) | 30 (C) | 84 (C) |
| Max indirect evolution (t2) / ms | 30.0 (H) | 9.0 (C) | 5.6 (C) |
| Sweep width (t3) / ppm | N/A | 40.3 (H) | 40.3 (H) |
| Max indirect evolution ( t 3 ) / ms | N/A | 30.0 (H) | 30.0 (H) |
| Transfer I | HN (dipolar) | HCA (dipolar) | HCA (dipolar) |
| ${ }^{1} \mathrm{H}$ field / kHz | 98.2 | 100.9 | 103.6 |
| X field / kHz | 38.1 | 40.1 | 40.1 |
| Shape | 100-80\% ramp (H) | 85-100\% ramp (H) | 85-100\% ramp (H) |
| Carrier ${ }^{13} \mathrm{C}$ | N/A | 53.7 | 53.7 |
| Time / ms | 1.15 | 3.5 | 3.5 |
| Transfer II | HN (dipolar) | CAN (dipolar) | CACBCA(scalar) |
| ${ }^{1} \mathrm{H}$ field / kHz | 94.5 | N/A | N/A |
| ${ }^{13} \mathrm{C}$ field / kHz | N/A | 27.4 | N/A |
| ${ }^{15} \mathrm{~N}$ field / kHz | 38.1 | 26.6 | N/A |
| Carrier ${ }^{13} \mathrm{C}$ | $\mathrm{N} / \mathrm{A}$ | $53.7$ | 53.7 and 48 |
| Shape | 100-80\% ramp (H) | Tan_ampm | 63_94.land (N) |
| Time / ms | 0.8 | 9 | $6$ |
| Transfer III |  | NH (dipolar) | CAN (dipolar) |
| ${ }^{1} \mathrm{H}$ field / kHz | N/A | 98.1 | N/A |


| Spectrum | $(\mathrm{H}) \mathrm{NH}$ | $(\mathrm{H}) \mathrm{CANH}$ | $(\mathrm{H})(\mathrm{CO}) \mathrm{CA}(\mathrm{CO}) \mathrm{NH}$ |
| :---: | :---: | :---: | :---: |
| ${ }^{13} \mathrm{C}$ field $/ \mathrm{kHz}$ | $\mathrm{N} / \mathrm{A}$ | $\mathrm{N} / \mathrm{A}$ | 27.4 |
| ${ }^{15} \mathrm{~N}$ field $/ \mathrm{kHz}$ | $\mathrm{N} / \mathrm{A}$ | 38.1 | 26.6 |
| Carrier ${ }^{13} \mathrm{C}$ | $\mathrm{N} / \mathrm{A}$ | $\mathrm{N} / \mathrm{A}$ | 53.3 |
| Shape | $\mathrm{N} / \mathrm{A}$ | $100-80 \%$ ramp $(\mathrm{H})$ | Tan_ampmod_63_94.land <br> $(\mathrm{N})$ |
| Time $/ \mathrm{ms}$ | $\mathrm{N} / \mathrm{A}$ | 0.85 | 9 |
| Transfer IV | $\mathrm{N} / \mathrm{A}$ | NH (dipolar) |  |
| ${ }^{1} \mathrm{H}$ field $/ \mathrm{kHz}$ | $\mathrm{N} / \mathrm{A}$ | 97.2 |  |
| ${ }^{13} \mathrm{C}$ field $/ \mathrm{kHz}$ | $\mathrm{N} / \mathrm{A}$ | $\mathrm{N} / \mathrm{A}$ | $\mathrm{N} / \mathrm{A}$ |
| ${ }^{15} \mathrm{~N}$ field $/ \mathrm{kHz}$ | $\mathrm{N} / \mathrm{A}$ | $\mathrm{N} / \mathrm{A}$ | 38.1 |
| Carrier ${ }^{13} \mathrm{C}$ | $\mathrm{N} / \mathrm{A}$ | $\mathrm{N} / \mathrm{A}$ | $\mathrm{N} / \mathrm{A}$ |
| Shape |  | $\mathrm{N} / \mathrm{A}$ | $100-80 \%$ ramp $(\mathrm{H})$ |
| Time $/ \mathrm{ms}$ |  | 0.85 |  |

Table 2.4: NMR experiment parameters used in sequence specific assignments in the bound state CitA PASpc sample with IVFL reverse labeling.

| Spectrum | (H) NH | (H)CANH | (H)(CO)CA(CO)NH | (H)(CA)CB(CA)NH | $\begin{gathered} (\mathrm{H})(\mathrm{CA}) \mathrm{CB}(\mathrm{CA}) \\ (\mathrm{CO}) \mathrm{NH} \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Scans per point | 80 | 16 | 64 | 32 | 72 |
| Experimental time / h | 6.2 | 85.3 | 153.5 | 158.4 | 337.9 |
| Signal/noise | 181.46 | 21.65 | 10.86 | N/A | N/A |
| Field | 850 | 850 | 850 | 850 | 850 |
| Spinning frequency/Hz | 55000 | 55000 | 55000 | 55000 | 55000 |
| interscan delay /s | 1 | 2 | 1 | 1 | 1 |
| Sweep width <br> (t1) / ppm | 120 (N) | 36 (N) | 36 (N) | 36(N) | 34(N) |
| Max indirect evolution (t1) / ms | 13.5 (N) | 16.1 (N) | 14.5 (N) | 14.5 (N) | 15.0 (N) |
| Sweep width (t2) / ppm | 40.8 (H) | 32 (C) | 32 (C) | 70.0 (C) | 70 (C) |
| Max indirect evolution (t2) / ms | 29.5 (H) | 7.0 (C) | 7.0 (C) | 6.6 (C) | 6.4 (C) |
| Sweep width <br> (t3) / ppm | N/A | 58.8 (H) | 58.8 (H) | 58.8 (H) | 58.8 (H) |
| Max indirect evolution (t3) / ms | N/A | 20.5 (H) | 20.5 (H) | 20.5 (H) | 20.5 (H) |
| Transfer I | HN <br> (dipolar) | HCA <br> (dipolar) | HCO (dipolar) | HCA (dipolar) | HCA (dipolar) |
| ${ }^{1} \mathrm{H}$ field / kHz | 96 | 92.9 | 82.6 | 90.7 | 87.3 |
| X field / kHz | 38.1 | 41 | 41 | 41 | 37.7 |
| Shape | $\begin{gathered} 100-80 \% \\ \text { ramp (H) } \end{gathered}$ | $\begin{gathered} 85-100 \% \\ \text { ramp (H) } \end{gathered}$ | 85-100 \% ramp <br> (H) | 85-100 \% ramp <br> (H) | $\begin{gathered} 85-100 \% \\ \text { ramp (H) } \end{gathered}$ |
| Carrier ${ }^{13} \mathrm{C}$ |  | 53.7 | 173.3 | 53.7 | 53.7 |
| Time / ms | 1 | 6 | 6 | 5.5 | 4 |
| Transfer II | HN (dipolar) | CAN (dipolar) | COCA (scalar) | CACBCA(scalar) | CACBCA(scal ar) |
| ${ }^{1} \mathrm{H}$ field / kHz | 95.4 | N/A | N/A | N/A | N/A |
| ${ }^{13} \mathrm{C}$ field / kHz | N/A | 36 | N/A | N/A | N/A |


| Spectrum | (H) NH | (H)CANH | (H)(CO)CA(CO)NH | (H)(CA)CB(CA)NH | $\begin{gathered} (\mathrm{H})(\mathrm{CA}) \mathrm{CB}(\mathrm{CA}) \\ (\mathrm{CO}) \mathrm{NH} \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| ${ }^{15} \mathrm{~N}$ field / kHz | 38.1 | 28.4 | N/A | N/A | N/A |
| Carrier ${ }^{13} \mathrm{C}$ | N/A | 53.7 | 173.3 and 53.3 | 53.7 and 48 | 53.7 and 48 |
| Shape | $\begin{array}{\|l\|} \hline 100-80 \% \\ \operatorname{ramp}(H) \end{array}$ | Tan_ampm | od_63_94.land (N) | N/A | N/A |
| Time / ms | 0.8 | 11 | 15.6 | 18.4 | 18.4 |
| Transfer III |  | $\begin{gathered} \mathrm{NH} \\ \text { (dipolar) } \end{gathered}$ | CON (dipolar) | CAN (dipolar) | COCA (scalar) |
| ${ }^{1} \mathrm{H}$ field / kHz | N/A | 95.4 | N/A | N/A | N/A |
| ${ }^{13} \mathrm{C}$ field / kHz | N/A | N/A | 35.4 | 36 | N/A |
| ${ }^{15} \mathrm{~N}$ field / kHz | N/A | 38.1 | 31 | 28.9 | N/A |
| Carrier ${ }^{13} \mathrm{C}$ | N/A | N/A | 173.3 | 53.3 | 173.3 and 53.3 |
| Shape | N/A | $\begin{gathered} 100-80 \% \\ \operatorname{ramp}(\mathrm{H}) \end{gathered}$ | Tan_ampmod_63 94.land (N) | Tan_ampmod_63 | 3_94.land (N) |
| Time / ms | N/A | 1.15 | 11 | 11 | 15.6 |
| Transfer IV |  |  | NH (dipolar) | NH (dipolar) | CON (dipolar) |
| ${ }^{1} \mathrm{H}$ field / kHz | N/A | N/A | 92.2 | 89.6 | N/A |
| ${ }^{13} \mathrm{C}$ field / kHz | N/A | N/A | N/A | N/A | 33.5 |
| ${ }^{15} \mathrm{~N}$ field / kHz | N/A | N/A | 38.1 | 38.1 | 30.3 |
| Carrier ${ }^{13} \mathrm{C}$ | N/A | N/A | N/A | N/A | 173.3 |
| Shape | N/A | N/A | $\begin{gathered} 100-80 \% \text { ramp } \\ \text { (H) } \end{gathered}$ | $100-80 \% \text { ramp }$ (H) | Tan_ampmod_ 63_94.land (N) |
| Time / ms | N/A | N/A | 1.15 | 0.8 | 13 |
| Transfer V |  |  |  |  | NH (dipolar) |
| ${ }^{1} \mathrm{H}$ field / kHz | N/A | N/A | N/A | N/A | 88.7 |
| ${ }^{13} \mathrm{C}$ field / kHz | N/A | N/A | N/A | N/A | N/A |
| ${ }^{15} \mathrm{~N}$ field / kHz | N/A | N/A | N/A | N/A | 38.1 |
| Carrier ${ }^{13} \mathrm{C}$ | N/A | N/A | N/A | N/A | N/A |
| Shape | N/A | N/A | N/A | N/A | $\begin{gathered} 100-80 \% \\ \operatorname{ramp}(\mathrm{H}) \end{gathered}$ |
| Time / ms | N/A | N/A | 0.85 | N/A | 0.85 |

### 2.2.3 Automated assignment with FLYA

The peak lists extracted from the assignment experiments except for the lipid transfer $\mathrm{H}(\mathrm{H}) \mathrm{NH}$ spectrum from the deuterated triple labeled CitA PASpc and deuterated IVFL reverse labeled CitA

PASpc samples can be used in automated assignment by FLYA [126], which is an evolution algorithm based program. The addition of peak lists from IVFL reverse labeled spectra did not improve the results of the automated assignment, but aided in confirming the assignments, especially those in the transmembrane regions during the later step of the manual assignment (an example of manual assignment based on $\mathrm{C} \alpha, \mathrm{C} \beta$, and linking amide nitrogen is shown in Figure 2.10).

### 2.2.4 Secondary chemical shift calculation and torsion angle prediction with TALOS-N

The secondary chemical shift of a particular residue based on $\mathrm{C} \alpha$ and $\mathrm{C} \beta$ shifts are calculated with the following equation, after deuterium shift correction [135].

$$
\begin{equation*}
\Delta \delta_{i}=\left(\delta_{C \alpha}^{i}-\delta_{C \alpha}^{c o i l}\right)-\left(\delta_{C \beta}^{i}-\delta_{C \beta}^{c o i l}\right), \tag{2.1}
\end{equation*}
$$

where $\delta$ is the chemical shift. The random coil chemical shifts were taken from literature [188]. The chemical shifts from the sequence specific assignment can be put into TALOS-N [193] for residue specific torsion angle prediction. Only TALOS-N "strong" predictions (Table B. 4 and B.3) were included for structural model calculation with CYANA [84].

### 2.3 Results and Discussion

### 2.3.1 $\quad{ }^{1} \mathrm{H}$-detected-experiment based sequence specific assignments increase the completeness of the chemical shift assignment in CitA PASpc

The sensitivity gain, the additional proton dimension and the short experimental time of ${ }^{1} \mathrm{H}$ detected sequence specific assignment together improve the completeness of the assignment in CitA PASpc. The production of the citrate free sample from the citrate bound sample is crucial to get high enough sensitivity (increase in the sensitivity of the (H)NH spectra by $130 \%$ )(Figure $2.3, \mathrm{~F}$ ) in the citrate free state to perform residue specific assignment. When citrate dissociates from the PASp domain, the hydrogen bond between H 96 and the citrate is broken (Figure 2.3, E), and H96 becomes unstructured, thus losing its visibility in the solid-state spectrum. This allows


Figure 2.4: Automated assignment using FLYA with ${ }^{1} \mathrm{H}$-detected experiments based sequence specific assignments in the free (A) and bound (B) state of CitA PASpc. The dark blue shows assignment that is the same in $90 \%$ of the runs. FLYA could assign most of PASp in the bound state with certainty but only a small fraction of the residues in the free state.
monitoring of the unbinding process. The intensity of the H 96 side chain resonance in the (H)NH spectra decays to $30 \%$ after just 30 hours of incubation (Figure 2.3A to C). It should be noted that the protein did not denature during the whole process, as the unbound PASpc can be reversed to the bound state by simply supplementing the buffer with 5 mM sodium citrate (Figure 2.3D). 76\% of the residues in the free state and $65 \%$ of residues in the bound state can be manually assigned and, this corresponds roughly to $61.1 \%$ and $64 \%$ of the assignable peaks from all peaks (H)CANH spectra of the citrate free and citrate bound state of the PASpc construct, respectively. Using ${ }^{1} \mathrm{H}-$ detection, the total percentage of assigned resonances increased by $26 \%$ in the free state and $14 \%$ in the bound state (Table 2.5) compared with ${ }^{13} \mathrm{C}$-detection. This gain mainly comes from the resonance assignment of the TM helices, which was not available before using assignment transfer from the isolated domains. There is no major difference between the chemical shifts assigned with ${ }^{1} \mathrm{H}$ detection and that with ${ }^{13} \mathrm{C}$ detection. The PASc domain in the citrate bound state, however, has fewer assignments with ${ }^{1} \mathrm{H}$-detection than ${ }^{13} \mathrm{C}$-detection. This might be caused by a more rigorous process with ${ }^{1} \mathrm{H}$-detection versus the simple chemical shift transfer with ${ }^{13} \mathrm{C}$-detection, as all resonances assigned need to satisfy the magnetization transfer pathway of the assignment experiments. Upon citrate binding, the overall NMR visibility of the PASp domain increased from 78\% to $93 \%$, while that of the PASc domain dropped from $80 \%$ to $38 \%$ (Table 2.5). The same trend was observed with ${ }^{13} \mathrm{C}$-detection between the citrate free and the citrate bound state (in PASp, the assignment increased from $70 \%$ to $86 \%$; in PASc, it decreased from $59 \%$ to $45 \%$ ). The visibility of resonances in dipolar coupling transfer based experiments is highly dependent on the dynamics of the protein, because fast regime (in ns scale) and large amplitude motions reduce the magnitude of anisotropic interaction, which is crucial for CP transfer [222]. The direct interpretation of a lower NMR visibility is protein dynamics. So the citrate produces a "see-saw" type of dynamics change in PASp and PASc: it stabilizes the PASp and makes the PASc more flexible.

Citrate binding causes large chemical shift perturbation in the (H)CANH spectrum (Figure 2.5), as it induces large local and global structural differences and changes in the hydrogen bond network [186]. This can be observed in the large chemical shift changes between the two states. The chemical shift perturbation in the isolated PASp domain produced by citrate binding is mainly observed [178] in the $\beta$-scaffold of PASp. The major loop of PASp between residue L98 and I120 has in-


Figure 2.5: $\mathrm{N}-\mathrm{C} \alpha$ projection from 3D $(\mathrm{H}) \mathrm{CANH}$ spectrum of the citrate free (A-C) and citrate bound state ( $\mathrm{D}-\mathrm{E}$ ). The assignment is mapped onto the spectra. The citrate bound state has more isolated peaks than the citrate free state. All resonances from the assignment of the two state are included in Table B. 1 and Table B.2.

Table 2.5: Fraction of assigned residues in the PASp, TM and PASc domains in the CitA PASpc free and bound state with ${ }^{1} \mathrm{H}$-detected and ${ }^{13} \mathrm{C}$-detected MAS NMR experiments. Other than in the PASc domain in the bound state, ${ }^{1} \mathrm{H}$-detection increases the percentage of assigned residues in both free and bound state compared with ${ }^{13} \mathrm{C}$-detection.

|  | Free |  | Bound |  |
| :---: | :---: | :---: | :---: | :---: |
| Domain | ${ }^{1} \mathrm{H}$-detected | ${ }^{13}$ C-detected | ${ }^{1} \mathrm{H}$-detected | ${ }^{13} \mathrm{C}$-detected |
| PASp (31-160) | $78 \%$ | $70 \%$ | $93 \%$ | $86 \%$ |
| TM I (1-30) \& | $65 \%$ | $0 \%$ | $55 \%$ | $0 \%$ |
| TM II (161-199) | $80 \%$ | $59 \%$ | $38 \%$ | $45 \%$ |
| PASc (200-309) | $80 \%$ | $50 \%$ | $65 \%$ | $51 \%$ |
| Total | $76 \%$ |  |  |  |

creased visibility in the citrate bound state, as it forms the cradle for the citrate after binding. The opposite trend is observed in PASc. The NMR visibility of both the major loop between V233 and A272 and the $\beta$-scaffold decreased after citrate binding.

### 2.3.2 Reverse labeling and $\mathbf{H}(\mathbf{H}) \mathrm{NH}$ solvent transfer experiment confirm assignment in the TM helices

The biochemical properties and environment of the TM helices can be used to confirm their resonance assignments. The CitA TM helices have an over-representation of bulky amino acids compared with the cytosolic domains, namely the amino acids isoleucine, valine, phenylalanine and leucine. The range of $\mathrm{C} \alpha$ and $\mathrm{C} \beta$ chemical shifts in these residues is similar to that of aspartate and glutamate which are abundant in the PASp and PASc domains. To untangle this ambiguity, we reverse labeled I, V, F, L to confirm the residue typing of the assignment from the TM domains. Instead of relying solely on the combination of signature chemical shift alone, we could use the disappearing signal intensities in the reverse labeled residues during residue typing. This increases the confidence of the assignment, especially in the TM helices. An example is shown in Figure 2.7. All reverse labeled residue types like L175, L177, L178, F179 lose their intensity in the reverse labeled sample. It is worth noting, however, that the reverse labeling of valine is not complete by our protocol, as we observe residual intensities in some valine residues. Surprisingly, reverse label-


Figure 2.6: Availability of chemical shift assignment using ${ }^{1} \mathrm{H}$-detection MAS NMR mapped onto the CitA PASpc topology map in both the citrate free (blue) and citrate bound (yellow) states. The unassigned residues are shown in hollow shapes, the partially assigned residues are marked in shapes with colored frames and fully assigned residues in filled shapes. The fully assigned residues have resonance information on the $\mathrm{H}_{N}, \mathrm{~N}, \mathrm{C} \alpha, \mathrm{C} \beta$ and $\mathrm{C}^{\prime}$.
ing did not contribute significantly to the automated assignment process by FLYA, despite adding exclusive information which is not available in the set of 3D assignment experiments. FLYA might perform poorly in assigning the TM helices because they typically result in weak peaks, indicating dynamics and may have too many missing resonances to be assigned reliably by FLYA. The partially retained valine signal also makes it hard to integrate the information from reverse labeled sample without manual supervision.

The TM region is, by definition, contacting the lipids instead of water in the sample. Since the proton NMR signals from water and from lipids are separated by chemical shift, a "solvent dimension" can be added to distinguish the signals from water contacting (both PAS domains) and those from lipid contacting (transmembrane domains). Such experiment is proposed [149] by adding a proton to proton NOE mixing before the start of the initial CP transfer. The mixing time is chosen to maximize sensitivity in the lipid contacting region. The signals are separated based on their solvent environment as shown in figure 2.8 A and D . The lipid tail contacting region in the free state is more intense and has larger chemical shift dispersion in both the N and $\mathrm{H}_{N}$ dimension (figure 2.8 B and E ). A version of the solvent accessibility experiment that additionally acquires the $\mathrm{C}_{\alpha}$ dimension is available as a 4D spectrum, but in CitA PASpc, the sensitivity of such experiments is too low to be used, even using non-uniform sampling (NUS). There are additional resonances in the lipid contacting planes in both the free and bound state. They most likely belong to those unassigned residues in the TM helices. On the other hand, not all assigned residues in the TM helices show lipid contact. This is expected, as the linker regions (or at least part of it) are not predicted to be embedded in the lipid bilayer [202].

In the linker regions between the PASp and TM2 helix, a cysteine accessibility assay showed that the binding of citrate causes a long range, piston-like shift in the membrane embedded portion of TM2 in E. coli DcuS [145]. A similar trend is seen by NMR at the C-terminus of TM2: A184 and V185 show lipid contact in the citrate bound state but not in the citrate free state (Figure 2.9). This supports the upward movement of the TM2 helix into the periplasmic space upon citrate binding. Changes on the N -terminus of the TM1 helix are not as drastic, with L7 being the most upstream lipid contacting residue in both states (Figure 2.9). This indicates that the TM1 likely acts as a


Fully labeled (H)(CA)CB(CA)NH $\quad{ }^{1} \mathrm{H}$ [ppm]
Reverse labeled (H)(CA)CB(CA)NH
Figure 2.7: IVFL reverse labeled PASpc CitA sample helps with residue typing in the manual assignment process of the TM helices. An example is shown for the comparison of $\mathrm{H}(\mathrm{CA}) \mathrm{CB}(\mathrm{CA}) \mathrm{NH}$ spectra in both fully labeled (green) and reverse labeled (red) of residue L175 to F179 in the citrate bound state. The visibility along with the characteristic chemical shifts untangles the ambiguity of the assignment as the signal intensity for L175, L177, F179 disappeared, while the non-reverse labeled residue A176 remains the same.


Figure 2.8: (H)HNH lipid contacting spectra of CitA PASpc confirming chemical shift assignment of the TM helices in the citrate free (A, B, C) and citrate bound (D, E, F) state. The additional proton dimension separates the signal from the proton and amide nitrogen dimension into water contacting (blue) and lipid contacting (yellow) parts (A, D). The diagonal self correlation signals are shown in grey. The tail group ( 0.7 ppm ) contacting region in the free state has more intensity than in the bound state. The assigned TM helical resonances can be checked if they are contacting lipid on the $\mathrm{H}-\mathrm{N}$ planes ( $\mathrm{B}, \mathrm{E}$ ). The water ( 4.7 ppm ) contacting regions in both states is the same as the normal (H)NH spectra as isolated peaks mostly come from either PASp or PASc (C, F).


Figure 2.9: Lipid contacting residues in the TM helices mapped onto the CitA topology map in the free (left, blue) and bound (right, yellow) state of CitA. Residues A184 to V185 show lipid contacts in the bound state but not in the free state. Residue A190 loses its lipid contact upon citrate binding. The border of lipid contact in the TM1 helix does not change while the border of lipid contact in the TM2 helix is shifted towards to the cytosol in the TM2 helix.
rigid membrane anchor so that the TM2 can perform rearrangements in its membrane topology. The residue A190 also shows lipid contact even though it is far away from the other membrane contacting residues in the sequence, possibly due to the signal overlap in the $\mathrm{H}-\mathrm{N}$ dimension with residue S 13 . As signals separated only by the chemical shifts of $\mathrm{H}_{N}$ and N introduce too much ambiguity in a 309 residue large construct, the lipid contact experiment is used as a rough confirmation for the assignment of the TM region.

### 2.3.3 Citrate binding induces P-helix formation at PASp C-terminus and 192KK193 motif loosening at the linker between TM2 and PASc

The secondary chemical shift is sensitive to the torsion angles [226] in the peptide bond and is, therefore, a powerful reporter of the local secondary structure. For a short stretch of residues, a structural model can also be predicted based solely on chemical shifts. This has been done for the C-terminus of PASp, where there is an obvious switch from negative ( $\beta$-strand conformation) to positive ( $\alpha$-helical) secondary chemical shift values upon citrate binding. With the assignment
available for the TM helices, we observed changes in the secondary chemical shift between the free and bound state in the cytosol proximal part of TM2 helix between residue A181 to K193 (Figure 2.10). The same negative to positive secondary chemical shift change upon citrate binding as in the PASp C-terminus is observed from residue F179 to G183, while the opposite trend is seen from residue V191 to K193 (Figure 2.11C). This indicates that the citrate binding in the periplasm causes the TM2 helix upstream of the conserved 192KK193 motif the TM2 to be pulled up in a piston like motion forming a long $\alpha$-helix. This upward motion loosens the 192 KK 193 motif and allows the dynamic changes in the cytosolic domain. The torsion angles in the peptide bonds can be predicted using TALOS-N and are used to model the TM2 helix in both the free and bound states (Figure 2.11D). A "see-saw" type of conformational changes are seen on the two sides of the region between F179 to K193: with the helix forming at the N-terminus, the C-terminal 192KK193 motif is loosened into a random coil. The residue A184 and V185 showed lipid contact in the citrate bound state but not in the free state from the lipid contact experiment (Figure 2.9). Both residues also sit at the border of the inner membrane and the cytosol. This change in the solvent environment of this part of TM2 could cause the shift in secondary structure of 180GAVG183 from $\beta$-sheet to $\alpha$-helix upon citrate binding, since both glycine and alanine have a higher tendency to form an $\alpha$-helix in hydrophobic environment [117].

### 2.4 Conclusions

${ }^{1} \mathrm{H}$-detected MAS NMR improved the quality of assignment in the CitA PASpc construct. In combination with I, V, F, L reverse labeled CitA PASpc samples and lipid transfer (H)HNH experiments, sequence specific assignment in the TM helices is available in both the free and bound state. A structural model based on the chemical shift values of the C-terminus of PASp confirmed the P-helix formation upon citrate binding, which was previously proven only with the secondary chemical shift changes of the residue L154 (Figure 2.11). The solvent transfer experiment shows that citrate binding causes a piston-like upward shift of the TM2 helix into the periplasm, moving the residues A184 and V185 into the membrane. Accompanying the changes in solvent environment, this upward motion causes the 180GAVG183 to form a helix while loosening the 192KK193 motif into a random coil. With the de-novo sequence specific assignment available using ${ }^{1} \mathrm{H}$ -


Figure 2.10: Sequence specific assignment of residue A181 to K193 in citrate free(A) and citrate bound(B) state of CitA PASpc. The assignment process using (H)CANH, (H)(CO)CA(C))NH, $(\mathrm{H})(\mathrm{CA}) \mathrm{CB}(\mathrm{CA}) \mathrm{NH},(\mathrm{H})(\mathrm{CA}) \mathrm{CB}(\mathrm{CA})(\mathrm{CO}) \mathrm{NH},(\mathrm{H}) \mathrm{N}(\mathrm{CA})(\mathrm{CO}) \mathrm{NH}$ and $(\mathrm{H}) \mathrm{N}(\mathrm{CO})(\mathrm{CA}) \mathrm{NH}$ is shown. The same manual assignment process is done throughout CitA PASpc in both states. The $\mathrm{C} \beta$ chemical shifts of K 192 and K 193 in the $(\mathrm{H})(\mathrm{CA}) \mathrm{CB}(\mathrm{CA}) \mathrm{NH}$ spectra change to higher values with citrate binding. This indicates that the K192 and K193 residues have higher helix forming propensity in the citrate free state.


Figure 2.11: Secondary chemical shift changes upon citrate binding in the PASp domain and the TM2 helix. The C-terminus of PASp is pulled up to form the P-helix (orange in B) as indicated by the negative to positive secondary chemical shift changes from residue L154 to I158 (A) after citrate binding. This motion is propagated to the TM2 helix as residue F179 to G183 undergoes the same trend in secondary chemical shift. In contrary, the 192 KK 193 motif is loosened into a random coil conformation (interchanging negative and positive secondary chemical shift values in residue V191, K192 and K193) after citrate binding (D). This loosening allows elevated dynamics in the downstream PASc domain.
detected MAS NMR, structural changes in the TM helices and their accompanying linker regions with citrate binding could be clarified. The P-helix formation at the end of the PASp domain extending to further residues downstream could be confirmed. The higher mobility in the PASc domain in the citrate bound state observed with both ${ }^{1} \mathrm{H}$-detected and ${ }^{13} \mathrm{C}$-detected experiments can be explained with the structural model calculated from the chemical shift of the linker between the TM2 helix and the PASc domain. The loosened 192KK193 motif in the citrate bound state allows more flexibility for structural rearrangement in the PASc domain. In addition, it provides structural explanation why there is higher mobility in the PASc domain upon citrate binding. However, as CitA is a homo-dimer, the two monomer sub-units do not display chemical shift differences between each other. This hinders the direct structural characterization of the CitA dimer interface using NMR even when the monomer can be assigned to relative completeness. To study the dimer rearrangements in CitA and their effects on the kinase function, we designed a functional assay detecting the ATP hydrolysis rate (Chapter 3) and distance measurement using residue-specific $\mathrm{CF}_{3}$ tagging (Chapter 4).

## CHAPTER 3

## Functional analysis of CitA with phosphorous NMR

### 3.1 Introduction

Defining the functionality is as important as structural characterization in studies of proteins, especially in kinases, whose ATP hydrolysis catalyzing activity is tightly connected to their biological roles. M. Salvi has previously reported a potential PASc domain kinase control mechanism [177], based on chemical exchange saturation transfer (CEST) [214] and solvent paramagnetic relaxation enhancement (sPRE) measurements [236]. In the CEST studies, the N-terminal helix of the PASc domain undergoes conformational exchange in solution. The sPRE profile of the PASc in the citrate bound state resembles the model predicted for the parallel dimer and the profile in the citrate free form resembles that of an anti-parallel mutant that was solved by S. Becker in the department of NMR-based structural biology. Based on this evidence, we explored the hypothesis that the PASc dimer switches from an anti-parallel to parallel dimer arrangement upon activation by citrate binding (Figure3.1). The anti-parallel dimer was originally observed in the crystal structure of the N288D mutant in PASc from G. thermodenitrificans CitA (GT CitA). Structurally, the differences between the anti-parallel and parallel dimer are mainly in the PASc N -terminal inter-helix orientations (the anti-parallel dimer's $N$-terminal helices run in the same direction, while the parallel dimer's N -terminal helices run in opposite directions) and in the C-terminal inter-dimer distances. To confirm both functionally and structurally that the anti-parallel to parallel dimer rearrangement occurs upon citrate binding, an activity assay suitable for CitA needs to be designed. Functionally, if the anti-parallel dimer is the inactive form, attaching the mutant PASc domain that forms this dimer directly onto the kinase should lead to a lower activity. Structurally,
measuring the inter-N308C distance, which is located at the C-terminal end of the PASc domain, is crucial to distinguish the two dimer forms, as the inter-dimer distance in the parallel dimer is significantly shorter than that in the anti-parallel dimer. Available techniques for site-specfic distance measurement will be reviewed in Chapter 4, but it is important to note that a chemical modification on the target residue is required. Previously, the N308C residue has been tagged with the fluorophore Atto647N to prove that the solution dimer form of wild type (WT) PASc has the parallel arrangement by the cryogenic optical localization (COLD) measurement [224]. Since COLD measurement is not successful using liposome samples, another site-specific inter-dimer distance measurement had to be designed. The prerequisite to study a chemically tagged protein is the confirmation of its functionality. For CitA, these modifications must not disrupt its kinase activity nor its responsiveness to citrate binding. So an elevated ATP hydrolysis rate in the target construct after citrate binding should be observed before structural studies can be undertaken in CitA.

Biochemical methods for tracking the kinase activity typically fall into two categories depending on the readout: direct detection of phosphorylated kinase or indirect measurement of ATP hydrolysis [203]. The scintillation proximity assay (SPA) measures protein phosphorylation by the incorporation of ${ }^{33} \mathrm{P}$-labeled ATP into a kinase substrate [24]. The safety and cost of SPA are of concern to the users, and alternative nonradioactive methods are desired. Fluorescent or luminescent kinase assays have been designed using phosphopeptide binding reagents such as antibodies [156, 171, 69, 175], but they have varied binding specificity. Samples with low yield do not have high enough sensitivity for methods with direct readout to be used. The protein samples are also often exhausted after such measurement. Indeed, the SPA assay (provided by M. Stopp in the group of Prof. Unden from the University of Mainz), though indicating a lower kinase activity with the N288D mutant (Figure C.1), did not provide statistically significant results. ATP consumption can also be monitored by the amount of remaining ATP in the solution by generation of light in a Luciferase reaction. But the procedure itself is cumbersome and reports only ATP in a narrow dynamic range (smaller than $15 \mu \mathrm{M}$ ) outside of the useful range of many kinases [106]. This assay does not report ADP or free phosphate production either. In comparison, the detection of ATP in solution with NMR is very straightforward, owing to the


Figure 3.1: Crystal structure of the WT PASc parallel dimer (B) and the N288D anti-parallel dimer (A). In the parallel dimer, the N -terminal helices in WT PASc are parallel to each other and the $\beta$ scaffold are organized so that the C-termini are pointing to the same direction and close in space. The anti-parallel dimer's N -terminal helices runs in the opposite directions and $\beta$-scaffolds are organized so that the C-termini are far away from each other. The crystal structures are solved in the group of S. Becker.
$100 \%$ natural abundance of the NMR-active nucleus ${ }^{31} \mathrm{P}$ and its large chemical shift dispersion. It has been successfully used in several systems for measurement of kinase activity [212, 235, 26], dating back to the 1980s for studying the in vivo activity of creatine kinase in living mouse tissues. During the measurement, one can also detect the production of ADP and free phosphate in a one pot reaction, as they are separated from the ATP signal in chemical shift (Figure 3.4).

In this chapter, the ${ }^{31} \mathrm{P}$ NMR kinase activity assay will be used to test the activity in two constructs: the soluble PASc-kin construct with only the PASc and kinase domains and the full length CitA. With the PASc-kin constructs, the activities of the WT PASc-kin and the N288D anti-parallel
mutant PASc-kin were compared to test if the suspected kinase inactivation in the citrate free state by the anti-parallel dimer indeed leads to an attenuated activity. The activities of three full length CitA constructs were measured in both the citrate bound and citrate free state for the preparation of site-specific distance measurement in the N308C mutant: the unlabeled CitA N308C mutant, the N 3083 C mutant tagged with Methanethiosulfonate (MTSL) and with the $\mathrm{CF}_{3}$ group.

### 3.2 Materials and methods

### 3.2.1 Sample preparation

To produce soluble kinase samples with WT and N288D mutant PASc domains (PASc-kin construct), a pET16bTEV-construct coding for a C-terminal fragment of GT CitA starting from amino acid 200, comprising the PASc and the histidine kinase domains, was expressed at $30^{\circ} \mathrm{C}$ in strain BL21(DE3) in Luria-Bertani medium supplemented with $50 \mathrm{mg} / \mathrm{L}$ ampicillin by induction with 0.5 mM IPTG at $\mathrm{OD} 600=0.7$. The culture was harvested 7 hours after induction. The cells were lysed by ultrasonication and purified by immobilized metal affinity chromatography (IMAC) on $3 \mathrm{ml} \mathrm{Ni}{ }^{2+}-\mathrm{NTA}$ resin (Qiagen). The N-terminal Histidine-tag was cleaved off by digestion with Tobacco etch virus (IMAC) protease, removed with $\mathrm{Ni}^{2+}-\mathrm{NTA}$ resin and further purified by ion exchange chromatography on a Hi Trap Q XL column (GE Healthcare) and by gel-filtration on a SD75 16/60 column (GE Healthcare). The fractions containing the protein were combined and finally dialyzed against 20 mM Tris $/ \mathrm{HCl}, \mathrm{pH} 6.5,50 \mathrm{mM} \mathrm{KCl}, 10 \mathrm{mM} \mathrm{MgCl} 2,0.5 \mathrm{mM}$ EGTA. After dialysis 0.5 mM Pefabloc (Roth) and $0.02 \% \mathrm{NaN}_{3}(\mathrm{w} / \mathrm{v})$ were added. The final protein concentration was adjusted to 0.17 mM using a 10 kDa MWCO Vivascience concentrator (Sartorius). The same protocol was applied for producing and purifying the N288D mutant of this GT CitA fragment. This mutant fragment eluted from the gel-filtration as a single peak (Figure 3.2 D). All PASc-kinase mutants were diluted for measurement to a final concentration of 0.16 mM . ATP was added right before measurement to a final concentration of 6 mM . Critically, to prevent sedimentation, the appropriate amount of ATP should be pre-diluted in the Tris buffer at pH 6.5 with the addition of $10 \% \mathrm{D}_{2} 0$ before adding both components to the protein solution, as $\mathrm{D}_{2} \mathrm{O}$ precipitated the protein when added as an isolated component. All PASc-kinase samples can be stored under
room temperature.

Full length C12A/R93A/N308C GT CitA was expressed and purified using a pET16bTEV-vector based construct following the established protocol for the C12A/R93A/N308C GT PASpc construct (see section 2.2.1) with modifications. After purification by gel-filtration, the protein was loaded onto $4 \mathrm{ml} \mathrm{Ni}^{2+}$-NTA resin and eluted with $20 \mathrm{mM} \mathrm{Tris/HCl}, \mathrm{pH} 7.4,150 \mathrm{mM} \mathrm{NaCl}, 500$ mM Imidazole, $0.694 \%$ (w/v) decylmaltoside (DM) and 0.5 mM Tris-(2-carboxyethyl)-phosphine hydrochloride (TCEP). After adding 6 mM ATP, the protein was reconstituted into DMPC liposomes at a lipid to protein ratio of $20 / 1(\mathrm{w} / \mathrm{w})$, removing the detergent with BioBeads (RioRad). The final concentration of the liposome-reconstituted protein in the buffer was adjusted to 100 $\mu$ M. For tagging with (1-Oxyl-2,2,5,5-tetramethyl- $\Delta 3$-pyrroline-3-methyl) Methanethiosulfonate (paramagnetic MTSL), the protein was transferred into 20 mM Tris $\mathrm{pH} 7.4,150 \mathrm{mM} \mathrm{NaCl}, 0,3 \%$ ( $\mathrm{w} / \mathrm{v}$ ) LDAO in the gel-filtration step to remove reducing agent. MTSL was added in 20 fold excess $(\mathrm{mol} / \mathrm{mol})$ and the solution was incubated for 3 days on ice. The protein was again loaded onto 4 $\mathrm{ml} \mathrm{Ni}{ }^{2+}-$ NTA resin to switch to $0.694 \%$ DM and after adding 6 mM ATP reconstituted into DMPC liposomes at a lipid to protein ratio of $20 / 1(\mathrm{w} / \mathrm{w})$, adjusting the protein concentration to $100 \mu \mathrm{M}$.

Tagging of the C12A/R93A/N308C-GT CitA protein with 3-bromo-1,1,1-trifluoroacetone (BTFA) was performed similar to the protocol for MTSL tagging, using 50 mM sodium phosphate, pH $7.0,200 \mathrm{mM} \mathrm{NaCl}, 0.3 \%(\mathrm{w} / \mathrm{v})$ LDAO in the gel-filtration step. Subsequently BTFA was added drop-wise to the protein solution as described for the BTFA-tagged PASpc (section 4.2.1), from a 100 mM stock solution in 50 mM sodium phosphate, $\mathrm{pH} 7.0,200 \mathrm{mM} \mathrm{NaCl}$. After incubation overnight on ice, the protein was loaded according to the protocol for MTSL onto $4 \mathrm{ml} \mathrm{Ni}^{2+}-\mathrm{NTA}$ resin to switch to 0.694 \% DM and reconstituted in DMPC liposomes at a lipid to protein ratio of 20/1 (w/w), with 6 mM ATP added to the buffer. The final protein concentration was adjusted to $100 \mu \mathrm{M}$. To obtain the citrate bound state, buffer containing 5 mM sodium citrate was added to the sample and equilibrated overnight at $4^{\circ} \mathrm{C}$.


Figure 3.2: Purification of CitA PASc-kin WT (A and B) and N288D mutant (C and D) constructs by gel filtration. SDS-polyacrylamide gel (A) shows fractions 19 to 30 of the chromatography run (B) of the WT construct, which showed two peak representing different oligomer state. Particle size measurement with dynamic light scattering (DLS) (Figure C.3) confirmed the two peaks originate from a potential dimer to tetramer exchange. SDS-polyacrylamide gel (C) of the N288D mutant PASc-kin construct shows fractions 23 to 28 of the chromatography run (D) showed only a single peak. The data are provided by Karin Giller and Dr. Stefan Becker.


Figure 3.3: Purification of full length CitA R93A/C12A/N308C constructs by gel filtration. SDSpolyacrylamide gel (A) shows fractions 27 to 34 of the chromatography run (B). The data are provided by Karin Giller and Dr. Stefan Becker.

### 3.2.1.1 NMR spectroscopy and data analysis

1D phosphorus spectra were measured with a Bruker 400 MHz magnet. The spectra for PASc-kin WT and N288D, and full length un-tagged R93A/C12A/N308C CitA were measured with a room temperature QXI H/P-C/N/D five channel probe with a $\mathrm{B}_{1}$ field of 7.5 kHz . The spectra for MTSL and $\mathrm{CF}_{3}$ tagged $\mathrm{R} 93 \mathrm{~A} / \mathrm{C} 12 \mathrm{AN} / 308 \mathrm{C}$ CitA were measured with a room temperature TBO $\mathrm{H} / \mathrm{F}-\mathrm{C} / \mathrm{N} / \mathrm{P}-\mathrm{D}$ probe. All spectra were measured with an inter-scan delay of 1 s and an offset at -15 ppm . Number of scans was set to $1920.10 \% \mathrm{D}_{2} \mathrm{O}$ was used in all samples as lock signal. The temperature of measurement of all CitA full length constructs is $37^{\circ} \mathrm{C}$.

The initial speed of the reaction was used to measure the kinase activity since the only reactant (ATP) is added in large excess to the enzyme. ATP is stable under the experimental condition (Figure 3.4), so its auto-hydrolysis does not need to be taken into account. The error is estimated from the noise level of the spectra. According to first order kinetics, the consumption of the reactant in the complete reaction should follow a single exponential decay. At very short reaction time, the free phosphate $(\mathrm{Pi})$ production approaches a linear equation with the slope corresponding to the exponential decay rate (see section C.1). This can also be observed experimentally. For all PASc-kinase constructs, the reaction was measured to significantly long time to


Figure 3.4: The addition of the PASc-kin WT construct hydrolyzes ATP into ADP (B), which is otherwise stable under the experimental conditions (A). The $1 \mathrm{D}{ }^{31} \mathrm{P}$ spectrum of ATP does not change after 24 hours, indicating the stability of the ATP under the experimental conditions. The spectrum shows three peaks, corresponding to the signals of $\beta-\mathrm{P}, \alpha-\mathrm{P}$ and $\gamma-\mathrm{P}$. The addition of $\mathrm{PASc}-$ kinase leads to the appearance of signals of the degradation products ADP ( $\beta-\mathrm{P}$ and $\alpha-\mathrm{P}$ in ADP) and free phosphate (Pi)
acquire the full exponential decay. The exponential decay rate of the full reaction is the same as the linear decay rate in the initial phase of the reaction (Figure C.2). There are several advantages in monitoring the free phosphate during the initial reaction. Due to its narrow linewidth, the peak is easily trackable. Measuring only the initial rate also saves experimental time, especially in slow reactions like these. Product inhibition by ADP might become a significant factor later when the ADP concentration is getting higher, although such inhibition has not been observed by us, as the full reaction followed a single exponential decay till the end.


Figure 3.5: The kinase attached to the PASc N288D mutant has $25 \%$ lower activity in the ${ }^{31} \mathrm{P}$ assay PASc WT. The initial rate of the kinase activity with the PASc N288D mutant is $82 \mathrm{~h}^{-1}$ (yellow), and that of WT is $110 \mathrm{~h}^{-1}$ (blue). Both curves measured to 200 hours still satisfy the zero order reaction approximation and are linear (A). At the end of the reaction (195 h), ${ }^{31} \mathrm{P}$ NMR signal of free phosphate, one of the end product of ATP hydrolysis, is $25 \%$ lower with the N288D mutant (B) than with the WT PASc.

### 3.3 Results

### 3.3.1 Anti-parallel mutant N288D attenuates kinase activity

The addition of WT PASc-kinase leads to an immediate hydrolysis of ATP to ADP and free phosphate, as indicated by the decay of ATP peak intensities along with the appearance of ADP and free phosphate peaks. The N288D mutant of the PASc-kinase (which shows an anti-parallel dimer arrangement in the crystal structure in the isolated PASc domain) attenuates the kinase activity by $25 \%$ according to the production of the free phosphate. The same level of ATP consumption reduction was observed in the full reaction measured to 800 h (Figure C.2). This confirms that the initial rate of Pi production corresponds to the rate of ATP consumption. The WT PASc-kin eluted from the SEC column in a double peak, probably representing different aggregation states (Figure 3.2 B). A particle size measurement using dynamic light scattering (DLS) revealed that the two peaks represent an exchange between a dimer and a tetramer (Figure C.3). The possibility that any activity drop should come from a dissociated dimer can be ruled out. The N288D mutant PASc-kin sample eluted as one peak, but a fast exchange between a dimer and a tetramer is still possible. The kinase activity is not fully abolished when it is attached to the PASc N288D mutant, likely


Figure 3.6: Kinase activity of full length C12A/R93A/N308C CitA without tag (A), with MTSL (B) and with $\mathrm{CF}_{3}(\mathrm{C})$ from ${ }^{31} \mathrm{P}$ NMR assay. The citrate bound state (yellow) in the non-tagged and $\mathrm{CF}_{3}$-tagged CitA has two to three times higher activity compared with the citrate free state (blue). The MTSL tagged CitA does not respond to the addition of citrate, since the kinase activity is the same between the two states.
due to dimer exchanged in the PASc domain, as seen by CEST experiments done with isolated PASc domains [177]. Similar change in kinase activity was also confirmed by SPA assay with ${ }^{33}$ P-ATP (Figure C.1), although the rate changes are not statistically significant due to precision of the method. We also raised the temperature of the measurement to $37^{\circ} \mathrm{C}$ for the WT PASc-kinase and noticed a very dramatic jump of the kinase activity to four times compared with that at $25^{\circ} \mathrm{C}$. This fits well with the fact that G. thermodenitrificans is thermophilic and all proteins derived from there are optimized to function at very high temperature up to $60^{\circ} \mathrm{C}$.

### 3.3.2 Activity of CitA N308C mutant changes with different tags

The N308C mutant of the isolated WT PASc domain has been previously tagged with the fluorescent dye Atto647N for COLD studies and retains the parallel dimer forms observed in crystal[224]. The functionality of the full length N308C CitA without tag is confirmed again by the ${ }^{31} \mathrm{P}$ NMR activity assay. When citrate is added to the CitA N308C mutant in liposomes, the activity rises by a factor of $1.9\left(247 \mathrm{~h}^{-1}\right.$ to $\left.429 \mathrm{~h}^{-1}\right)$. In the $\mathrm{CF}_{3}$ tagged CitA, the activity rises by 2.6 times when citrate is added ( $15142 \mathrm{~h}^{-1}$ to $575 \mathrm{~h}^{-1}$ ). The in vivo $\beta$-Galactosidase activity assay of GT CitA performed in the group of Prof. Unden found the same factor of 2 to 3 times of activity gain with citrate binding [177]. This factor of increase in ATP hydrolysis rate might be subject to further
downstream signal amplification in the bacteria [88]. The MTSL labeled CitA, however, did not respond to the addition of citrate, with the free state having a slightly higher activity ( $305 \mathrm{~h}^{-1}$ without citrate compared with $275 \mathrm{~h}^{-1}$ with citrate). MTSL tagged CitA could be locked in either the inactive or the active state.

### 3.4 Discussion

Kinase activity can be measured to high precision by tracking the ATP hydrolysis and free phosphate production with ${ }^{31} \mathrm{P}$ NMR. Due to the $100 \%$ natural abundance and large chemical shift dispersion of ${ }^{31} \mathrm{P}$, the amount of individual components of the reaction can be easily determined. This method confirms the attenuating effect of the anti-parallel N288D mutant of PASc on the kinase activity, as it decreases the ATP consumption rate by $30 \%$ compared with the WT PASc. Interestingly, this is in rough agreement with the results from the more conventional radioactive ${ }^{33} \mathrm{P}$ SPA assay. However, it is important to note that these two methods measure essentially different parameters. While the ${ }^{31} \mathrm{P}$ NMR activity assay measures reaction kinetics by production of reaction products, the ${ }^{33} \mathrm{P}$ radioactivity SPA assay reports the speed of protein phosphorylation. These two parameters both reflect the the activity of the kinase, and should be comparable with each other if the dissociation of the phosphate from the kinase is not the rate limiting step of the reaction. The stability of the phosphorylated kinase is in the range of minutes [107], much shorter than the measured rate in the range of hours. It cannot be ruled out that the attenuated kinase activity of the N288D mutant PASc is caused by the lack of dimer to tetramer exchange observed in the WT PASc-kin construct (Figure 3.2). But there is no current evidence that such exchange promotes kinase activity. The propensity to form an anti-parallel dimer in the N288D instead of the parallel arrangement in the WT PASc is still considered to be the major cause of the lower activity in the PASc-kinase construct. So, the anti-parallel dimer indeed resembles the off state of CitA in its effect on the kinase activity.

The high precision and high sensitivity of the ${ }^{31} \mathrm{P}$ activity assay made it possible to determine the activity of the low-yield full length CitA construct. The functionality of CitA with site-specific tags can be tested, a prerequisite for inter-dimer distance determination. The $\mathrm{CF}_{3}$
tagged CitA has a slightly more elevated response to citrate than the untagged CitA. The reason is either the uncertainty in the protein quantity estimation as the efficiency of protein incorporation into liposome might be different between the samples, or the $\mathrm{CF}_{3}$ tag still slightly disturbed the protein structure, causing gain of function in the activity. For an even more precise rate measurement, all other phosphorous peaks can be calibrated to the ATP signal intensity at time zero since it is titrated to the same concentration. The MTSL tag, however, completely abolished CitA's response to citrate binding. MTSL is much larger than the $\mathrm{CF}_{3}$ group and is thus more likely to disrupt the PASc structure. Altogether, tagging with the small $\mathrm{CF}_{3}$ group has not impeded the kinase activity of CitA, opposite to tagging with MTSL. With $\mathrm{CF}_{3}$-tagged CitA at hand, functionally relevant distance changes in CitA should now be measurable. The measurement of site-specific distances using a $\mathrm{CF}_{3}$-tagged CitA PASpc construct will be described in Chapter 4.

## CHAPTER 4

# Distance Measurement between CitA Dimer with 19F CODEX 

### 4.1 Introduction

Understanding the dimer interface is crucial for membrane bound HKs like CitA which needs to be cross-phosphorylated for their functionality. This is not trivial for conventional NMR experiments. In uniformly labeled samples, if measured NMR contacts are inter- or intra-dimeric needs to be discerned. This is not straightforward for proteins in the size range of CitA. Alternatively, differential isotope labeling between dimer units has been used successfully in providing site-specific distance information in the isolated PASc dimer through the ${ }^{13} \mathrm{C} /{ }^{15} \mathrm{~N}$ double-edited NOESY experiment [ 105,177$]$. But in the liposome sample, this would require dimer mixing during reconstitution, which does not happen during CitA sample preparation. The double electron-electron resonance (DEER) [143, 142] experiment is designed to measure distance between electron spin pairs, usually in the form of MTSL labeled cysteine residues in proteins and is sensitive to a distance range of 1.8 to 6 nm in fully protonated membrane proteins [103]. However, MTSL labeled N308C CitA does not respond to citrate binding (Chapter 3), so could not provide functionally relevant distance information. The Cryogenic Optical Localization in 3D (COLD) has successfully reproduced the inter-dimer distance at N308 in the PASc WT crystal structure [224], but the technique itself is incompatible with liposome samples as it requires isotropic behavior of the molecule.

The centerband-only detection of exchange (CODEX) experiment has proven to be a unique solution to solving the oligomeric state in proteins and, after fitting to a rate equation, measuring
inter-oligomer distances. CODEX has been successful in elucidating functionally important side chain conformation in the influenza virus membrane proton channel M 2 [132, 133] in addition to other membrane associated systems such as antimicrobial peptides (AMPs) [137, 37]. The CODEX pulse program consists of two CSA recoupling blocks sandwiching a long mixing period $\tau_{m}$ that lasts an integer number of rotor periods, between which the magnetization is stored at $z$-direction and spin diffusion can happen [97]. If there is dipolar exchange between spins with different instantaneous CSA during the mixing period, the orientation dependent frequency is changed and leads to incomplete refocusing of the CSA. This dephasing is observed as an decrease in intensity compared with a reference spectrum that eliminates the effect of $\mathrm{T}_{1}$ relaxation during spin diffusion. A detailed description is available in section 1.6. The choice of nucleus is also critical. As the dephasing process is dipolar coupling driven, the dipolar coupling strength between spins will determine the dynamic range of the observed distance. ${ }^{19} \mathrm{~F}$ has the second highest gyromagnetic ratio after the proton. This confers high sensitivity in ${ }^{19} \mathrm{~F}$-detected NMR experiments and allows ${ }^{19} \mathrm{~F}$ to ${ }^{19} \mathrm{~F}$ spin diffusion to be sensitive to a relatively large distance range of 5 to $20 \AA$. For the CODEX experiment specifically, ${ }^{19} \mathrm{~F}$ detection does not need natural abundance correction either, like in its ${ }^{13} \mathrm{C}$-detected [228] counterpart, making precise distance determination easier.
${ }^{19} \mathrm{~F}$ has been used as a popular probe for biological NMR, because ${ }^{19} \mathrm{~F}$ is almost absent in proteins. Selective labeling with ${ }^{19} \mathrm{~F}$ can therefore be easily done without background. In both solution and solid-state NMR, ${ }^{19} \mathrm{~F}$ based experiments have yielded important functional results in systems like GPCRs [123] and HIV-1 Capsid protein [221]. A variety of ${ }^{19} \mathrm{~F}$ containing labels have been designed. In solution NMR, $\mathrm{CF}_{3}$ groups are preferred due to their smaller CSA, small size and neutral chemical properties compared with ${ }^{19} \mathrm{~F}$-containing aromatic groups [123]. The $\mathrm{CF}_{3}$ group also undergoes very fast axial rotation, making all three ${ }^{19} \mathrm{~F}$ atoms magnetically equivalent. This $\mathrm{CF}_{3}$ hopping motion gives a three fold signal enhancement and narrow line width in the NMR signal, making it an ideal tag in proteins when sensitivity is of concern. However, even with the sensitive ${ }^{19} \mathrm{~F}$ labeling, detecting a single tag to complex biological systems remains challenging due to low sensitivity. Recent advances in dynamic nuclear polarization (DNP) techniques have further increased the sensitivity of ${ }^{19} \mathrm{~F}$ detected NMR experiments [131]. Currently, in solid-state,
${ }^{19} \mathrm{~F}$ CODEX experiments are done using ${ }^{19} \mathrm{~F}$ labeled aromatic amino acids like phenylalanine and tryptophan, because ${ }^{19} \mathrm{~F}$ on aromatic rings have large CSA that is beneficial for the CSA encoding. However, for large membrane proteins like CitA, this labeling strategy will not be applicable due to inevitable chemical shift overlap. Here, we propose a solution by selectively tagging a single cysteine residue with a $\mathrm{CF}_{3}$ group to measure site-specific inter-dimer distances in CitA. This is combined with dynamic nuclear polarization (DNP) and proton to ${ }^{19} \mathrm{~F}$ CP for signal enhancement.

### 4.2 Material and Methods

### 4.2.1 Hexafluoroacetone(HFA) and protein sample preparation

The 8 M and 8 mM hexafluoroacetone (HFA) DNP sample was prepared by mixing pure HFA and 1000x dilution of HFA in water, respectively, with the "DNP juice" ( 10 mM TEMTriPol, $60 \%$ glycerol, $30 \% \mathrm{H}_{2} \mathrm{O}$ and $10 \% \mathrm{D}_{2} \mathrm{O}$ ) in a ratio of 1:3.

For incorporating ${ }^{19}$ F-tryptophan into mutant $\mathrm{C} 12 \mathrm{~A} /$ R93A GT CitA PASpc protein $\left({ }^{19} \mathrm{~F}\right.$ W163 CitA PASpc) in the citrate bound state, we basically followed a published protocol [49]. One hour before induction, $60 \mathrm{mg} / \mathrm{L}$ of 5-fluoroindole (TCI) were added to M9 minimal medium supplemented with ${ }^{15} \mathrm{~N}-\mathrm{NH}_{4} \mathrm{Cl}$. Expression was performed at $20{ }^{\circ} \mathrm{C}$ by induction at OD600 of 0.65 with 0.5 mM isopropyl- $\beta$-D-thiogalactopyranoside (IPTG, AppliChem). The cells were harvested 16 hours after induction. Protein purification and reconstitution were performed as described in section 2.2.1.

The introduction of fluorine labels using cysteine alkylation by BTFA is done according to the protocols published by the group of Schofield [1, 34, 173]. For tagging with BTFA (Aldrich) of ${ }^{15} \mathrm{~N}$-labelled, sodium citrate loaded C12A/R93A/N308C mutant of GT CitA PASpc, the initial purification step on the $\mathrm{Ni}^{2+}$-column was performed with 5 mM dithiothreitol (DTT, GERBU) added to all buffers. After elution from the $\mathrm{Ni}^{2+}$-column the GT CitA PASpc mutant protein solution was supplemented with 5 mM Tris(2-carboxyethyl)phosphine-hydrochloride (TCEP, Sigma-Aldrich) and incubated for 1 hour on ice to secure complete reduction of cysteine 308 .


Figure 4.1: Purification of CitA PASpc construct by after $\mathrm{Ni}^{2+}$ column. SDS-polyacrylamide gel (A) shows fractions 32 to 42 of the chromatography run (B). Data are provided by Karin Giller and Dr. Stefan Becker

Exchange against BTFA-tagging buffer ( 50 mM sodium phosphate $\mathrm{pH} 7.0,200 \mathrm{mM} \mathrm{NaCl}, 5$ mM sodium citrate, $0.3 \%(\mathrm{w} / \mathrm{v}) \mathrm{n}$-dodecyl-N, N-dimethylamine-N-oxide (LDAO, Anatrace)), was achieved by gel filtration on a SD200 16/60 column (GE Healthcare). BTFA was added drop-wise with intermediate vortexing in 35 fold excess ( $\mathrm{mol} / \mathrm{mol}$ ) to the protein solution, from a 100 mM stock solution in 50 mM sodium phosphate, $\mathrm{pH} 7.0,200 \mathrm{mM} \mathrm{NaCl}, 5 \mathrm{mM}$ sodium citrate. After incubation overnight on ice the volume of the protein solution was reduced with a 30,000 MWCO Amicon Ultra concentrator (Millipore) and excess BTFA agent was removed by another gel-filtration step on a SD200 16/60 column equilibrated with 20 mM sodium phosphate, pH 6.5, $150 \mathrm{mM} \mathrm{NaCl}, 0.3 \%$ (w/v) LDAO, 5 mM sodium citrate. For final reconstitution into liposomes a lipid film of 1,2-dimyristoyl-sn-glycero-3-phosphocholine (DMPC)/ 1,2-dimyristoyl-sn-glycero-3-phosphate (DMPA) (9/1, mol/mol, Avanti Polar Lipids) was dissolved at $5 \mathrm{mg} / \mathrm{ml}$ in the gel-filtration buffer, sonicated to obtain a homogeneous suspension and added to the protein solution at a final lipid to protein ratio of $75 / 1(\mathrm{~mol} / \mathrm{mol})$. After incubation for two hours, the detergent was removed by adding BioBeads (BioRad, 2 g BioBeads/66 mg LDAO) followed by further incubation overnight at $42^{\circ} \mathrm{C}$ on an orbital shaker. To separate the liposomes from
the beads the mixture was loaded onto a gravity-flow column and the liposomes containing the reconstituted, BTFA-tagged C12A/R93A/N308C mutant GT CitA PASpc protein were washed from the column with 20 mM sodium phosphate $\mathrm{pH} 6.5,5 \mathrm{mM}$ sodium citrate, 0.5 mM Pefabloc (Roth, Germany), $0.02 \%(\mathrm{w} / \mathrm{v}) \mathrm{NaN}_{3}$. The CitA PASpc liposome samples are produced in the bound form initially, and the free state sample is prepared by stripping the citrate bound proteins off of citrate using the protocol introduced in section 2.2.1 under incubation at $40^{\circ} \mathrm{C}$.

The liposome samples are prepared for DNP experiments according to matrix free preparation protocol by adding TEMTriPol powder to the liposome sample until the solubility is saturated. All samples are packed into 2.5 mm phoenix MAS rotors and shock frozen by plunging into liquid nitrogen.

### 4.2.2 CODEX measurement

All CODEX experiments are measured with a previously published pulse program [97, 132, 228] on a Bruker 600 MHz magnet, with a 2.5 mm Phoenix DNP probe equipped with H/F double channel tuning at 20 kHz MAS and a set temperature of 90 K . We measured a DNP enhancement, $\epsilon$, of 8 from both proton one pulse and ${ }^{1} \mathrm{H}$ to ${ }^{19} \mathrm{~F}$ CP experiment (Figure D.1). ${ }^{1} \mathrm{H}$ to ${ }^{19} \mathrm{~F}$ CP retains the enhancement factor from that of the proton. Measurement of DNP enhancement on ${ }^{19} \mathrm{~F}$ is not possible as for dilute samples ${ }^{19} \mathrm{~F}$ direct irradiation does not yield enough signal with or without DNP. The initial ${ }^{1} \mathrm{H}$ to ${ }^{19} \mathrm{~F}$ CP contact time is $1500 \mu \mathrm{~s}$ with $41.6 \mathrm{kHz}{ }^{19} \mathrm{~F}$ irradiation and 51 kHz ${ }^{1} \mathrm{H}$ irradiation. The ${ }^{19} \mathrm{~F}$ and ${ }^{1} \mathrm{H}$ hard pulse power is 65.8 kHz and 53.2 kHz , respectively. The ${ }^{1} \mathrm{H}$ TPPM decoupling power is set to 50 kHz . The inter-scan delays are optimized for each sample individually. The offset of ${ }^{19} \mathrm{~F}$ and ${ }^{1} \mathrm{H}$ is -74 ppm and 3 ppm respectively. The sweep width for all ${ }^{19} \mathrm{~F}$-detected experiments is set to 400 ppm .

### 4.2.3 Fitting of CODEX curve

The spin diffusion rate can be calculated from the CODEX dephasing curve using models described in literature [132, 204, 57], by the following equations:

$$
\begin{equation*}
M(t)=e^{-K t} M(0) \tag{4.1}
\end{equation*}
$$

Equation 4.1 describes the magnetization evolution, $M(t)$, with spin diffusion time. $K$ is the $n$ dimensional exchange matrix containing the rate constants $k_{i j}$ between exchange of two spins $i$ and $j$, where $n$ is the total number of orientationally different spins in close enough vicinity to undergo magnetization exchange.

$$
\begin{equation*}
k_{i j}=0.5 \pi \cdot F_{i j}(0) \cdot \omega_{i j}^{2} \tag{4.2}
\end{equation*}
$$

Balancing of the exchange matrix requires the sum of each column of the exchange matrix, $K$, to be zero and that the rate constants satisfy $k_{i j}=k_{j i}$ for equal population of magnetization [132, 15]. Note that $K$ should contain not only the rate of direct exchange $k_{i j}$ but also relayed elements, which are magnetization transfer through two or more spins. It can be shown that at large enough $t, M(t)$ approaches the value of $1 / n$. This means that CODEX decay will plateau at the value of one over the oligomer number. Distance determination using CODEX relies on the dependence of spin diffusion rate. The spectral overlap function $F_{i j}(0)$ is the overlap integral describing the probability that single-quantum transition occurs at the same frequency for two spins. The exact value of it is usually extracted by fitting rates to known crystal structures. Here, we took the previously published value of 30 to $60 \mu \mathrm{~s}$ [172]. Least square fitting of the exchange rate is done using home written MATLAB code [228].

### 4.3 Results

### 4.3.1 $\mathrm{CF}_{3}$ hopping exits at 90 K under DNP condition

The $\mathrm{CF}_{3}$ group undergoes fast rotational motional averaging under room temperature, making all three fluorines chemically and magnetically equivalent. This behavior is favorable due to the
additional sensitivity enhancement offered by the three fluorines. However, it has not been reported if this is still true under the DNP experimental temperature of 90 K . Since CODEX is sensitive to magnetically nonequivalent spins, the CODEX decay in the $\mathrm{CF}_{3}$ group can be used as a simple test for the existence of the $\mathrm{CF}_{3}$ group hopping. We performed the CODEX experiment on the small molecule hexafluoroacetone (HFA). In the 8M HFA sample, the CODEX curves decays slowly and plateaus at 0.5 , meaning the three fluorine spins are orientationally equivalent also at 90 K . This makes tagging protein with $\mathrm{CF}_{3}$ groups optimal as this offers a three-fold signal enhancement just like under room temperature. We mimicked the concentration in the range expected for a membrane protein sample by diluting the HFA sample to 8 mM . With both the DNP and ${ }^{1} \mathrm{H}$ to ${ }^{19} \mathrm{~F}$ CP applied, there is decent signal to noise ratio with 16 scans (Figure 4.2 D ). ${ }^{19} \mathrm{~F}$ one pulse experiment, on the other hand, did not yield any signal from HFA even with DNP enhancement, instead, we were only able to see a sharp background after 1024 scans. This sharp background potentially originates from the fluorinated materials used in the probe design. It is clear that for a membrane protein, enhancement offered by ${ }^{1} \mathrm{H}$ to ${ }^{19} \mathrm{~F} \mathrm{CP}$ will be indispensable to make the experiment feasible. Since CODEX experiments involve two CSA recoupling blocks, the small CSA of the $\mathrm{CF}_{3}$ group might be concerning. However, with the observation of spinning side bands of HFA at 20 kHz MAS frequency, we can assume that the CSA of the $\mathrm{CF}_{3}$ group is larger than 20 kHz and thus not averaged out completely under the MAS frequency used here. It agrees with the CSA magnitude of 63 ppm (corresponding to 36 kHz for ${ }^{19} \mathrm{~F}$ in a 600 MHz magnet) in the $\mathrm{CF}_{3}$ group of 3-F-alanine reported in literature [56]. We observed an unstable buildup of the HFA CODEX curve under 2 ms of mixing time. As the magnetization is stored at the $z$-direction after the first CSA recoupling block, the mixing period functions additionally as a $z$-filter to eliminate unwanted transverse terms. A mixing period shorter than 2 ms might be inefficient as a $z$-filter and thus cause unreliable readouts. So for CODEX experiments, a true zero mixing time has not been recorded, and previous CODEX experiments also started with the measurement at roughly 2 to 5 ms of mixing time [132].// // We then proceeded with the ${ }^{19} \mathrm{~F}$-W163 CitA PASpc sample in the citrate bound state to test our experimental conditions. This sample was tested prior to the $\mathrm{CF}_{3}$ group tagged CitA PASpc sample due to the high efficiency of incorporating fluorine labeled amino acids into proteins. So the ${ }^{19} \mathrm{~F}-\mathrm{W} 163$ CitA PASpc is used as to gauge the sensitivity of the CODEX experiment in membrane proteins. Indeed, with the experiment setup established for the


Figure 4.2: CODEX decay curve for HFA plateaus at 0.5 proving the existence of fast $\mathrm{CF}_{3}$ hopping at 90 K . With 8 M HFA, the one pulse experiment has strong signal with a DNP enhancement factor of $10(\mathrm{~B})$, the ${ }^{1} \mathrm{H}$ to ${ }^{19} \mathrm{~F}$ CP gives only very weak signal due to the low proton content in the sample. in diluted HFA of 8 mM , the H to F CP experiment has significantly better signal with 16 scans ( C , black), while the one pulse experiment gives only a background signal after 1024 scans (C, red). The plateau of the CODEX dephasing curve is 0.5 (D) instead of 0.167 supporting orientationally averaged fluorines on the $\mathrm{CF}_{3}$ groups, after 2 ms of mixing time ( D , red). All spectra are measured with an inter-scan delay of 10 s , an acquisition time of 1.5 ms .


Figure 4.3: CODEX experiment of ${ }^{19} \mathrm{~F}-\mathrm{W} 163$ CitA PASpc plateaus at 0.5 (B), indicating a dimeric TM2 interface. The DNP enhancement combined with ${ }^{1} \mathrm{H}$ to ${ }^{19} \mathrm{~F}$ yields decent sensitivity to monitor CODEX decay (A). A mono-exponential decay can be fitted to the CODEX rate equation, the extracted rates infer a inter-helical distance of $6 \AA$ at W163.

8 mM HFA sample, we could acquire a CODEX decay curve. We observed a plateau of around 0.5 at 50 ms of mixing, which is compatible with a dimeric arrangment of the TM2. The fitted rate revealed a inter-dimer distance of $6 \AA$ at W163 for CitA. Such distances suggest that the residues W163 from the monomers are facing each other at the dimer interface when the citrate is bound, which is compatible with the TM2 dimer modeled with cysteine crosslinking data [202].

### 4.3.2 Site-specific distance measurement supports an anti-parallel to parallel dimer rearrangement in PASc upon citrate binding

The tagging of a specific location in a protein with the $\mathrm{CF}_{3}$ group relies on a single site cysteine at this position that does not interfere with the functionality and structure of the protein. Fortuitously, for CitA, the N308C mutation at the C-terminus of the PASc domain has been previously shown by COLD to conserve the structure observed by X-ray crystallography [177]. We further validated the functionality of this mutant along with its $\mathrm{CF}_{3}$ tagged counterpart using ${ }^{31} \mathrm{P}$ ATP assay in Chapter 3. The inter-dimer distance at this position can help to discern the parallel ( $11 \AA$ ) and the antiparallel ( $45 \AA$ ) dimer arrangement (Figure 4.4A and B), as N308 is at the very end of the PASc domain. Now, with the availability of CODEX and the favorable conditions offered by using a $\mathrm{CF}_{3}$ pair as a distance ruler, we can distinguish between the parallel and anti-parallel dimers in the membrane bound PASpc sample in its functional states, i.e., citrate bound and citrate free states.

The readout is straightforward for anti-parallel dimer, as the inter-C308 distance in it is larger than $45 \AA$ (Figure 4.4 A , right panel), which is beyond the limit for inter-fluorine spin diffusion to happen. This is what we observed in the free state of CitA PASpc, where there is no decay in the CODEX signal compared with the reference experiment beyond 500 ms (Figure 4.4C, blue). In the case of the parallel dimer, for whom the inter-C308 distance is $11 \AA$, we should be able to observe a CODEX decay rate corresponding to this distance. We extracted a single exponential decay of $0.5 * e^{(-0.0006 * t)-0.5}$ for the CODEX decay curve in the CitA PASpc bound sample and found a distance of $14.5 \pm 3 \AA$, fitting exactly to the parallel dimer (where the inter-N308C thiol group distance measures $11 \AA$ ). A single exponential fit suffices here because the CODEX decays curve plateaued at a value of 0.5 . The short ${ }^{19} \mathrm{~F}_{1}$ of 321 ms (Figure 4.4D) prevented the acquisition of mixing time beyond 500 ms . However, as we already observed the plateau in the bound state at 250 ms (Figure 4.4A and B), it is sufficient to acquire the data at a mixing time of around 300 ms . We observed some fluctuating, minor decay also for the free state, especially at 250 ms and 300 ms mixing, but not at 500 ms mixing time (when the $\mathrm{S} / \mathrm{S}_{0}$ value equals ones exactly). From the NMR settings, this might be caused by minor incomplete CSA refocusing from spinning speed deviation or imperfect pulse power calibrations. But more likely, this can also be attributed to fractions of bound PASpc population in the sample as there is still very minor intensity of the H96 side chain, which is an indicator of the citrate bound state of PASpc, in the measured (H)NH spectrum of the $\mathrm{CF}_{3}$-tagged PASpc after washing with the citrate free buffer (Figure D.2).

### 4.4 Discussions

We applied CODEX to measure the inter-oligomer distances in the range of 5 to $20 \AA$ in a membrane protein aided by the sensitivity enhancement offered by DNP, $\mathrm{CF}_{3}$ hopping and ${ }^{1} \mathrm{H}$ to ${ }^{19} \mathrm{~F}$ CP. With this approach, we observed dramatic inter-dimer distance changes at the C-terminus of the PASc domain in CitA. Upon citrate binding, the C-terminus of PASc switches from being more than $20 \AA$ apart to $11 \AA$ apart, providing site-specific distance evidence for previously hypothesized [177] anti-parallel to parallel dimer rearrangement. For a more precise determination, an experimentally fitted $\mathrm{F}(0)$ can be done with bis- $\mathrm{CF}_{3}$-phenyl with a known inter $\mathrm{CF}_{3}$ distance of $5.9 \AA$ [56]. Tagging of CitA with a chemically neutral, and small $\mathrm{CF}_{3}$


Figure 4.4: Large inter-dimer distance at C-terminus of PASc changes observed by CODEX dephasing between bound and free state of CitA PASpc. At mixing time of 250 ms , the bound state CODEX signal decays to 0.60 (Table D.2) of the reference experiment ( B , left); the decay rate can be fitted to a inter $\mathrm{CF}_{3}$ distance of $14.5 \pm 3 \AA(\mathrm{C}$, yellow), corresponding exactly the the inter-dimer distance at the C-terminus of the parallel dimer ( B , right). At the same mixing time, the free state CODEX signal is almost the same (Table D.1) as the reference experiment (A, left) through all mixing times, corresponding to a large inter dimer distance at the C-terminus of more than $20 \AA$, agreeing with the anti-parallel dimer (A, right). The CODEX decay curve cannot be acquired to more than 500 ms due to ${ }^{19} \mathrm{~F}_{1}$ of $321 \mathrm{~ms}(\mathrm{D})$, but is sufficient for observation of the plateau.
group does not disturb its functionality, making site-specific distance measurement possible. In addition, dilution of the sample with either lipids or untagged proteins is not necessary because the measurement is sensitive only to a short range of distances and given the large dimer size is thus not expected to be influenced by inter-dimer contacts. This is beneficial, especially if the protein of interest tends to cluster in the membrane. In our CitA liposome sample, the DNP enhancement is only 8 times, which is significantly lower than what had been achieved by other groups of at least 50 times [131]. The DNP conditions including the type of biradical, the mixing strategy etc. can be optimized to further improve the sensitivity of the method. This will allow site-specific distance measurements in even larger, more challenging constructs like full length CitA, where not only the spin density is halved due to the size of the construct, but also the yield of the protein is much poorer. But already with the current setup, measurement is possible even in membrane protein samples with a $\mathrm{CF}_{3}$ label density in the $\mu \mathrm{M}$ range. This provides an alternative solution to measure site-specific inter-oligomer distances when the system is too large for conventional NMR contact determination or when homodimers cannot be prepared with orthogonal labeling.

With the combination of determination of the inter-N308C distance in both the citrate bound and citrate free state, functionality test of the different dimer-forming mutants using the ${ }^{31} \mathrm{P}$ activity assay (Chapter 3) and the residue-specific assignment using ${ }^{1} \mathrm{H}$-detected MAS NMR (Chapter 2), key events underlying the activation of the kinase activity of CitA can be defined. A model for the transmembrane signal transduction mechanism from the end of the PASp domain, through the TM2 and its accompanying linker regions to the PASc domain can be developed and is summarized in Chapter 6.

## CHAPTER 5

# Transferred-Rotational-Echo DOuble Resonance (TREDOR) 

This chapter is based entirely on the following publication, and contains identical text passages: Xizhou Cecily Zhang, Marcel C Forster, Evgeny Nimerovsky, Kumar Tekwani Movellan, and Loren B Andreas. Transferred-rotational-echo double resonance. The Journal of Physical Chemistry $A, 125(3): 754-769,2021$. The author of this thesis, Xizhou Cecily Zhang, contributed to the writing of the manuscript, the development and analysis of the pulse program, the processing of the data and the structure calculation.

### 5.1 Introduction

Distance determination is the foundation for determination of 3D molecular structure via NMR, both in solution and in solid samples. Multidimensional spectra, in combination with homonuclear recoupling or spin diffusion methods have been developed for structure determination with applications to biological molecules [162, 211, 47, 219, 190, 74] and materials.[199, 62, 23] Typically, a large set of internuclear distances, often categorized as imprecise distance ranges, are used as input to simulated annealing protocols that converge to the correct protein fold. These structural representations are improved with more precise distance information.[217, 216, 74] However determination of precise distances is still extremely challenging for proteins, particularly for large proteins in the solid state where multiple dimensions are required to resolve resonances.

Improved distance precision typically requires many such multidimensional data sets, each acquired with a different mixing time such that distance-dependent buildup of magnetization can be recorded precisely. This dramatically increases the required measurement time.

Commonly, homonuclear recoupling or spin diffusion methods [4, 17, 120, 108] such as RFDR [21], DARR [207, 206] and DREAM [215] are employed for distance determination and subsequent 3D structure calculation. These have the drawback of yielding only rough distance bounds [121, 234, 122], while for solution NMR, experiments for the precise determination of these have been developed.[217, 216] Only recently, attempts at determining precise distances in the solid state using RFDR have been made.[74]

Recoupling of heteronuclear dipole interactions in magic-angle spinning (MAS) NMR is a well-established method to measure distances [151, 150] and order parameters.[13, 98, 60, 127, 129, 128, 174] Due to a favorable scaling factor and relatively low RF power requirement, one of the earlier recoupling sequences, rotational echo double resonance (REDOR) [80, 183] remains widely applied to both materials and biological samples. Since the spin part of the recoupled Hamiltonian is identical to the J-coupling Hamiltonian, a transferred sequence analogous to the solution HSQC sequence was developed soon after, and is referred to as transferred-echo double resonance (TEDOR).[92] The REDOR and TEDOR sequences were originally devised for isolated spin pairs. Application to uniformly labeled samples by addition of z-filters [101] or insertion of selective pulses [99] has extended the applicability of the method. The REDOR and TEDOR pulse sequences have also been combined sequentially with other recoupling sequences to construct multidimensional pulse sequences for assignment and distance determination.[9, 50, 180]

A key advantage of the REDOR pulse sequence is that a reference spectrum is interleaved with the dephased spectrum in order to remove the effects of transverse coherence decay. On the other hand, a key advantage of TEDOR is that the dephasing nucleus is frequency encoded, and it is possible to separate the effects of multiple dephasing spins. This has been used for the simultaneous determination of multiple distances.[101, 7] A major disadvantage in the use of

TEDOR for precise distance determination is that unlike REDOR, there is no reference spectrum to account for transverse coherence decay. To make matters worse, there is a second parameter needed to fit TEDOR data, which is an overall amplitude scaling factor. The amplitude scale is not evident from TEDOR alone, but can often be approximately determined based on TEDOR peaks arising from strong couplings or from a separate reference spectrum.[93, 94, 101] In practice, this means that when precise distances are needed, typical TEDOR data are recorded to sufficient time so as to observe a dipolar oscillation, and when only a partial oscillation can be recorded, or when the signal is over-damped due to coherence decay, free variation of the two fit parameters (amplitude scaling and coherence decay) results in fits to the data for a wide range of dipolar couplings.[7] The case of over-damping (transverse coherence decay rates of comparable magnitude to the couplings) occurs for weak couplings that encode useful structural information in protein samples, particularly for non-crystalline samples like membrane proteins, which are of great biological interest. The ${ }^{15} \mathrm{~N} \mathrm{~T}_{2}$ time, relevant during REDOR periods, is reported to be around 10 ms for non-exchanging backbone amide nitrogens in M2 protein from the influenza virus [96], and around 31 ms in perdeuterated SH 3 microcrystals ( $100 \%$ back exchanged) without decoupling.[115] In the case of deuterated proteins or ultrafast MAS, proton $T_{2}$ can also reach $\sim 5$ ms or more, long enough to acquire REDOR data [67] and suggesting that complementary $\mathrm{H}-\mathrm{C}$ distances could be recorded.

In addition to $\mathrm{T}_{2}$ decay, the effects of multiple spin interactions, as well as pulse imperfections can lead to faster signal loss during REDOR periods.[101, 196] This results in lower signal-to-noise and less precise distance determination, particularly for uniform labeled samples. Ideally, we would like to apply a sequence that can precisely determine distances using short mixing times (less than a dipolar oscillation) where the signal is still strong. At the same time, the sequence should identify both the dephased and the dephasing spins such that it can be applied to uniformly labeled samples.

We took inspiration from transfer sequences used for the measurement of homonuclear Jcouplings [116, 19, 146] and for protein assignment [76] in order to design a heteronuclear sequence that retains both the starting signal (REDOR) as well as the transferred signal (TEDOR).

The resulting transferred-rotational-echo double resonance pulse sequence (TREDOR) coacquires the chemical shifts of both dipolar coupled nuclei (here ${ }^{13} \mathrm{C}$ and ${ }^{15} \mathrm{~N}$ or ${ }^{13} \mathrm{C}$ and ${ }^{1} \mathrm{H}$ ) in one indirect dimension. Pulse sequences for two implementations of TREDOR are shown in Figure 5.1. By tracking both the original and transferred signal, it is possible to account for coherence decay at each mixing time, and in so doing to remove two fit parameters of amplitude scaling and transverse coherence decay. The result is a single parameter fit to determine the dipolar coupling.

### 5.2 Material and Methods

### 5.2.1 SH3 sample preparation

Perdeuterated chicken brain $\alpha$-spectrin SH3 was expressed, purified and crystallized based on previous publications. [160, 44] Transformed Escherichia coli BL21(DE3) cells were grown in 250 $\mathrm{ml} \mathrm{D}_{2} \mathrm{O}$-based M9 minimal medium with $3 \mathrm{~g} /{ }^{13}{ }^{13} \mathrm{C}$ - $\mathrm{d}_{7}$-glucose and $1 \mathrm{~g} /{ }^{15} \mathrm{~N}-\mathrm{NH}_{4} \mathrm{Cl}$, at $37^{\circ} \mathrm{C}$ with shaking at 120 rpm . At $\mathrm{OD}_{600 \mathrm{~nm}} 0.7$, the temperature was switched to $30^{\circ} \mathrm{C}$ until the $\mathrm{OD}_{600 \mathrm{~nm}}$ reached $\sim 0.8$ before induction with 1 mM isopropyl $\beta$-D-1-thiogalactopyranoside (IPTG). After overnight expression, SH3 was purified by anion exchange chromatography (HiTrap Q XL, GE Healthcare, 20 mM Tris, $\mathrm{pH} 8.0,1 \mathrm{mM}$ EDTA, gradient $0-1 \mathrm{M} \mathrm{NaCl}$ ), gel filtration (Superdex 75, GE Healthcare, 20 mM citric acid, $\mathrm{pH} 3.5,200 \mathrm{mM} \mathrm{NaCl}, 1 \mathrm{mM}$ EDTA) followed by dialysis against $\mathrm{H}_{2} \mathrm{O}-\mathrm{HCl}(\mathrm{pH} 3.5)$. Lyophilized protein was resuspended in $\mathrm{H}_{2} \mathrm{O}-\mathrm{HCl}(\mathrm{pH} 3.5)$ at $\sim 20 \mathrm{mg} / \mathrm{ml}$, and the same volume of $200 \mathrm{mM}\left(\mathrm{NH}_{4}\right)_{2} \mathrm{SO}_{4}\left(\mathrm{pH} 3.5,0.04 \% \mathrm{NaN}_{3}\right)$ was added. Crystallization was induced by shifting the pH to $\sim 7.0$ with gaseous $\mathrm{NH}_{3}$. Samples were subsequently kept for 3 days at $4^{\circ} \mathrm{C}$ before packing into a Bruker zirconia 1.3 mm NMR rotor using centrifugation protocol introduced previously.

### 5.2.2 NMR spectroscopy

All TREDOR SH3 spectra were recorded on a Bruker AVIIIHD 600 UltraShield spectrometer with a field strength of 14.1 Tesla, with a MASDVT600W2 BL1.3 HXY probe. The MAS frequency was set 55.555 kHz and the temperature was set to 240 K ( $1000 \mathrm{~L} / \mathrm{h}$ cooling gas). Proton and ${ }^{13} \mathrm{C}$ hard pulse powers were both 100 kHz , and ${ }^{15} \mathrm{~N}$ hard pulse power was 83.3
kHz . REDOR pulses were applied on the carbon channel, employing the xy-8 scheme [79]. TPPM heteronuclear proton decoupling [22] was 12 kHz , MISSISSIPPI water suppression [233] was applied for 100 ms with 13.9 kHz , and WALTZ-16 heteronuclear decoupling [191] was 10 kHz .

Pseudo-4D TREDOR N-Cx spectra were recorded with 8 scans and a recycle delay of 1 s , with a total acquisition time of $\sim 2$ days and 1 hour for each mixing time ( $4,6,10 \mathrm{~ms}$ ). For ${ }^{1} \mathrm{H}$, the carrier frequency was set to 4.5 ppm , acquisition time was 20.5 ms , and spectral width was 41.7 ppm. For ${ }^{13} \mathrm{C}$ (the combined dimension), the carrier frequency was 40 ppm , the acquisition time 8 ms (making the ${ }^{15} \mathrm{~N}$ acquisition time in this dimension 19.9 ms ), and the spectral width was 130.7 ppm. For ${ }^{15} \mathrm{~N}$, the carrier was 90 ppm , the acquisition time 16.5 ms , and the spectral width was $30 \mathrm{ppm} .{ }^{1} \mathrm{H}$ to ${ }^{15} \mathrm{~N}$ cross polarization was $700 \mu$ s long, with ${ }^{15} \mathrm{~N}$ power of 45 kHz and a linear power ramp on proton from 89.6 Hz to $112 \mathrm{~Hz} .{ }^{15} \mathrm{~N}$ to ${ }^{1} \mathrm{H}$ cross polarization was $500 \mu$ s long, with ${ }^{15} \mathrm{~N}$ power of 45 kHz and a linear power ramp on proton from 112 Hz to 89.6 Hz . The selective Reburp [119] pulse during the REDOR period was adjusted to have a bandwidth of 48 ppm , with an offset placing the center at 28 ppm .

Pseudo-4D TREDOR H-CO spectra were recorded with 4 scans and a recycle delay of 1.5 s , with a total acquisition time of $\sim 1$ day and 20 hours for each mixing time ( 0.6 and 1.2 ms ). For ${ }^{1} \mathrm{H}$, the carrier frequency was set to 4.5 ppm , acquisition time was 20.5 ms , and spectral width was 41.7 ppm . For ${ }^{13} \mathrm{C}$ (the combined dimension), the carrier frequency was 203.7 ppm to place the double quantum artifacts away from the signal of interest (supporting information Figure S2). The acquisition time is 7.2 ms for both ${ }^{13} \mathrm{C}$ and ${ }^{1} \mathrm{H}$, such that only ${ }^{13} \mathrm{C}$ has the correct ppm scale. The spectral width was 184.4 ppm . For ${ }^{15} \mathrm{~N}$, the carrier was 118 ppm , the acquisition time 16.5 ms, and the spectral width was $30 \mathrm{ppm} .{ }^{1} \mathrm{H}$ to ${ }^{15} \mathrm{~N}$ cross polarization was $1700 \mu$ s long with ${ }^{15} \mathrm{~N}$ power of 41 kHz and a linear power ramp on proton from 85.6 Hz to $107 \mathrm{~Hz} .{ }^{15} \mathrm{~N}$ to ${ }^{1} \mathrm{H}$ cross polarization was $600 \mu \mathrm{~s}$ long with ${ }^{15} \mathrm{~N}$ power of 45 kHz and a linear power ramp on proton from 110 Hz to 88 Hz was applied. The selective Reburp [119] pulse during the REDOR period was adjusted to have a bandwidth of 100 ppm , with an offset placing the center at 203.7 ppm .

Pseudo-4D Opa60 H-CO spectrum was recorded on a BRUKER ASCEND 1.2 GHz mag-
net equipped with a MASDVT1200S6 BL0.7 NCH probe. The MAS frequency was set to 100 kHz and the temperature to 265 K ( $425 \mathrm{l} / \mathrm{h}$ cooling gas). Proton hard pulse power was set to 147 $\mathrm{kHz},{ }^{13} \mathrm{C}$ to 114 kHz and ${ }^{15} \mathrm{~N}$ to 78 kHz . TPPM heteronuclear [22] proton decoupling was 23 kHz and MISSISSIPPI [233] water suppression was 25 kHz applied for 80 ms . The spectrum was recorded with 4 scans at two mixing times ( 0.64 ms and 0.96 ms ), and the measurement time totaled 1 day and 7 hours for each mixing time. The interscan delay was set to 0.9 s . The ${ }^{1} \mathrm{H}$ dimension had a carrier frequency at 4.72 ppm , an acquisition time of 21 ms and spectral width of 40.4 ppm . The ${ }^{13} \mathrm{C}$ dimension (the combined TREDOR dimension) has a spectral width of 331.3 ppm and an acquisition time of 3 ms with a carrier frequency at 203.7 ppm . The ${ }^{15} \mathrm{~N}$ dimension's carrier frequency was set to 120 ppm , with a spectral width of 30 ppm and an acquisition time of 6.3 ms . ${ }^{1} \mathrm{H}$ to ${ }^{15} \mathrm{~N}$ cross polarization was $1400 \mu$ s long with ${ }^{15} \mathrm{~N}$ power of 65.6 kHz and a linear power ramp on proton from 158 Hz to $197 \mathrm{~Hz} .{ }^{15} \mathrm{~N}$ to ${ }^{1} \mathrm{H}$ cross polarization was $350 \mu \mathrm{~s}$ long with ${ }^{15} \mathrm{~N}$ power of 65.6 kHz and a linear power ramp on proton from 197 Hz to 158 Hz was applied. Additionally, due to the large field drift of the newly charged magnet, we applied linear drift correction [148] to the spectra before analysis. All other parameters were the same the H-CO TREDOR acquired for SH3.

### 5.2.3 SH3 data analysis and structure calculation

SH3 TREDOR spectra were processed with Bruker TopSpin 3.5 and analysed with CcpNmr.[197, 218] Side-chain carbon and backbone carbonyl resonances were assigned using the pseudo-4D NCx and H-CO TREDOR at short mixing time and verified against published chemical shifts.[115] Extracted peak intensities were fit with equation E. 6 using MATLAB R2016b [141] to determine internuclear distances. The rms noise level was used to estimate the error in the fits. Since the random error always corresponded to less than $10 \%$, and $10 \%$ deviation can occur due to geometrical considerations [101], the imposed error for the calculation was always $10 \%$. The SH3 structure was calculated using CYANA 3.98.13.[84] Specifically, 100 structures were calculated to satisfy the TREDOR distance restraints, entered as upper and lower distance boundaries, as well as TALOS-N torsion angle restraints (generated from all assigned residues which include $\mathrm{C} \alpha, \mathrm{C} \beta$ chemical shifts).[193] Only TALOS-N "strong" predictions were included (see supporting infor-
mation Table S3). The final restraint list can be found in the supporting information. After an initial structure calculation, two TALOS-N torsion angle restraints (psi of residue 38 and phi of residue 39) were observed to violate by more than 50 degrees on average. These were removed from the restraint list. For RMSD calculations, all heteroatoms of residues 11-58 were compared. Images of protein structures were prepared using UCSF Chimera 1.11.2.[163]

### 5.2.4 Simulations

TREDOR simulations were performed with in-house MATLAB scripts by numerical solutions of the von Neumann equations of motion.[223] The numerical solution was obtained using a previously described method [152] where each of the Dyson-dependent propagators was divided on a series of N Dyson-independent propagators with the first order Hamiltonian approximation.[138, 85] For each of N propagators the analytical integration of the time dependent functions of the first order Hamiltonian was applied and N propagators in the matrix form were multiplied on each other, keeping the order. This converges to the exact solution for large enough N . The simulated signals represent the powder integration of the product of the trigonometric functions with power 2. 1154 angles were used in the powder integrations according to ZCW1. The Bessel function simulation was also performed with in-house MATLAB scripts according to the previously published Bessel approximation.

### 5.2.5 TREDOR fitting

TREDOR curves were fit in a MATLAB script (available upon request) based on the Bessel function approximation of TREDOR described in this paper. The best fit dipolar coupling was found by minimization of the reduced $\chi^{2}$ (Equation5.1).

$$
\begin{equation*}
\chi^{2}=\sum\left(\zeta_{\text {fitted }}-\zeta_{\text {experimental }}\right)^{2} \tag{5.1}
\end{equation*}
$$

The fit curves were plotted with the ggplot package in R.[165] Experimental error is estimated by propagating spectral noise (taken at one standard deviation). Fitting error was generated by Monte Carlo error analysis with 100 Monte Carlo runs assuming a Gaussian noise distribution.

### 5.3 Results and discussion

### 5.3.1 Pulse program and sequence analysis

Shown in Figure 5.1 are the pulse programs for pseudo-4D TREDOR. The pulse sequence analysis for the TREDOR period will exclusively focus on the pseudo-4D (H)(N)CNH, as the pseudo-4D (H)N(H)COH experiment requires only replacing N with H .

The TREDOR pulse sequence resembles that of the 3D zf-TEDOR introduced previously [101, 99] and modified later for proton detection [112] except for four major distinctions. First, during acquisition of the indirect (carbon) dimension, TREDOR co-acquires the untransferred (nitrogen) signal. These spectral regions can be placed in the spectrum relative to one another by appropriate placement of the offset, and need not have the same sampling rate. Additional phases and appropriate processing of sum and differences could also be used to separate the two pathways.[192] We used a dwell time ratio of $\sim 2.48$, such that both carbon and nitrogen peaks display correctly in ppm after Fourier transformation. Second, TREDOR removes the first z-filter, since it is incompatible with storing both transferred and dephased signals that lie along x and y after the first REDOR period. The second z -filter can be retained, and doubles as water suppression. Third, our implementation of TREDOR begins with cross polarization (CP) to nitrogen, since ${ }^{15} \mathrm{~N}-{ }^{15} \mathrm{~N}$ J couplings are negligible, and therefore antiphase terms associated with homonuclear J-couplings do not build up during the first REDOR period. This allows the removal of the z-filter without significant spectral artifacts even at long mixing times. Fourth, rather than detecting a heteronucleus, the TREDOR sequence is implemented here with a final CP to proton for detection, in order to improve sensitivity and to resolve the resonances in an additional dimension.

For the case of two spins, the pulse program can be understood with a product operator analysis as follows, where we start with transverse nitrogen magnetization generated by CP from


Figure 5.1: Pseudo-4D TREDOR $(H)(N) C N H$ and $(H) N(H) C H$ pulse sequences shown in $(A)$ and (B), respectively. Narrow and wide filled rectangles represent hard $\pi / 2$ and $\pi$ pulses respectively, while soft selective pulses on the carbon channel are shown as parabolas. The REDOR periods are implemented with the usual two hard $\pi$ pulses [80,183] per rotor period applied to the carbon channel. REDOR pulses were cycled according to to the $x y-8$ scheme.[79] In the middle of each REDOR period, a REBURP [119] shaped pulse is used to select the ${ }^{13} \mathrm{C}$ chemical shifts of interest. For ${ }^{15} \mathrm{~N}-{ }^{13} \mathrm{C}_{\alpha}$ TREDOR, the bandwidth of this pulse is set to 40 to 70 ppm ; for ${ }^{15} \mathrm{~N}-{ }^{13} \mathrm{Cx}$ TREDOR, to 5 to 53 ppm , which should refocus all side-chain ${ }^{13} \mathrm{C}$ shifts except for that of the $\mathrm{C}_{\beta}$ of serine and threonine; for H-CO TREDOR, to 154 ppm to 254 ppm . In (A) water suppression [233] is split before and after acquisition of the second dimension $\left(\mathrm{t}_{2}\right)$. This doubles as two z-filter elements, allowing a reduced phase cycle. Pulses were phase cycled as $\Phi_{1}=11333311, \Phi_{2}=00222200, \Phi_{3}=$ $01, \Phi_{5}=0022, \Phi_{6}=1133, \Phi_{7}=0022, \Phi_{8}=2200, \Phi_{9}=0022, \Phi_{10}=2, \Phi_{r e c^{\prime} r}=02202002$, where $0=x, 1=y, 2=-x, 3=-y$. Unless indicated, other pulses have phase 0 . To conveniently encode a correct ppm scale during acquisition of the first indirect dimension in (A) for both ${ }^{15} \mathrm{~N}$ and ${ }^{13} \mathrm{C}$, the increment of the ${ }^{13} \mathrm{C}$ shifts $\mathrm{t}_{1 C}$ is set to $\mathrm{t}_{1 N}{ }^{*}\left(\gamma^{15} \mathrm{~N} /{ }^{13} \mathrm{C}\right)$, where $\gamma$ is the gyromagnetic ratio, so that ${ }^{15} \mathrm{~N}$ and ${ }^{13} \mathrm{C}$ will share the same ppm scale. Hypercomplex data were acquired by shifting $\Phi_{7}, \Phi_{8}, \Phi_{10}$ by -90 degrees, and $\Phi_{9}$ by +90 in a separate acquisition to acquire pure phases, according to the procedure of Ruben and co-workers.[200]
the protons:

$$
\begin{align*}
\mathbf{N}_{x} & \xrightarrow{R E D O R} \mathrm{~N}_{x} \mathrm{c}_{12}+2 \mathbf{N}_{y} \mathrm{C}_{z} \mathrm{~s}_{12} \xrightarrow{90 x(\mathrm{~N}), 90-x(\mathrm{C})} \mathrm{N}_{x} \mathbf{c}_{12}+2 \mathbf{N}_{z} \mathrm{C}_{y} \mathrm{~s}_{12} \\
& \xrightarrow{t_{1 N}, t_{1} C} \\
& \mathrm{~N}_{x} \mathrm{c}_{12} \cos \left(\Omega_{N} t_{1 N}\right)+2 \mathbf{N}_{z} \mathrm{C}_{y} \mathrm{~s}_{12} \cos \left(\Omega_{C} t_{1 C}\right) \\
& \xrightarrow{90_{x}(\mathrm{~N}), 90_{x}(\mathrm{C})} \mathrm{N}_{x} \mathrm{c}_{12} \cos \left(\Omega_{N} t_{1 N}\right)-2 \mathbf{N}_{y} \mathrm{C}_{z} \mathrm{~s}_{12} \cos \left(\Omega_{C} t_{1 C}\right)  \tag{5.2}\\
& \xrightarrow{R E D O R} \mathrm{~N}_{x}\left[\mathrm{c}_{12}^{2} \cos \left(\Omega_{N} t_{1 N}\right)+\mathrm{s}_{12}^{2} \cos \left(\Omega_{C} t_{1 C}\right)\right]
\end{align*}
$$

with

$$
\begin{aligned}
& \mathrm{s}_{12}=\sin \left(\omega \frac{t_{m i x}}{2}\right) \\
& \mathrm{c}_{12}=\cos \left(\omega \frac{t_{m i x}}{2}\right)
\end{aligned}
$$

All terms not converted to observable magnetization are ignored. The analysis presented here follows the real part of the signal in $t_{1}$; that is, the cosine-modulated part of the signal. Since the spin part of the Hamiltonian is identical to a J-coupling, the analysis is essentially identical to the 'in-phase COSY' [19] with the only difference being the orientation dependence of the coupling frequency $\omega$, as in REDOR and TEDOR. The first REDOR period creates antiphase carbon coherence with respect to nitrogen $\left(\mathrm{N}_{y} \mathrm{C}_{z}\right)$, which is frequency labeled in $\mathrm{t}_{1 \mathrm{C}}$ with the ${ }^{13} \mathrm{C}$ chemical shift after coherence transfer $\left(\mathrm{N}_{z} \mathrm{C}_{y}\right)$ with two $\pi / 2$ pulses. The second REDOR period then converts it back to in-phase nitrogen magnetization, which is subsequently frequency labeled in $t_{2}$ with the ${ }^{15} \mathrm{~N}$ chemical shift. The remaining untransferred nitrogen magnetization $\left(\mathrm{N}_{x}\right)$ stays the same during both REDOR periods; it is frequency labeled in both $t_{1 N}$ and $t_{2}$ with the ${ }^{15} \mathrm{~N}$ chemical shift and will thus appear as diagonal peaks in the $t_{1}$ and $t_{2}$ dimensions. Fortunately, there are relatively few untransferred nitrogen signals, one for each residue, while there are potentially many transferred signals that are resolved in an additional dimension. It should also be noted that during acquisition of the first indirect dimension, the carbon spins $\left(-2 \mathrm{~N}_{z} \mathrm{C}_{y}\right)$ have a 180 degree phase shift with respect to the untransferred ${ }^{15} \mathrm{~N}$ shifts $\left(\mathrm{N}_{x}\right)$. They will thus appear with opposite sign in the spectrum and are easily distinguishable.

In proteins, spin systems typically contain multiple couplings, which has the potential to
generate multiple quantum terms. For such cases, the product operator analysis for a $\mathrm{NC}_{2}$ spin system with the nitrogen coupled to two carbon spins can be considered explicitly, as follows, again starting from nitrogen transverse magnetization:

$$
\begin{align*}
& \mathrm{N}_{x} \xrightarrow{\omega_{12} 2 N_{z} C_{2 z}, \omega_{13} 2 N_{z} C_{3 z}} \mathrm{~N}_{x} \mathrm{c}_{12} \mathrm{c}_{13}+2 \mathrm{~N}_{y} C_{2 z} \mathrm{~s}_{12} \mathrm{c}_{13}+2 \mathrm{~N}_{y} C_{3 z} \mathrm{c}_{12} \mathrm{~s}_{13}-4 \mathrm{~N}_{x} C_{2 z} C_{3 z} \mathrm{~s}_{12} \mathrm{~s}_{13} \\
& \xrightarrow{90 x(\mathrm{~N}), 90-x}{ }^{(\mathrm{C})} \mathrm{N}_{x} \mathrm{c}_{12} \mathrm{c}_{13}+2 \mathrm{~N}_{z} C_{2 y} \mathrm{~s}_{12} \mathrm{c}_{13}+2 \mathrm{~N}_{z} C_{3 y} \mathrm{c}_{12} \mathrm{~s}_{13}-4 \mathrm{~N}_{x} C_{2 y} C_{3 y} \mathrm{~s}_{12} \mathrm{~s}_{13} \\
& \xrightarrow{t_{1 N}, t_{1} C} \mathrm{~N}_{x} \mathrm{c}_{12} \mathrm{c}_{13} \cos \left(\Omega_{N} t_{1 N}\right)+2 \mathrm{~N}_{z} C_{2 y} \mathrm{~s}_{12} \mathrm{c}_{13} \cos \left(\Omega_{2 C} t_{1 C}\right)+2 \mathrm{~N}_{z} C_{3 y} \mathrm{c}_{12} \mathrm{~s}_{13} \cos \left(\Omega_{3 C} t_{1 C}\right) \\
& -4 \mathrm{~N}_{x} C_{2 y} C_{3 y} \mathrm{~s}_{12} \mathrm{~s}_{13} \cos \left(\Omega_{N} t_{1 N}\right) \cos \left(\Omega_{2 C} t_{1 C}\right) \cos \left(\Omega_{3 C} t_{1 C}\right) \\
& \xrightarrow{90_{x}(\mathrm{~N}), 90_{x}(\mathrm{C})} \mathrm{N}_{x} \mathrm{c}_{12} \mathrm{c}_{13} \cos \left(\Omega_{N} t_{1 N}\right)-2 \mathrm{~N}_{y} C_{2 z} \mathrm{~s}_{12} \mathrm{c}_{13} \cos \left(\Omega_{2 C} t_{1 C}\right)-2 \mathrm{~N}_{y} C_{3 z} \mathrm{c}_{12} \mathrm{~s}_{13} \cos \left(\Omega_{3 C} t_{1 C}\right) \\
& -4 \mathrm{~N}_{x} C_{2 z} C_{3 z} \mathrm{~s}_{12} \mathrm{~s}_{13} \cos \left(\Omega_{N} t_{1 N}\right) \cos \left(\Omega_{2 C} t_{1 C}\right) \cos \left(\Omega_{3 C} t_{1 C}\right) \\
& \omega_{12} 2 N_{z} \xrightarrow{C_{2 z}, \omega_{13} 2 N_{z} C_{3 z}} \mathrm{~N}_{x} \mathrm{c}_{12}^{2} \mathrm{c}_{13}^{2} \cos \left(\Omega_{N} t_{1 N}\right)+\mathrm{N}_{x} \mathrm{~s}_{12}^{2} \mathrm{c}_{13}^{2} \cos \left(\Omega_{2 C} t_{1 C}\right)+\mathrm{N}_{x} \mathrm{c}_{12}^{2} \mathrm{~s}_{13}^{2} \cos \left(\Omega_{3 C} t_{1 C}\right) \\
& +\mathrm{N}_{x} \mathrm{~s}_{12}^{2} \mathrm{~s}_{13}^{2} \cos \left(\Omega_{N} t_{1 N}\right) \cos \left(\Omega_{2 C} t_{1 C}\right) \cos \left(\Omega_{3 C} t_{1 C}\right) \tag{5.3}
\end{align*}
$$

with

$$
\begin{aligned}
& \mathrm{s}_{12}=\sin \left(\omega_{12} \frac{t_{m i x}}{2}\right) \\
& \mathrm{c}_{12}=\cos \left(\omega_{12} \frac{t_{m i x}}{2}\right) \\
& \mathrm{s}_{13}=\sin \left(\omega_{13} \frac{t_{m i x}}{2}\right) \\
& \mathrm{c}_{13}=\cos \left(\omega_{13} \frac{t_{m i x}}{2}\right)
\end{aligned}
$$

All multiple quantum terms not converted to detectable signal are ignored in the analysis, however, one multiple quantum term survives. There is a 3 -spin term, $4 \mathrm{~N}_{\mathrm{x}} \mathrm{C}_{2 \mathrm{y}} \mathrm{C}_{3 \mathrm{y}}$ during $\mathrm{t}_{1}$ evolution, that could appear in the first dimension with a frequency that is dependent on the chemical shifts of all spins. The term is modulated by a sine squared function of both active coupling strengths, such that it builds up more slowly. We identified such multiple quantum signals for H-C TREDOR, as weak peaks placed at the sum of the 3 chemical shifts, and at the proton shift minus the sum of the carbon offsets (see Figure S2). These produce artifacts in the spectrum, similar to those detailed
previously [101] but the position of the artifacts can be placed away from the peaks of interest such that they do not degrade the spectrum.

For a $\mathrm{N}_{1}-\mathrm{C}_{i}$ spin pair with an active dipolar coupling of $\omega_{1 i}$, its crosspeak intensity $V_{1 i}\left(t_{m i x}\right)$ in a TEDOR-type spectrum with mixing time $\mathrm{t}_{\text {mix }}$, is given as:

$$
\begin{equation*}
V_{1 i}\left(t_{m i x}\right)=V_{1}(0) \exp \left(-\Gamma_{1} t_{m i x}\right)\left\langle\sin ^{2}\left(\omega_{1 i} t_{m i x} / 2\right) \prod_{k=1 \neq i}^{n_{i}} \cos ^{2}\left(\omega_{1 k} t_{m i x} / 2\right)\right\rangle \tag{5.4}
\end{equation*}
$$

We follow the notation previously introduced [101] in which $V_{1}(0)$ is the intensity of the $\mathrm{N}_{1}$ spin at 0 ms mixing time, $n_{i}$ is the number of ${ }^{13} \mathrm{C}$ nuclei that are simultaneously coupled to $\mathrm{N}_{1}$ within the same spin system with a passive coupling of $\omega_{1 k}$. The $\rangle$ symbols indicate a powder average. The parameter $\Gamma_{1}$ gives the coherence decay rate of the spin coherence, which can be modeled as a single exponential. The corresponding REDOR-type nitrogen signal, dephased by all multiple couplings inside the system, is:

$$
\begin{align*}
V_{1}\left(t_{m i x}\right) & =V_{1}(0) \exp \left(-\Gamma_{1} t_{m i x}\right)\left\langle\prod_{k=1}^{n_{i}} \cos ^{2}\left(\omega_{1 k} t_{m i x} / 2\right)\right\rangle  \tag{5.5}\\
& =V_{1}(0) \exp \left(-\Gamma_{1} t_{m i x}\right)\left\langle\cos ^{2}\left(\omega_{1 i} t_{m i x} / 2\right) \prod_{k=1 \neq i}^{n_{i}} \cos ^{2}\left(\omega_{1 k} t_{m i x} / 2\right)\right\rangle \tag{5.6}
\end{align*}
$$

In the pseudo-4D TREDOR spectrum, since the intensity of the untransferred part of the magnetization is also recorded, the following ratio $\zeta_{i j}\left(t_{m i x}\right)$ of REDOR and TREDOR terms approximately removes the influence of coherence decay and passive couplings:

$$
\begin{align*}
& \zeta_{1 i}\left(t_{m i x}\right)=\frac{V_{1 i}\left(t_{m i x}\right)}{V_{1}\left(t_{m i x}\right)+V_{1 i}\left(t_{m i x}\right)}  \tag{5.7}\\
& =\frac{\left\langle\sin ^{2}\left(\omega_{1 i} t_{m i x} / 2\right) \prod_{k=1 \neq i}^{n_{i}} \cos ^{2}\left(\omega_{1 k} t_{m i x} / 2\right)\right\rangle}{\left\langle\sin ^{2}\left(\omega_{1 i} t_{m i x} / 2\right) \prod_{k=1 \neq i}^{n_{i}} \cos ^{2}\left(\omega_{1 k} t_{m i x} / 2\right)+\cos ^{2}\left(\omega_{1 i} t_{m i x} / 2\right) \prod_{k=1 \neq i}^{n_{i}} \cos ^{2}\left(\omega_{1 k} t_{m i x} / 2\right)\right\rangle}  \tag{5.8}\\
& =\frac{\left\langle\sin ^{2}\left(\omega_{1 i} t_{m i x} / 2\right) \prod_{k=1 \neq i}^{n_{i}} \cos ^{2}\left(\omega_{1 k} t_{m i x} / 2\right)\right\rangle}{\left\langle\prod_{k=1 \neq i}^{n_{i}} \cos ^{2}\left(\omega_{1 k} t_{m i x} / 2\right)\right\rangle}  \tag{5.9}\\
& \approx\left\langle\sin ^{2}\left(\omega_{1 i} t_{m i x} / 2\right)\right\rangle \tag{5.10}
\end{align*}
$$

The TREDOR parameter $\zeta_{1 i}\left(t_{m i x}\right)$ is free of the impact of coherence decay, if both the transferred and the total magnetization follow the same decay properties during the REDOR periods. This is found to be true for SH 3 spectra, even though ${ }^{15} \mathrm{~N} \mathrm{~T}_{2}$ is not the dominant source of signal loss, as discussed later. The ratio $\zeta_{1 i}\left(t_{m i x}\right)$ does not depend on the starting signal or need correction for experimental imperfections as both signals are acquired simultaneously. Similar to REDOR, the buildup of $\zeta_{1 i}\left(t_{m i x}\right)$ is sensitive to the strength of the dipolar coupling and follows an absolute amplitude scale such that dipolar coupling measurements can be performed with short mixing times before the first dipolar oscillation. A good approximation based on the expansion of Bessel functions was derived previously [147] to describe the powder averaged dipolar recoupling signal under MAS. Only the zeroth order Bessel function expansion $J_{0}(x)$ is needed to describe the observed signal buildup, and the error introduced by ignoring the relative orientations of the active and passive dipolar couplings was shown to be less than 5 to 10 percent.[101] The ratio $\zeta_{1 i}\left(t_{m i x}\right)$ can then be approximated as:

$$
\begin{equation*}
\zeta_{1 i}\left(t_{m i x}\right)=\frac{1}{2}\left(1-\left[J_{0}\left(\sqrt{2} D_{1 i} t_{m i x}\right)\right]^{2}\right) \tag{5.11}
\end{equation*}
$$

where $\mathrm{J}_{0}$ is the $0^{\text {th }}$ order Bessel function. This applies for any spin pair 1 i in which the spin 1 is coupled to an arbitrary number of heteronuclei i. Formally, this means that the TREDOR curve will build up to a maximum value of 0.5 in a fully labeled sample. Partial labeling of the dephasing nucleus would result in a predictable down-scaling of the TREDOR curve. In a standard TEDOR fit [101], to extract the dipolar couplings, one needs to additionally fit the overall coherence decay rate and an arbitrary amplitude scaling factor since the starting signal is typically not recorded. This consequently puts a high demand on the data density, i.e. many mixing times recorded. In comparison to TEDOR, TREDOR reduces the number of fit parameters by two, which as shown in the later sections allows determination of the dipolar couplings, and therefore $\mathrm{C}-\mathrm{N}$ distances, with a single mixing time. The two fit parameters that are removed by TREDOR are an amplitude scaling factor and a relaxation parameter, namely $V_{1}(0)$ and $\Gamma_{1}$ in equation 5.4)

### 5.3.2 Buildup of the multiple quantum terms

For a multiple spin system with an I spin coupled to more than one spin, the product operator analysis showed that there exists a multiple quantum term that is modulated by two couplings (Equation 5.3). This term is eliminated in zf-TEDOR by the first z-filter, but not removed in TREDOR. It could be detected by an appropriate phase cycle to select double or zero quantum coherences, however, the term builds up slower than the antiphase TEDOR terms (Figure 5.2), and will therefore be more difficult to detect. In TREDOR, it represents a mechanism for total signal loss, and we observe artifacts from this term in the H-CO TREDOR spectrum at the expected offsets for the component that is double quantum in carbon (see Figure S2). The artifacts are similar in appearance to those seen before for carbon detected TEDOR.[101] We simulated the buildup of this term for an $\mathrm{NC}_{2}$ spin system with similar couplings (Figure 5.2A), and found that it is negligible when the mixing time is smaller than 8 ms . However, when the two couplings are different, the buildup of this term can be as fast as the desired TEDOR term (Figure 5.2B)[48], which explains the observation of artifacts in the $\mathrm{H}-\mathrm{CO}$ spectra. (The artifacts can be placed such that they do not obscure the desired peaks, see the experimental section and supporting information). However, for mixing times smaller than 4 ms , the contribution of this term is in all cases negligible for N-C TREDOR. Multiple quantum terms with even higher coherence orders coming from systems with more than three spins are not considered, as they will build up even more slowly than the double quantum terms. The influence of passive couplings in a multi-spin system is also revealed by the exact simulation (Figure 5.2C). For the coupling of interest, the modulation by passive couplings in the system leads to a slight damping of the buildup compared with simulation of an isolated spin pair which could bias the fitting towards a slightly larger distance ( $4.1 \AA$ instead of $4 \AA$ ). This bias could be reconciled by fitting TREDOR curves in a system-wide way, taking into account the modulation by other couplings (supporting information). However, for us, the analysis with the single curve fit method (Equation 5.11) produced the same results within experimental error.


Figure 5.2: Build up of multiple quantum terms in pseudo-4D TREDOR as a function of mixing time. In (A) and (B) an $\mathrm{NC}_{2}$ system was simulated by an exact numerical method, with distances of $\mathrm{r}_{N C_{1}}=3 \AA$ and $\mathrm{r}_{N C_{2}}=3.5 \AA$, and of $\mathrm{r}_{N C_{1}}=2.5 \AA$ and $\mathrm{r}_{N C_{2}}=4 \AA$, respectively. The black line shows buildup of transferred signal via the $2 \mathrm{~N}_{y} \mathrm{C}_{z_{1}}$ operator, the thick red line shows the buildup of the $2 \mathrm{~N}_{y} \mathrm{C}_{z_{2}}$ term, and the blue dotted line shows the buildup of the $4 \mathrm{~N}_{x} \mathrm{C}_{z_{1}} \mathrm{C}_{z_{2}}$ term. The area indicated with a yellow rectangle is expanded in the inset to show the difference in initial buildup rates. In (C), exact simulation of TREDOR signal for a nitrogen-carbon spin pair with distance of $4 \AA$ in a $\mathrm{NC}_{4}$ system (black line), for isolated nitrogen-carbon spin pairs with distances of $4 \AA$ (thin red dashed line), $4.1 \AA$ (red dashed line) and $4.2 \AA$ (thick red dashed line) is shown.

### 5.4 TREDOR fitting

To test the performance of TREDOR in measuring accurate distance information in a protein, spectra were acquired at different mixing times for the microcrystalline protein SH 3 . Since pulse imperfections and RF inhomogeneity impact the apparent dipolar oscillation, we used the one bond $\mathrm{N}_{H}-\mathrm{C}_{\alpha}$ distance of Glycine 51 to calibrate the fit dipolar coupling (Figure 5.3). Since in our spectrum, both dimensions are undersampled, both ${ }^{13} \mathrm{C}$ and ${ }^{15} \mathrm{~N}$ have approximately the same lineshape such that the use of peak amplitude was a good measure of the intensity. In other cases, it may be necessary to integrate peaks, or scale amplitudes according to the linewidths. The theoretical dipolar coupling for a rigid one-bond distance of $1.45 \AA$ [58] between ${ }^{15} \mathrm{~N}$ and ${ }^{13} \mathrm{C}$ is 1005 Hz when delta pulses are assumed, compared with the coupling value of 810 or 798 Hz measured using TREDOR, giving us an overall scaling factor of 0.8 . One contribution to scaling is the result of non-perfect coherence transfer caused by non-ideal pulses. These imperfections include RF inhomogeneity [155, 196], pulse miscalibration and finite pulse effects [102], all of which can be simulated. Under our experimental conditions, the finite pulse effect accounts for a scaling of the dipolar coupling by 0.93 . The remaining scaling comes from inhomogeneity, as well as a true scaling, which is a result of fast molecular motions at ambient temperature [64, 210, 89], compared with a low temperature crystal. This factor can be approximated by the order parameter which is reported to be about 0.9 at the protein backbone.[86,182,184,13] Combining the two factors, finite pulses and order parameter, already comes close to the measured scaling factor of 0.8 . This value was used to calibrate all other measured distances.

Since TREDOR extracts dipolar couplings by fitting a single parameter, in principle, only one data point is needed for fitting each curve. Figure 5.4 shows TREDOR distance determination for structurally important distances using 1 , 2, or 3 mixing points (Figure 5.4A). The full set of distances (above 3-bonds separated) are shown in panel A. All two point fits correctly reported the same distance as the three point fits. However, in some cases, single points with very short (4 ms ) or very long mixing time ( 10 ms ) lead to deviation from the fitting with the full set, while the 6 ms mixing time provided faithful fitting. To some degree this is expected, in particular for stronger couplings, due to the non-monotonous nature of the dipolar oscillation curve; without


Figure 5.3: Pseudo 4D $\mathrm{N}-\mathrm{C}_{\alpha}$ TREDOR and determination of scaling factor. The 2D carbon(nitrogen)-proton plane of pseudo $4 \mathrm{D} \mathrm{N}-\mathrm{C}_{\alpha}$ TREDOR at 5.8 ms TREDOR mixing is shown in (A). Positive signals from ${ }^{13} \mathrm{C}$ resonances are contoured in orange while the negative ${ }^{15} \mathrm{~N}$ signals are shown in black. The peaks of Glycine 51 of the untransferred ${ }^{15} \mathrm{~N}$ and transferred carbon resonances are indicated with black crosses. (B) Signal modulation of dephased and transferred magnetization of Glycine $51 \mathrm{~N}-\mathrm{C}_{\alpha}$, shown as 1D carbon (nitrogen) dimension traces at different mixing times. The relevant peaks are as labeled. (C) Fitting of the experimental TREDOR signal to two spin simulations $\zeta_{N-C \alpha}$ with Bessel approximation (black) and exact numerical simulation (red). The dipolar coupling is fit to 810 Hz with the Bessel approximation and to 798 Hz with the exact numerical simulation, which corresponds to a $\mathrm{N}-\mathrm{C}_{\alpha}$ distance of $1.45 \AA$ [58] in the crystal structure (inset), revealing a scaling factor of 0.8 (details in text). Asterisks indicates overlapped signals from residues K18, K59, I30 and E45, which are separated in the pseudo-4D spectrum.
prior knowledge of the range of reasonable coupling values, a single point might result in an unstable fit. However, such a case can be easily recognized, since it will only occur when the measured point reaches close to the maximum value of 0.5 . Importantly, site-specific distance information was readily determined with short mixing times of 4 and 6 ms , which suggests that the method will be applicable to samples with a wide range of relaxation properties. In Figure 5.4B-E, both intra-residue (Va19N to Va19C $\mathcal{\beta}_{\beta}$ and $\mathrm{C}_{\gamma}$ ) and inter-residue ( $\operatorname{Trp} 42 \mathrm{~N}_{\epsilon}$ to Ala55C ${ }_{\beta}$ ) distances are highlighted. Since these distances are well isolated in pseudo-4D TREDOR spectra and have known dipole couplings, we chose them to show in detail how TREDOR faithfully reproduces their N to C distance even with sparse data. The $\operatorname{Trp} 42 \mathrm{~N}_{\epsilon}$ to Ala55C $\mathrm{C}_{\beta}$ distance is of particular interest for three-dimensional protein structure determination, and was investigated previously using REDOR in a specifically labeled sample.[134] We found the same dipolar coupling using TREDOR, but in a uniformly labeled sample. The TREDOR measured value after scaling of 55.3 $\pm 1.4 \mathrm{~Hz}$ is equivalent to the previously reported $53 \pm 8 \mathrm{~Hz}$ within experimental error. Figure 5.4F shows resolved cross-peaks in the pseudo-4D HCO TREDOR spectrum.

### 5.4.1 Coherence decay under TREDOR and Choice of Mixing Time

As TREDOR fitting with a single point is possible (Figure 5.4A), it makes sense to choose the optimal mixing time that will provide the most precise fitting. Two opposing factors must be taken into consideration. First, the mixing time needs to be sufficiently long so that the signal can build up, and second, the overall intensity should not relax beyond detection. Since TREDOR measures multiple couplings simultaneously, there will not be a single optimum. Nevertheless, a single mixing point is near optimal for the range of structurally relevant couplings below about 100 Hz , as detailed below. The trade-off between the two factors can be modeled by scaling the TREDOR curve by an exponential decay as in Equation 5.12, taking again the Bessel approximation of powder averaged dipolar recoupling. Additionally, the uncertainty in the TREDOR curve is not constant, but is reduced for later mixing times due to the additional information detected in the


Figure 5.4: Dipolar couplings extracted from pseudo-4D N-Cx and H-CO TREDOR with different sets of mixing times. (A) shows all contacts found in SH 3 , with dipole coupling measured by fitting subsets of one mixing time (black) and two mixing times (blue) plotted against the fit with the complete set. Site-specific TREDOR fitting for (B,D) Val9 N (C,E) $\operatorname{Trp} 42 \mathrm{~N}_{\epsilon}$, with distances from crystal structure as inset. Bessel function fits are shown with three mixing times (solid line), sets of two mixing times (dashed lines), and single mixing time (dotted lines). (F) shows exemplary TREDOR H-CO strips for $\operatorname{Trp} 42 \mathrm{~N}_{\epsilon}, \operatorname{Val} 9 \mathrm{~N}$, and Gly51 N with a mixing time of 1.2 ms .

REDOR part of the signal. Combining both factors,

$$
\begin{equation*}
S / N_{1 i}\left(t_{m i x}\right)=\exp \left(-\Gamma_{i} t_{m i x}\right) \frac{V_{1 i}\left(t_{m i x}\right)}{V_{1}\left(t_{m i x}\right)+V_{1 i}\left(t_{m i x}\right)}\left[\frac{V_{1 i}\left(t_{m i x}\right)^{2}+V_{1 i}\left(t_{m i x}\right)^{2}}{\left(V_{1}\left(t_{m i x}\right)+V_{1 i}\left(t_{m i x}\right)\right)^{2}} \sigma^{2}\right]^{-0.5} \tag{5.12}
\end{equation*}
$$

The optimal mixing time is found when $S / N_{1 i}\left(t_{m i x}\right)$ is at its maximum. This represents a 'transfer efficiency' that takes into consideration the signal available from both the REDOR and TEDOR components. We simulated several combinations of active and passive couplings that are representative of typical spin systems relevant for protein structure determination (Figure 5.5). We found that for a microcrystalline sample like SH 3 , this optimal mixing time is around 8 ms for a typical $\mathrm{N}_{H}-\mathrm{C}_{\beta}$ coupling of 132 Hz , when the coherence decay time is 10 ms (Figure 5.5 A ). For coupling strengths relevant for structure calculation, which are around 30 to 60 Hz for measuring torsion angles or long range distances in proteins, the optimal mixing time is below 8 ms when the transverse decay time is smaller than 10 ms . However, in practice, it is advisable to use mixing times slightly smaller than that. This is not only to observe spins with short site-specific transverse coherence lifetime, but also to more accurately fit those that have a larger $\mathrm{N}_{H}-\mathrm{C}_{\beta}$ coupling. This explains our observation that a mixing time of 6 ms leads to the most stable fitting. The effect of other passive couplings in the system is seen by comparing the buildup of similar couplings with varying number and strength of passive couplings. When a relatively weak dipolar coupling ( 30 or 60 Hz ) is modulated by two passive couplings ( $150 \mathrm{~Hz}, 65 \mathrm{~Hz}$ ), the absolute intensity is only slightly smaller than when there is only one passive coupling ( 150 Hz ). In the extreme case, when a weak coupling $(60 \mathrm{~Hz})$ is modulated by a very large passive coupling ( 800 Hz ) (Figure 5.5 D ), the overall profile of the buildup is similar to a smaller passive coupling (Figure 5.5D) but with slightly reduced intensity. This shows that the optimal mixing time is mostly determined by the coherence decay rate and the active coupling. Equation 5.7 assumes the decay of both the REDOR and TEDOR part of the magnetization is dominated by a single exponential decay, which would follow if it is dominated by ${ }^{15} \mathrm{~N} \mathrm{~T}_{2}$. This can be checked experimentally by comparing the decay of total signal in TREDOR for each residue in SH3. Indeed, one single exponential decay rate results in a good fit to the total signal decay (Figure 5.6). Surprisingly though, the coherence decay under TREDOR is much faster than the ${ }^{15} \mathrm{~N}_{2}$ measured site-specifically via the dephased signals in the (H)NH spectrum. This potentially originates from relaxation of the multiple quantum terms generated during


Figure 5.5: Bessel approximation of the TREDOR 'transfer efficiency', shown as signal to noise $S / N_{1 i}$ in spin systems with different combinations of active and passive dipolar coupling. Typical active C-N dipole coupling strengths for proteins are indicated, with passive coupling(s) in brackets. Different site-specific coherence decay rates are also included; the system with one spin (A), two ( $\mathrm{B}, \mathrm{D}, \mathrm{E}$ ) and three ( $\mathrm{C}, \mathrm{F}$ ) coupled spins all have an optimal mixing time between 4 to 16 ms when $T_{2}$ is smaller than 10 ms . The maximum TREDOR signal to noise when decay time is short $(<10 \mathrm{~ms})$ is around 5 percent of the starting signal for a 60 Hz coupling and around 2 percent for 30 Hz coupling. Optimal mixing times when the decay time is 5 ms (grey dashed lines) and 2 ms (black dashed lines) are indicated.
the REDOR periods from non ideal pulses. One potential origin is the RF inhomogeneity of the hard pulses during REDOR which will cause incomplete inversion of anti-phase terms $2 \mathrm{~N}_{y} \mathrm{C}_{z}$. In that case, the additional undesired operators $-2 \mathrm{~N}_{y} \mathrm{C}_{x}$ and $2 \mathrm{~N}_{y} \mathrm{C}_{y}$ are created. The effects are minimized with xy phase cycling [79], but not removed. The quantitative description of the influence of the RF inhomogeneity on the TREDOR signal is complicated with the additional influences of the carbon offset, the external field inhomogeneity, the carbon chemical shift anisotropy interaction, the carbon spin-spin relaxation, and non-ideal long selective pulses. All these effects can be approximately replaced with the influence of the apparent spin-spin coherence decay, i.e the measured decay of the combined REDOR and TEDOR parts of the signal. The REDOR pulses on the carbon channel could also result in decoherence through a $\mathrm{T}_{2 \rho}$ process. We measured the bulk $\mathrm{T}_{2 \rho}$ of $\mathrm{C} \alpha$ and $\mathrm{C}^{\prime}$ with various spin lock offsets and power (supporting information Table S 4 and Table S5). However, $\mathrm{T}_{2 \rho}$ values of interest are significantly longer than the apparent relaxation rate in TREDOR, eliminating $\mathrm{T}_{2 \rho}$ as the major contributor to signal losses. The dramatic increase in decay rates further justifies the need for a dipolar recoupling measurement that only requires a short mixing time. Figure 5.6 indicates coherence decay times of about 5 to 10 ms . Note that several residues deviate from the average, but this is likely the result of fitting only 3 time points. A typical TREDOR decay time of 5 to 10 ms indicates an ideal TREDOR mixing time of around 6 ms (Figure 5.5), and the stable fits for 4 and 6 ms suggest that TREDOR will also be useful in the case of faster decay.

### 5.4.2 Structure calculation

We recorded site-specific TREDOR data on a microcrystalline SH3 sample and performed a structure calculation. The structure of SH 3 has previously been calculated [40] using ${ }^{13} \mathrm{C}$-detected solid-state NMR, based largely on restraints derived from a set of PDSD spectra with a range of mixing times. The distances determined from pseudo-4D TREDOR (full fitting information available in supporting information) are in good agreement with a previously published crystal structure of the SH3 domain (PDB-code 2NUZ). Discrepancies are mostly due to spectral overlap or ambiguous assignments. The fit dipolar couplings were multiplied with the previously determined scaling factor of 1.25 and converted to distances. Unambiguous pseudo-4D N-Cx TREDOR re-


Figure 5.6: Site-specific ${ }^{15} \mathrm{~N} \mathrm{~T}_{2}$ rate during TREDOR (A yellow) and (H)NH (A dark blue) and (H)NH spectrum at 0 ms delay (B). The topology of SH 3 is plotted under (A); there is no obvious correlation of the size of the ${ }^{15} \mathrm{~N} \mathrm{~T}_{2}$ with the secondary structure of the residue. The coherence decay rate under TREDOR is significantly higher than that under (H)NH (supporting information table S 1 ); but for all residues, a single exponential decay well predicts the total signal decay (examples of decay of residues A55, G51 and W42 are shown in (C), (D) and (E)).
straints relevant for torsion angle determination can be compared with distances in the crystal structure (Figure 5.7). Compared with TEDOR data alone, TREDOR determines the $\chi 1$ and $\psi$ angle more accurately as indicated by comparison of the corresponding distances with the crystal structure (correlation coefficient of 0.82 for TREDOR compared with 0.30 for TEDOR using 3 data points). For the comparison, only isolated peaks were considered. Where peak overlap occurs, the TREDOR distance tends to be too large, since the overlap mainly increases the intensity of the REDOR signal. Avoiding this problem would require a more sophisticated peak deconvolution, or extension to higher dimensional spectra. This is also seen from the fit curves: most cases where fit curves deviate from the experimental data significantly are due to spectral overlap (supporting in-
formation Figure S 1 ). However, TREDOR still performed better in predicting the precise distance when overlapped peaks in the 2D (H)NH spectra (Figure 5.6B) are included for the analysis (correlation coefficient of 0.57 for TREDOR compared with 0.21 for TEDOR). All distances extracted from the pseudo-4D N-C TREDOR and the pseudo-4D H-CO TREDOR were subsequently used as restraints for a CYANA [84] structure calculation (see Material and Methods). The pseudo-4D H-CO TREDOR spectra provide orthogonal contacts to define the beta-fold of SH3 better and are particularly suitable for determination of inter-strand contacts in anti-parallel beta sheet structures. As input, we used $5(\mathrm{~N}-\mathrm{Cx})+12(\mathrm{H}-\mathrm{CO})$ medium (contacts 2 to 4 residues apart) and $18(\mathrm{~N}-\mathrm{Cx})$


Figure 5.7: Comparison of NMR derived distances that define $\chi 1$ and $\psi$ torsion angles for residues with a single conformer in the crystal structure. Distances are compared with those of the crystal structure 2 NUZ either fitting with pseudo-4D TREDOR data (yellow and grey) or only the N-C TEDOR component (black). Long range contacts or ambiguous torsion angle restraints are not included in the analysis to exclude potential assignment errors. Contacts with overlapped nitrogen signals are shown in grey and were not included in the determination of $R^{2}$. Pseudo-4D TREDOR predicts distances ( $R^{2} 0.82$ ) more accurately than TEDOR ( $R^{2} 0.30$ ) with data from 3 mixing times. Yellow error bars are indicated at $\pm 10 \%$ to indicate the expected error from ignoring relative orientations.[101]
$+16(\mathrm{H}-\mathrm{CO})$ long range restraints (contacts greater than 4 residues apart) from the $\mathrm{N}-\mathrm{Cx}$ and $\mathrm{H}-$ CO spectra (details in the supporting information). In addition we input $83(\mathrm{~N}-\mathrm{Cx})+26(\mathrm{H}-\mathrm{CO})$ intra-residue or sequential restraints that help define torsion angles. These include the $\psi$ angle that
is already defined by the chemical shifts for most residues, but also the $\chi 1$ angle that is not. The 10 percent distance error estimates used here results in large errors in angles, and further improvement would be needed for true angle determination. Nevertheless, the information excludes part of the Ramachandran space, which is helpful particularly for glycine residues where TALOS does not always provide confident predictions. Considering that the short mixing time TREDOR was used primarily for assignments, four days of experiments are enough to determine the distances used in the structure calculation. Additionally, we enforced backbone torsion angles predicted by TALOS-N.[193] The resulting structured ensemble (20 lowest energy structures, residues 11-58) is shown in Figure 5.8, alongside an overlay of the average structure with the reference crystal structure (PDB-code 2NUZ). Distance information from the TREDOR method faithfully reproduced the overall fold of the SH3 domain with an backbone ensemble RMSD of $1.8 \AA$ in the structured part (residues 11 to 58). This covers nearly the range of assigned resicues (7-62), which coincides with the range of residues determined by x-ray diffraction. The TREDOR calculated structure differs from the crystal structure by $2.1 \AA$ (again comparing residues $11-58$ ) mainly on the ends of the sequence due to lack of contacts, and the very dynamic loop region. Additionally, we measured N-CA, N-CO and H-CA distances with TREDOR. However, we found very few structurally interesting long-range distances, which is likely due to the presence very strong 1-bond dipole couplings for the N-CA and N-CO cases, and to somewhat longer distances for the H-CA case as compared with H-CO distances. Mostly we observed intra-residue or sequential contacts. We therefore used only the $\mathrm{N}-\mathrm{Cx}$ and $\mathrm{H}-\mathrm{CO}$ data during structure calculation. Figure 5.8 C shows the per-residue RMSD as compared to the crystal structure. In the loop regions, TREDOR side-chain to side-chain contacts (see supporting information Table S2, last 7 contacts, for details) improve the RMSD and thus aid in accurately determining structure. Since the N-Cx TREDOR data contains a multitude of backbone to side-chain contacts, it is surprisingly valuable in defining the structure of the RT-loop, which is particularly challenging using backbone data alone.[121, 122] This is obvious, as in the loop region, the all atom RMSD is improved by 2 to $4 \AA$ (Figure 5.8C)


Figure 5.8: Structure of SH3 obtained from TREDOR distances and TALOS-N backbone dihedral angle-restraints. (A) shows the 20 lowest energy structures of 100 calculated structures from a CYANA calculation. The structurally defined region from residues $11-58$ is shown. The backbone ensemble RMSD of 20 structures is $1.8 \AA$ for these residues. (B) compares the lowest-energy TREDOR structure with the reference crystal structure (PDB-code 2NUZ, orange), revealing the correct overall fold of SH3. The RMSD of the TREDOR calculated structure vs the crystal structure A (upper panel) is $2.1 \AA$. (C) TREDOR derived restraints faithfully reproduced the crystal SH3 structure, as shown by the low residue specific all atom RMSD values across the sequence to both conformations in the crystal structure (conformers A and B). Including side-chain to sidechain contacts (black line), which are a unique feature of TREDOR, increases the accuracy in the loop region (blue shading) compared with the structure calculated without (yellow line). Dashed lines indicate residues with side-chain proton to side-chain carbon contacts.

### 5.5 Conclusion

In conclusion, we demonstrate TREDOR as a fast and robust method to precisely measure sitespecific internuclear distances using MAS NMR. We show that the 2-fold increased information in TREDOR leads to accurate distance determination by stabilizing the dipolar oscillation fitting even for the extreme limit of a single point fit. This allows acquisition at the optimal mixing time where signal is maximized, which together with the simultaneous acquisition inherent to the TREDOR method leads to an order of magnitude improvement. We demonstrate TREDOR in two variants, pseudo-4D N-Cx and $\mathrm{H}-\mathrm{CO}$. The data results in efficient protein structure determination. We expect that adaptations of TREDOR, including extension to other spin $1 / 2$ nuclei, will be useful for a variety of applications in materials science, chemistry and biology. While we demonstrate TREDOR with deuterated protein and fast spinning of 55 kHz , or with fully protonated protein and 100 kHz spinning, the relatively low RF requirement of REDOR will allow extension to even faster spinning, so long as the hardware allows the Rabi frequency of the REDOR pulses to exceed the magic-angle spinning frequency.

## CHAPTER 6

## Conclusion

The transmembrane signaling mechanism of the histidine kinase CitA can be solved piece-wise by a combination of NMR techniques (Figure 6.1). The possibility to do sequence specific assignment offered by the high sensitivity and additional proton dimension of ${ }^{1} \mathrm{H}$-detected MAS NMR made the resonances of TM helices available (Chapter 2). The analysis of chemical shift revealed in secondary structure changes involved in the kinase activation. The monomer unit could be assigned to up to $70 \%$ completeness despite CitA having the largest monomer size of a membrane protein to be assigned in such a way up till today. The P-helix formation at the end of PASp from a coil, which was only shown in one residue, L154, previously [178], could be extended to further residues from L155 to I158 into the TM2 helix. The coil to helix transition is also seen at 180GAVG183 motif, which sits at the interface between the inner membrane and the cytosol according to the solvent transfer experiments. This allows the upward, piston-like motion of TM2 into the periplasm. The conserved 192KK193 linker acts like an anchor between TM2 and PASc and loosens the PASc dynamics with the TM2 pulling by transitioning into a coil conformation. As a result, the PASc domain has higher mobility and necessary for conformational changes.

The cytosolic signaling mechanism of the PAS domain, found in more than 2000 sensor kinases [113] is not known. The N-terminal helix of PASc, which directly follows the TM2 helix, undergoes functionally important exchange in solution as seen by CEST measurement [177]. Following this, M. Salvi postulated that the PASc domain undergoes dramatic changes from an anti-parallel to a parallel dimer arrangement in the PASc N-terminal helix upon CitA activation [177]. From the crystal structure, the N-terminal helix rearrangement is accompanied by the
drastic movement of the $\beta$-sheets of the PASc domain, which can be observed at the PASc domain C-terminal as the large difference in the inter-dimer distance. This model is confirmed in this thesis both by the ${ }^{19} \mathrm{~F}$ CODEX based site-specific distance measurement (Chapter 4) and the validated functionally ${ }^{31} \mathrm{P}$-detected NMR based assay (Chapter C). The N288D anti-parallel dimer mutation in the PASc domain of the PASc-kin construct results in a drop of the ATP hydrolysis rate compared to the WT PASc, as revealed by the ${ }^{31} \mathrm{P}$ activity assay. The inter-dimer distance between residue N308 at the C-terminus of the PASc domain in the PASpc construct decreased to $11 \AA$ A , leading to an observable ${ }^{19} \mathrm{~F}$ CODEX decay.

We were able to paint a holistic picture of CitA activation by citrate binding in the periplasm to the DHp domain in the cytosol through eclectic NMR approaches. However, the signal transduction mechanism from the cytosolic PAS domain to the DHp domain cannot be studied with the current constructs used in this thesis. The common themes involved in the signal transduction to DHp domains is the symmetry-asymmetry transitions (where the DHp dimer transition from a symmetric dimer to an asymmetric dimer) and stabilization-destabilization of the $\alpha$-helical linkers at the DHp domain N-terminus [88, 159]. The faster dynamics and the parallel dimer arrangement observed by the experiments presented here can contribute to the destabilization of the $\alpha$-helical linkers and the symmetry-assymetry transition, respectively. But, how exactly theses changes upon citrate binding in the PASc domain would cause the DHp domain activation requires further studies using the full length CitA [81]. For more detailed structural insights into the PASpc construct, side chain resonance assignment will also be a must. To achieve this, either experimental conditions compatible with non-deuterated sample or contact measurements using carbon or nitrogen nuclei are needed. In addition, enough contacts should be available to resolve the ambiguity between inter- versus intra-monomer contacts. For this, more time-saving contacts determination methods applicable to membrane proteins like TREDOR (Chapter 5) will be preferred. With the availability of the high magnetic field up to 1.2 GHz , ultra-fast MAS up to 100 kHz and better pulse sequences, solving the full structure of the CitA PASpc construct might indeed be on the horizon.


Figure 6.1: Mechanism of CitA activation by citrate binding. The binding of citrate in the PASp citrate binding site causes a change in the hydrogen bond network and a contraction of the $\beta$ scaffold. This stabilizes the PASp and forms a P-helix at the PASp C-terminus. Such change in the secondary structure propagates through the membrane, shifting the TM2 helix upwards in a pistonlike motion into the periplasm. The 180GAVG183 motif at the end of TM2 undergoes the same random coil to $\alpha$-helix transition as the P-helix after citrate binding. Effectively, the 192KK193 motif upstream of PASc gets loosened due to the upward pulling of TM2 and increases the PASc dynamics downstream. These sequential structural and dynamics changes allows the PASc dimer to switch from an anti-parallel to parallel arrangement. The parallel arrangement in the PASc has a smaller inter-dimer distance compared with the anti-parallel arrangement, which potentially causes DHp domain symmetry-asymmetry transition and consequently, CitA cross-phosphorylation.

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APPENDIX A

## Appendix: Chapter 1



Figure A.1: In vivo testing of the proposed G. thermodenitrificans CitA PASc functional mutants performed in Prof. Unden lab. In dark blue is shown the value in absence of the substrate; in light blue, green and yellow are shown the activities in presence of succinate, fumarate and citrate, respectively. Figure prepared by M. Salvi [177].

## APPENDIX B

## Appendix: Chapter 2

Table B.1: Chemical shifts from ${ }^{1} \mathrm{H}$ detected sequence specific assignment of the citrate bound state of CitA PASpc

| Residue | H | N | C | Ca | Cb |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1Met | None | None | None | None | None |
| 2Lys | None | None | None | None | None |
| 3Leu | None | None | None | None | None |
| 4GIn | None | None | None | None | None |
| 5 Thr | None | None | None | None | None |
| 6Arg | 9.36 | 120.09 | 173.9 | 54.1 | 27.89 |
| 7Leu | 7.92 | 120.01 | 177.77 | 58.13 | 40.94 |
| 8Met | 8.43 | 119.57 | 177.98 | 58 | 29.76 |
| 9 Val | 7.72 | 118.45 | 176.88 | 67.2 | 29.03 |
| 10Ile | 7.73 | 118.42 | None | 60.01 | 40.44 |
| 11 lle | None | None | None | None | None |
| 12Ala | None | None | None | None | None |
| 13Ser | None | None | None | None | None |
| 14Leu | 7.71 | 120.52 | 178.6 | 57.9 | 40.45 |
| 15Leu | 7.92 | 120.17 | 177.11 | 56.29 | 41.24 |
| 16Leu | 8.95 | 118.51 | 178.24 | 58.76 | 40.15 |
| 17Phe | 8.06 | 117.18 | 178.44 | 58.83 | 38.19 |
| 18 Val | None | None | None | None | None |
| 191le | None | None | None | None | None |
| 2011 e | None | None | None | None | None |
| 21Phe | None | None | None | None | None |
| 22Leu | None | None | 178.6 | 58.33 | 39.86 |
| 23Thr | 8.1 | 118.04 | 177.68 | 66.47 | 67.99 |
| 24Phe | 8.52 | 118.01 | 177.9 | 57.64 | 38.19 |
| 25Leu | None | None | None | None | None |
| 26Phe | None | None | None | None | None |
| 27GIn | None | None | None | None | None |
| 28 His | None | None | None | None | None |
| 29Met | None | None | None | 58.32 | 31.77 |
| 30Phe | 8.29 | 116.33 | 175.92 | 59.69 | 38.76 |
| 31Ala | 8.76 | 121.72 | 177.75 | 55.58 | 17.4 |
| 32Ala | 8.09 | 120.7 | 178.89 | 54.83 | 17.49 |
| 33Thr | None | None | 179.25 | 66.68 | 68.49 |
| 34Leu | 8.76 | 123.36 | 178.94 | 57.34 | 39.68 |
| 35Lys | 8.1 | 117.81 | 178.51 | 58.92 | 31.38 |
| 36Glu | None | None | None | None | None |
| 37GIn | None | None | None | None | None |
| 38lle | None | None | None | None | None |
| 39Gly | None | None | None | None | None |
| 40Met | None | None | None | None | None |
| 41Arg | None | None | None | None | None |
| 42Ala | 8.78 | 121.34 | 179.63 | 55.29 | 17.4 |
| 43Leu | 8.74 | 117.48 | 178.28 | 57.33 | 40.07 |
| 44Asn | 8.89 | 116.89 | 178.77 | 56.25 | 38.24 |
| 45 Val | 8.15 | 121.01 | 177.3 | 67.41 | 30.75 |
| 46Ala | 8.84 | 123.99 | 179.76 | 55.6 | 17.33 |
| 47Glu | 9.13 | 114.35 | 179.94 | 58.23 | 29.28 |


| Residue | H | N | C | Ca | Cb |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 48Thr | 8 | 117.58 | 177.66 | 66.88 | 68.17 |
| 49 Val | 8.59 | 121.74 | 178.7 | 67.04 | 31.1 |
| 50Ala | 8.77 | 118.57 | 178.21 | 54.59 | 17.96 |
| 51Ser | 7.4 | 111.66 | 174.35 | 59.26 | 64.25 |
| 52Thr | 7.84 | 114.99 | 176 | 62.6 | 70.2 |
| 53Ser | None | None | None | None | None |
| 54Leu | None | None | 177.5 | 57.96 | 41.3 |
| 55 Val | 6.91 | 114.61 | 175.88 | 65.07 | 30.26 |
| 56Arg | 6.84 | 115.07 | 180.15 | 59.19 | 29.11 |
| 57Glu | 8.54 | 118.2 | 179.77 | 58.67 | 28.57 |
| 58Ala | 8.41 | 121.48 | 179.41 | 53.81 | 17.26 |
| 59Phe | 7.55 | 114.31 | 177.08 | 61.21 | 38.22 |
| 60Arg | 7.8 | 116.85 | 176.82 | 55.93 | 29.47 |
| 61Asp | 7.44 | 120.92 | 176.11 | 53.74 | 40.5 |
| 62Ser | 8.69 | 116.04 | 175.53 | 61.01 | 61.95 |
| 63Asn | 8.12 | 114.06 | 174.17 | 49.56 | 37.99 |
| 64Pro | None | None | 176.1 | 64.4 | 32.68 |
| 65Ser | 7.55 | 107.32 | 175.97 | 61.89 | 63.67 |
| 66 Val | 7.25 | 118.99 | 178.58 | 66.29 | 29.86 |
| 67Arg | 8.33 | 113.98 | 179.3 | 57.75 | 31.37 |
| 68Leu | 8 | 116.48 | 177.48 | 57.61 | 42.29 |
| 69GIn | 8.7 | 119.21 | 175.02 | 60.07 | 23.98 |
| 70Pro | None | None | 180.11 | 65.29 | 29.72 |
| 71Phe | 6.66 | 117 | 176.1 | 59.94 | 38.97 |
| 72Ala | 8.86 | 122.12 | 179.68 | 55.33 | 17.42 |
| 73Glu | 8.13 | 115.66 | 178.6 | 57.48 | 29.5 |
| 74Arg | 7.63 | 120.98 | 178.51 | 58.64 | 28.61 |
| 751le | 7.84 | 117.32 | 179.68 | 61.79 | 33.8 |
| 76Arg | 8.96 | 124.99 | 178.03 | 60.56 | 28.31 |
| 77GIn | 8.05 | 116.52 | 179.05 | 58.47 | 27.83 |
| 78Lys | None | None | None | None | None |
| 79Thr | None | None | 176.14 | 62.86 | 71.07 |
| 80Gly | 7.73 | 108.48 | 174.09 | 45.12 | None |
| 81Ala | 7.13 | 121.62 | 175.7 | 51.11 | 17.37 |
| 82Glu | 8.05 | 120.9 | 176.6 | 57.3 | 28.14 |
| 83Tyr | 6.41 | 104.33 | 172.77 | 54.45 | 38.38 |
| 84 Val | 7.88 | 120.87 | 174.27 | 62.11 | 31.11 |
| 85 Val | 9.79 | 126.78 | 175.96 | 60.58 | 33.4 |
| 86Ile | 7.49 | 124.28 | 175.4 | 59.42 | 39.37 |
| 87Gly | 9.78 | 115.73 | 172.9 | 43.77 | None |
| 88Asn | 7.99 | 116.41 | 176.54 | 50.67 | 38.28 |
| 89Arg | 7.42 | 115.49 | 176.19 | 58.2 | 29.03 |
| 90GIn | 7.35 | 115.41 | 176.08 | 55.49 | 27.85 |
| 91Gly | 8.22 | 107.74 | 172.72 | 45.12 | None |
| 92Ile | 7.5 | 119.84 | 175.83 | 57.89 | 35.23 |
| 93Ala | 7.77 | 125.43 | 177 | 52.13 | 18.11 |
| 94Tyr | 9.81 | 122.4 | 174.82 | 55.31 | 39.75 |
| 95Ala | 7.86 | 119.92 | 175.32 | 51.11 | 21.47 |
| 96 His | 9.06 | 123.61 | 172.61 | 55.68 | 33.68 |


| Residue | H | N | C | Ca | Cb |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 97Pro | None | None | 178.11 | 64.28 | 30.82 |
| 98Leu | 10.96 | 123.13 | 177.36 | 52.94 | 39.94 |
| 99Thr | 8.47 | 120.32 | 177.86 | 65.71 | 67.76 |
| 100Glu | 9.36 | 119.64 | 176.6 | 57.8 | 27.89 |
| 101Arg | 7.97 | 119.87 | 178.56 | 52.57 | 28.32 |
| 102lle | 7.26 | 121.92 | 177.44 | 63.67 | 36.19 |
| 103Gly | 9.59 | 115.29 | 173.66 | 44.66 | None |
| 104Lys | 7.8 | 118.43 | 176.71 | 53.42 | 34.06 |
| 105Ser | 8.32 | 116.96 | 173.66 | 59.7 | 63.44 |
| 106Met | 8.75 | 122.42 | 176.49 | 56.29 | 34.91 |
| 107Ile | 10.24 | 129.59 | 175.34 | 59.45 | 39.08 |
| 108Gly | 8.27 | 112.21 | 176.19 | 44.67 | None |
| 109Gly | 8.95 | 108.53 | 174.98 | 46.28 | None |
| 110Asp | 8.13 | 116.43 | 176.62 | 52.02 | 37.97 |
| 111Asn | 8.38 | 115.1 | 177.77 | 53.95 | 38.46 |
| 112Lys | 7.9 | 120.01 | 179.01 | 60.81 | 31.65 |
| 113Glu | 9 | 115.4 | 178.97 | 58.23 | 28.47 |
| 114 Val | 7 | 119.77 | 180.54 | 62.96 | 30.35 |
| 115Leu | 7.59 | 118.16 | 178.09 | 56.46 | 40.19 |
| 116Lys | 7.04 | 115.96 | 176.91 | 56.03 | 31.79 |
| 117Gly | 8.35 | 107.26 | 173.7 | 44.99 | None |
| 118Lys | 7.79 | 122.41 | 174.16 | 54.99 | 32.88 |
| 119Ser | 8.09 | 116.45 | 175.14 | 57.18 | 63.55 |
| 120Ile | 8.97 | 116.82 | 173.59 | 59.11 | 42.19 |
| 121Ile | 8.11 | 120.95 | 176.27 | 60.8 | 38.51 |
| 122Ser | 9.54 | 122.26 | 173.76 | 55.06 | 64.81 |
| 123Glu | 8.47 | 128.46 | 175.29 | 54.6 | 30.22 |
| 124Ala | 8.73 | 126.35 | 174.8 | 50.58 | 21.51 |
| 125 Val | 8.56 | 119.8 | 175.53 | 61.92 | 29.94 |
| 126Gly | 6.75 | 112.11 | 176.93 | 44.29 | None |
| 127Ser | 7.22 | 120.8 | 176.75 | 62.72 | 61.94 |
| 128Leu | 11.08 | 123.33 | 176.8 | 54.75 | 40.71 |
| 129Gly | 7.2 | 104.79 | 172.21 | 43.64 | None |
| 130Pro | None | None | 177.26 | 63.36 | 31.3 |
| 131Ala | 9.49 | 129.45 | 175.12 | 52.02 | 24.05 |
| 132Ile | 8.54 | 117.7 | 174.07 | 59.48 | 39.96 |
| 133Arg | 9.4 | 122.87 | 175.28 | 53.99 | 33.01 |
| 134Gly | 9.15 | 110.62 | 171.98 | 43.73 | None |
| 135Lys | 9.17 | 122.8 | 173.66 | 54.07 | 33.22 |
| 136Ala | 8.91 | 122.74 | 173.91 | 47.51 | 21.16 |
| 137Pro | None | None | 174.64 | 60.64 | 30.5 |
| 138lle | 7.52 | 118.12 | 175.38 | 59.52 | 38.78 |
| 139Phe | 8.75 | 126.04 | 177.13 | 56.42 | 41.53 |
| 140Asp | 8.93 | 119.03 | 178.3 | 51.65 | 40.59 |
| 141Glu | 9.58 | 117.95 | 176.78 | 58.59 | 27.97 |
| 142Asn | 8.21 | 116.08 | 175.86 | 52.49 | 39.02 |
| 143Gly | 8.04 | 107.8 | 174.35 | 45.48 | None |
| 144Ser | 8.63 | 118.73 | 174.08 | 57.61 | 62.98 |
| 145 Val | 8.85 | 124.59 | 177.4 | 63.16 | 30.6 |


| Residue | H | N | C | Ca | Cb |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 146Ile | 8.91 | 120.67 | 175.28 | 60.49 | 38.88 |
| 147Gly | 7.25 | 106.63 | 170.13 | 45.64 | None |
| 148lle | 8.63 | 118.89 | 174.14 | 60.13 | 44.55 |
| 149 Val | 9.14 | 124.78 | 174.31 | 60.67 | 32.75 |
| 150Ser | 9.55 | 122.29 | 173.9 | 54.98 | 65.04 |
| 151 Val | 9.13 | 128.8 | 174.96 | 60.15 | 31.9 |
| 152Gly | 7.04 | 112.16 | 171.18 | 43.34 | None |
| 153Phe | 8.52 | 116.72 | 175.17 | 56.73 | 42.05 |
| 154Leu | 9.58 | 120.47 | 179.35 | 54.98 | 39.41 |
| 155Leu | 8.82 | 123.82 | 179.74 | 57.34 | 39.89 |
| 156Glu | 8.97 | 117.77 | 178.26 | 59.06 | 28.91 |
| 157Asp | 8.59 | 118.28 | 178.27 | 57 | 40.77 |
| 158lle | 8.6 | 121.66 | 177.72 | 65.97 | 37.7 |
| 159GIn | None | None | None | None | None |
| 160Arg | None | None | 177.45 | 60.36 | 28.92 |
| 161 Thr | 8.4 | 120.11 | 177.77 | 65.52 | 67.75 |
| 162 Val | 7.65 | 118.22 | 177.36 | 66.92 | 30.89 |
| 163Trp | None | None | None | None | None |
| 164Ser | None | None | None | None | None |
| 165Tyr | None | None | None | None | None |
| 166Ser | None | None | None | None | None |
| 167Met | None | None | None | None | None |
| 168Lys | None | None | None | None | None |
| 1691le | None | None | None | None | None |
| 170Phe | None | None | None | None | None |
| 171Phe | None | None | None | None | None |
| 172Phe | None | 122.24 | 176.11 | 58.93 | 38.84 |
| 173Ser | 8.85 | 121.35 | 178.72 | 59.09 | 61.72 |
| 174 Val | 8.39 | 120.86 | 177.52 | 65.82 | 28.35 |
| 175Leu | 8.66 | 120.44 | 177.54 | 60.18 | 41.06 |
| 176Ala | 8.43 | 119.78 | 178.31 | 55.24 | 17.21 |
| 177Leu | 8.5 | 117.59 | 177.93 | 57.7 | 40.3 |
| 178Leu | 8.33 | 119.16 | 178.47 | 57.8 | 40.13 |
| 179Phe | 8.28 | 116 | 176.72 | 57.72 | 38.22 |
| 180Gly | 8.36 | 107.77 | 174.7 | 45.21 | None |
| 181Ala | 8.67 | 118.85 | 175.03 | 54.81 | 18.02 |
| 182 Val | 9.58 | 122.23 | 173.93 | 64.64 | 32.86 |
| 183Gly | 7.63 | 107.63 | 172.76 | 45.31 | None |
| 184Ala | 8.19 | 121.62 | 177.5 | 54.83 | 17.37 |
| 185 Val | 8.01 | 121.1 | 177.37 | 67.44 | 30.86 |
| 186Ala | 8.83 | 124.02 | 177.95 | 55.38 | 17.28 |
| 187Ile | 7.86 | 116.29 | 177.66 | 66.28 | 38.54 |
| 188Ala | 8.77 | 121.79 | 179.6 | 55.39 | 17.55 |
| 189Lys | 8.34 | 114.84 | 179.01 | 57.53 | 29.92 |
| 190Ala | 7.67 | 121.33 | 177.55 | 55.04 | 17.68 |
| 191 Val | 9.03 | 115.37 | 177.76 | 58.28 | 28.25 |
| 192Lys | 8.02 | 115.87 | 176.04 | 58.23 | 30.73 |
| 193Lys | 7.77 | 118.84 | 178.6 | 54.77 | 34.16 |
| 194Ser | None | None | None | None | None |


| Residue | H | N | C | Ca | Cb |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 195lle | None | None | None | None | None |
| 196His | None | None | None | None | None |
| 197Gly | None | None | None | None | None |
| 198Leu | None | None | None | None | None |
| 199Glu | None | None | None | None | None |
| 200Pro | None | None | 178.45 | 66.72 | 29.05 |
| 201Glu | 8.5 | 117.56 | 178.11 | 57.49 | 28.47 |
| 202Glu | 7.98 | 121.27 | 177.42 | 57.39 | 29.26 |
| 20311 e | 7.65 | 121.01 | 177.72 | 64.63 | 41.29 |
| 204Gly | 8.37 | 107.02 | 174.86 | 47.38 | None |
| 205Leu | 8.36 | 119.26 | 177.72 | 57.81 | 40.17 |
| 206Leu | None | None | None | None | None |
| 207 Tyr | None | None | 177.66 | 58.38 | 38.79 |
| 208GIn | 7.89 | 117.89 | 179.01 | 57.47 | 29.59 |
| 209Glu | 7.75 | 120.82 | 178.55 | 57.4 | 28.56 |
| 210Lys | 7.94 | 117.23 | 177.75 | 58.46 | 31.34 |
| 211GIn | 7.84 | 116.63 | 178.96 | 58.65 | 28.08 |
| 212Ala | None | None | None | None | None |
| 2131le | None | None | 179.19 | None | None |
| 214Leu | 8.55 | 122.95 | None | 57.64 | 40.31 |
| 215Glu | 7.74 | 114.79 | 178.34 | 57.48 | 28.46 |
| 216Ala | 8.08 | 121.32 | 179.49 | 55.12 | 17.56 |
| 217lle | 8.12 | 118.39 | 178.65 | 66.54 | 36.33 |
| 218Arg | None | None | None | None | None |
| 219Glu | None | None | None | None | None |
| 220Gly | None | None | None | None | None |
| 22111 e | None | None | None | None | None |
| 222Val | None | None | None | None | None |
| 223Ala | None | None | None | None | None |
| 224Ile | None | None | None | None | None |
| 225Asn | None | None | None | None | None |
| 226GIn | None | None | None | None | None |
| 227Glu | None | None | None | None | None |
| 228Gly | None | None | None | None | None |
| 229Thr | 7.53 | 114.85 | 174.53 | 61.07 | 68.18 |
| 23011 e | 8.33 | 124.24 | 177.27 | 62.71 | 36.12 |
| 232Met | None | None | None | None | None |
| 233Val | None | None | None | None | None |
| 234Asn | None | None | None | None | None |
| 235GIn | None | None | None | None | None |
| 236Thr | None | None | 178.53 | 65.85 | 68.4 |
| 237Ala | 8.3 | 120.01 | 179.67 | 55.18 | 17.16 |
| 238Leu | 8.61 | 117.5 | 179.51 | 57.47 | 40.06 |
| 239Lys | None | None | None | None | None |
| 240Leu | None | None | None | None | None |
| 241Leu | None | None | None | None | None |
| 242Gly | None | None | None | None | None |
| 243Tyr | None | None | None | None | None |
| 244Asp | None | None | None | None | None |


| Residue | H | N | C | Ca | Cb |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 245Asn | None | None | None | None | None |
| 246Glu | None | None | None | None | None |
| 247Arg | None | None | None | None | None |
| 248Asn | None | None | None | None | None |
| 249 Val | None | None | None | None | None |
| 250Leu | None | None | 178.08 | None | 40.4 |
| 251Gly | 8.95 | 109.6 | 174.17 | 44.86 | None |
| 252Thr | None | None | None | None | None |
| 253Pro | None | None | None | None | None |
| 254Ile | None | None | None | None | None |
| 255Leu | None | None | None | None | None |
| 256GIn | None | None | None | None | None |
| 257Leu | None | None | None | None | None |
| 258Ile | None | None | None | None | None |
| 259Pro | None | None | None | None | None |
| 260His | None | None | None | None | None |
| 261Ser | None | None | None | None | None |
| 262Arg | None | None | None | None | None |
| 263Leu | None | None | None | None | None |
| 264Pro | None | None | None | None | None |
| 265Glu | None | None | None | None | None |
| 266 Val | None | None | None | None | None |
| 267 Ile | None | None | None | None | None |
| 268Arg | None | None | None | None | None |
| 269Thr | None | None | None | None | None |
| 270Gly | None | None | 172.83 | 47.23 | None |
| 271GIn | 8.03 | 119.23 | 174.35 | 53.62 | 29.3 |
| 272Ala | 8.38 | 125.14 | 176.44 | 51.72 | 20 |
| 273Glu | 8.56 | 118.25 | 177.78 | 57.5 | 28.78 |
| 274Tyr | 7.64 | 121.06 | 177.48 | 57.74 | 41.29 |
| 275Asp | 8.95 | 119.06 | 175.43 | 51.66 | 40.67 |
| 276Asp | None | None | None | None | None |
| 277 Glu | None | None | None | None | None |
| 278Met | 9.13 | 124.81 | 174.97 | 54.49 | 30.62 |
| 279 Val | None | None | None | None | None |
| 280Leu | None | None | None | None | None |
| 281Gly | None | None | None | None | None |
| 282Gly | None | 104.25 | 173.66 | 44.73 | None |
| 283Glu | 7.79 | 121.01 | 174.31 | 54.81 | 30.9 |
| 284Thr | 8.66 | 118.52 | 175.93 | 62.6 | 70.69 |
| 285 Val | 9.14 | 121.46 | 177.87 | 58.87 | 35.63 |
| 286Ile | None | None | None | None | None |
| 287Ala | None | None | None | None | None |
| 288Asn | None | None | None | None | None |
| 289Arg | None | None | None | None | None |
| 290lle | None | None | None | None | None |
| 291Pro | None | None | None | None | None |
| 292Ile | None | None | None | None | None |
| 293Lys | 8.57 | 126.26 | 176.02 | 54.06 | 35.29 |


| Residue | H | N | C | Ca | Cb |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 294Asn | 8.46 | 117.91 | None | 50.23 | None |
| 295Lys | None | None | 177.28 | 58.32 | 38.24 |
| 296Gln | 7.43 | 115.93 | 176.25 | 55.63 | 28.94 |
| 297Gly | 8.2 | 107.55 | 173.8 | 45.23 | None |
| 298Arg | 7.74 | 121.97 | 175.95 | 54.84 | 32.79 |
| 299Val | None | None | None | None | None |
| 300Ile | None | None | None | None | None |
| 301Gly | None | None | 171.34 | 45.25 | None |
| 302Ala | 8.51 | 120.02 | 174.2 | 52.15 | 21.87 |
| 303Val | None | None | None | None | None |
| 304Ser | None | None | None | None | None |
| 305Thr | None | None | None | None | None |
| 306Phe | None | None | None | None | None |
| 307Arg | None | None | None | None | None |
| 308Asn | None | None | None | None | None |
| 309Lys | None | None | None | None | None |


| Residue | H | N | C | Ca | Cb |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 47Glu | 9.19 | 114.54 | 179.11 | 58.36 | 28.83 |
| 48Thr | None | None | None | 66.85 | 68.19 |
| 49 Val | 8.66 | 122.01 | 178.12 | 67.02 | 30.77 |
| 50Ala | 8.58 | 118.83 | 178.06 | 54.67 | 18.44 |
| 51Ser | 7.44 | 109.79 | 178.31 | 58.15 | 63.75 |
| 52Thr | None | None | None | None | None |
| 53Ser | None | None | None | 62.51 | None |
| 54Leu | 7.88 | 120.17 | 178.05 | 58.1 | 40.78 |
| 55 Val | 6.97 | 116.5 | 176.44 | 65.54 | 30.24 |
| 56Arg | 7.03 | 116 | 179.93 | 59.46 | 29.13 |
| 57 Glu | 8.28 | 118.07 | 179.11 | 58.59 | 30.77 |
| 58Ala | 8.51 | 122.13 | 179.62 | 53.97 | 17.22 |
| 59Phe | 7.64 | 114.71 | 177.15 | 61.23 | 38.42 |
| 60Arg | 7.82 | 116.83 | 176.81 | 55.87 | 29.49 |
| 61Asp | 7.46 | 121.1 | 176.09 | 53.87 | 40.51 |
| 62Ser | 8.73 | 116.05 | 175.57 | 61.1 | 61.93 |
| 63Asn | 8.19 | 114.12 | 174.18 | 49.58 | 37.93 |
| 64Pro | None | None | 176.1 | 64.27 | None |
| 65Ser | 7.6 | 107.49 | 175.97 | 61.8 | 63.56 |
| 66 Val | 7.26 | 119.68 | 178.56 | 66.26 | 29.93 |
| 67Arg | 8.27 | 113.92 | 179.55 | 57.65 | 31.52 |
| 68Leu | 8.07 | 116.56 | 177.42 | 57.36 | 41.99 |
| 69GIn | 8.73 | 119.25 | 174.19 | 54.78 | 30.94 |
| 70Pro | None | 118.74 | 179.88 | 65.06 | 29.7 |
| 71Phe | 6.7 | 117.81 | 176.17 | 60.31 | 39.01 |
| 72Ala | 8.87 | 121.71 | 179.45 | 55.36 | 17.45 |
| 73Glu | 8.13 | 115.97 | 177.65 | 58.03 | 27.96 |
| 74Arg | 8.01 | 120.11 | 177.99 | 58.03 | 29.24 |
| 751le | 8.07 | 118.8 | 179.66 | 62.42 | 40.82 |
| 76Arg | 8.85 | 124.61 | 178.1 | 60.42 | 30.37 |
| 77GIn | 8.04 | 116.73 | 178.9 | 58.43 | 27.81 |
| 78Lys | 8.14 | 117.28 | 178.38 | 57.39 | 32.23 |
| 79Thr | 7.89 | 104.15 | 176.98 | 62.07 | 70.07 |
| 80Gly | 8.56 | 109.72 | 174.13 | 45.59 | None |
| 81Ala | 7.32 | 122.12 | 176.16 | 51.46 | 17.7 |
| 82Glu | 8.08 | 120.81 | 176.2 | 57.51 | 29.21 |
| 83Tyr | 6.46 | 104.25 | 172.88 | 54.39 | 38.61 |
| 84 Val | 7.87 | 120.25 | 173.92 | 62.04 | 32.49 |
| 85 Val | 9.5 | 126.7 | 175.41 | 59.88 | 33.9 |
| 86Ile | 8.08 | 123.98 | 175.44 | 59.77 | 40.22 |
| 87Gly | 9.79 | 115.65 | 172.69 | 43.89 | None |
| 88Asn | 7.99 | 116.52 | 176.66 | 50.8 | 38.4 |
| 89Arg | 7.48 | 115.73 | 176.08 | 58.19 | 28.87 |
| 90GIn | 7.48 | 115.76 | 176.06 | 55.97 | 28.17 |
| 91Gly | 8.2 | 107.17 | 172.76 | 45.16 | None |
| 92Ile | 7.5 | 119.79 | 175.96 | 57.88 | 35.3 |
| 93Ala | 7.83 | 125.53 | 177.04 | 52.3 | 18.12 |
| 94Tyr | 9.82 | 122.45 | 174.5 | 55.18 | 39.78 |
| 95Ala | 7.92 | 119.54 | 175.46 | 51.03 | 21.53 |

Table B.2: Chemical shifts from ${ }^{1} \mathrm{H}$ detected sequence specific assignment of the citrate free state of CitA PASpc

| Residue | H | N | C | Ca | Cb |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1Met | None | None | None | None | None |
| 2 Lys | None | None | None | None | None |
| 3Leu | None | None | None | None | None |
| 4GIn | None | None | None | None | None |
| 5 Thr | None | None | 174.49 | None | None |
| 6Arg | 9.33 | 119.99 | 176.4 | 54.25 | 30.7 |
| 7Leu | 8.78 | 120.72 | 177.76 | 58.95 | 40.89 |
| 8Met | 8.36 | 119.98 | 177.83 | 58.14 | 30.85 |
| 9 Val | 7.81 | 118.1 | 177.63 | 66.51 | 30.73 |
| 10Ile | 8.85 | 121.7 | 177.52 | 66.97 | 38.88 |
| 11Ile | 8.83 | 122.5 | 178.09 | 66.95 | 36.28 |
| 12Ala | 8.65 | 122.23 | 178.09 | 55.32 | 17.38 |
| 13Ser | 8.58 | 118.39 | 178.25 | 59.76 | 62.85 |
| 14Leu | 8.45 | 119.21 | 178.02 | 57.78 | 40.87 |
| 15Leu | 7.98 | 120.37 | 178.99 | 55.27 | 40.75 |
| 16Leu | 8.25 | 118.28 | 178.44 | 58.46 | 38.33 |
| 17Phe | 8.29 | 118.36 | None | None | None |
| 18 Val | None | None | None | None | None |
| 191le | None | None | None | None | None |
| 20Ile | None | None | 175.12 | 63.04 | 41.42 |
| 21Phe | 8.78 | 120.32 | 179.17 | 58.72 | 38.37 |
| 22Leu | 8.01 | 117.1 | 179.03 | 57.7 | 40.29 |
| 23Thr | 8.05 | 118.3 | 179.11 | 66.88 | 68.11 |
| 24Phe | 8.57 | 122.24 | 177.87 | 60.14 | 38.54 |
| 25Leu | 7.98 | 117.65 | 178.48 | 57.23 | 38.39 |
| 26Phe | 8.78 | 121.76 | 178.28 | 59.81 | 37.57 |
| 27GIn | 8.47 | 118.99 | 178.98 | 58.95 | 28.39 |
| 28 His | 8.25 | 118.19 | 178.65 | 59.67 | 30.23 |
| 29Met | 7.53 | 117.92 | 178.92 | 58.98 | 30.27 |
| 30Phe | 7.89 | 118.47 | 177.88 | 60.44 | 40.15 |
| 31Ala | 8.58 | 120.5 | 178.07 | 54.91 | 16.58 |
| 32Ala | 8.54 | 120.06 | 178.51 | 55.39 | 17.14 |
| 33Thr | 7.94 | 115.01 | 178.89 | 57.5 | 68.36 |
| 34Leu | 7.75 | 120.78 | 178.45 | 57.78 | 40.67 |
| 35Lys | None | None | None | None | None |
| 36Glu | None | None | None | None | None |
| 37GIn | None | None | None | None | None |
| 38lle | None | None | None | None | None |
| 39Gly | None | None | None | None | None |
| 40Met | None | None | None | None | None |
| 41Arg | None | None | None | None | None |
| 42Ala | None | None | None | None | None |
| 43Leu | None | None | None | None | None |
| 44Asn | None | None | None | None | None |
| 45 Val | None | None | None | None | None |
| 46Ala | None | None | 179.29 | 55.92 | None |


| Residue | H | N | C | Ca | Cb |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 96His | 9.24 | 124.54 | 173.7 | 54.25 | 33.08 |
| 97Pro | None | None | None | None | None |
| 98Leu | 10.98 | 123.02 | 177.36 | 52.94 | None |
| 99Thr | None | None | None | None | None |
| 100Glu | None | None | None | 58.5 | 27.96 |
| 101Arg | 8.33 | 116.44 | 179.03 | 55.61 | 28.64 |
| 102lle | 7.31 | 121.6 | 177.67 | 63.71 | 36.14 |
| 103Gly | 9.56 | 115.5 | 172.46 | 44.75 | None |
| 104Lys | 7.88 | 118.61 | 174.27 | 53.7 | 33.72 |
| 105Ser | None | None | None | None | None |
| 106Met | None | None | None | None | None |
| 107Ile | None | None | None | None | None |
| 108Gly | 9.63 | None | 173.48 | 44.85 | None |
| 109Gly | 9.03 | 108.75 | 172.98 | 46.34 | None |
| 110Asp | 8 | 118.91 | 176.91 | 53.73 | None |
| 111Asn | None | None | None | None | None |
| 112Lys | None | None | None | None | None |
| 113Glu | None | None | 178.97 | 58.69 | None |
| 114 Val | 7.04 | 119.65 | 177.94 | 63.07 | 30.59 |
| 115Leu | 7.69 | 118.15 | 178.06 | 56.48 | 40.27 |
| 116Lys | 7.1 | 116.3 | 176.93 | 56.42 | 31.84 |
| 117Gly | 8.43 | 106.98 | 173.51 | 45.08 | None |
| 118Lys | 7.73 | 121.93 | 174.26 | 55.14 | 29.31 |
| 119Ser | 8.22 | 116.43 | 178.08 | 57.54 | None |
| 120Ile | None | None | None | None | None |
| 121Ile | None | None | None | None | None |
| 122Ser | None | None | None | None | None |
| 123Glu | None | None | 173.07 | 59.68 | 31.58 |
| 124Ala | 8.81 | 126.28 | 177.19 | 50.53 | 19.42 |
| 125 Val | 8.85 | 119.33 | 178.22 | 60.25 | 31.79 |
| 126Gly | 7.24 | 112.29 | 171.5 | 43.36 | None |
| 127Ser | None | None | None | None | None |
| 128Leu | None | None | None | None | None |
| 129Gly | None | None | None | None | None |
| 130Pro | None | None | None | None | None |
| 131Ala | None | None | None | None | None |
| 132lle | None | None | 175.35 | 60.31 | None |
| 133Arg | 9.14 | 125.86 | 174.72 | 53.88 | 32.54 |
| 134Gly | 9.18 | 109.99 | 171.69 | 43.67 | None |
| 135Lys | 9.07 | 122.9 | 173.85 | 54.17 | 36.43 |
| 136Ala | 9.01 | 122.27 | 173.84 | 47.79 | 21.88 |
| 137Pro | None | None | 174.41 | 60.61 | 30.9 |
| 138Ile | 7.52 | 117.86 | 175.16 | 59.66 | 38.81 |
| 139Phe | 8.88 | 126.13 | 177.14 | 56.5 | 41.55 |
| 140Asp | 8.96 | 119.13 | 178.35 | 51.7 | 40.6 |
| 141Glu | 9.56 | 117.86 | 176.71 | 58.6 | 27.94 |
| 142Asn | 8.23 | 116.07 | 175.83 | 52.61 | 38.98 |
| 143Gly | 8.07 | 107.87 | 174.33 | 45.5 | None |
| 144Ser | 8.64 | 118.67 | 173.95 | 57.71 | 63 |


| Residue | H | N | C | Ca | Cb |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 145 Val | 8.91 | 124.54 | 177.55 | 63.17 | 30.54 |
| 146Ile | 8.95 | 120.57 | 175.47 | 60.59 | 38.84 |
| 147Gly | 7.28 | 106.82 | 169.96 | 45.69 | None |
| 148lle | 8.59 | 118.29 | 174.08 | 60.07 | 44.54 |
| 149 Val | 9.15 | 124.88 | 174.36 | 60.54 | 33.08 |
| 150Ser | 9.41 | 121.27 | 173.68 | 55.18 | 64.54 |
| 151 Val | 9.18 | 126.91 | 174.24 | 60.21 | 33.28 |
| 152Gly | 7.14 | 112.07 | 171.8 | 43.41 | None |
| 153Phe | 8.41 | 117.96 | 178.54 | 55.98 | 40.66 |
| 154Leu | 8.92 | 120.34 | 174.83 | 54.27 | 40.98 |
| 155Leu | 8.91 | 120.64 | 174.87 | 55.22 | 40.97 |
| 156Glu | 8.64 | 120.42 | 176.56 | 54.24 | 30.94 |
| 157Asp | 7.91 | 120.42 | 175.54 | 55.07 | 40.74 |
| 158lle | 8.63 | 119.09 | 175.29 | 60.01 | 37.29 |
| 159GIn | None | None | None | None | None |
| 160Arg | None | None | None | None | None |
| 161 Thr | None | None | None | None | None |
| 162 Val | None | None | None | None | None |
| 163Trp | None | None | None | None | None |
| 164Ser | None | None | None | None | None |
| 165Tyr | None | None | None | None | None |
| 166Ser | None | None | None | None | None |
| 167Met | None | None | None | None | None |
| 168Lys | None | None | None | None | None |
| 1691le | None | None | None | None | None |
| 170Phe | None | None | None | None | None |
| 171Phe | None | None | None | None | None |
| 172Phe | None | None | None | 60.28 | 37.69 |
| 173Ser | 8.75 | 121.59 | 174.43 | 60.06 | None |
| 174 Val | 8.77 | 121.26 | 177.76 | 66.81 | 30.84 |
| 175Leu | 8.69 | 119.73 | 178.21 | 60.09 | 40.99 |
| 176Ala | None | None | None | None | None |
| 177Leu | None | None | None | None | None |
| 178Leu | None | None | None | None | None |
| 179Phe | None | None | 175.13 | None | None |
| 180Gly | 8.27 | 112.13 | 176.29 | 44.65 | None |
| 181Ala | 8.18 | 116.72 | 179.34 | 52.4 | 21.6 |
| 182 Val | 9.08 | 124.39 | 174.61 | 60.46 | 33.14 |
| 183Gly | 9.14 | 110.32 | 171.48 | 43.67 | None |
| 184Ala | 8.87 | 122.78 | 179.34 | 54.95 | 17.18 |
| 185 Val | 8.1 | 116.76 | 177.42 | 66.41 | 28.76 |
| 186Ala | 8.71 | 122.44 | 179.8 | 54.67 | 17.23 |
| 187Ile | 8.24 | 117.96 | 177.4 | 66.24 | 38.36 |
| 188Ala | 8.84 | 122.2 | 179.42 | 55.85 | 17.29 |
| 189Lys | 9.12 | 115.65 | 180.12 | 59.13 | 29.02 |
| 190Ala | 8.59 | 118.57 | 179.29 | 55.32 | 17.82 |
| 191 Val | 7.77 | 116.57 | 177.46 | 66.17 | 31.08 |
| 192Lys | 8.3 | 119.45 | 178.15 | 58.84 | 30.93 |
| 193Lys | 8.44 | 121.15 | 178.88 | 59.97 | 30.57 |


| Residue | H | N | C | Ca | Cb |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 194Ser | None | None | 174.29 | 61.63 | 68.38 |
| 195Ile | 8.32 | 124.4 | 176.88 | 62.53 | 37.66 |
| 196His | 8.64 | 117.41 | 177.69 | 62.33 | 28.26 |
| 197Gly | 8.52 | 107.35 | 175.15 | 45.05 | None |
| 198Leu | 7.96 | 123.81 | 175.39 | 59.75 | 40.24 |
| 199Glu | None | None | None | None | None |
| 200Pro | None | None | 177.75 | 66.62 | 30.85 |
| 201Glu | 8.58 | 118.95 | 178.95 | 57.71 | 30.97 |
| 202Glu | 7.84 | 120.65 | 177.71 | 57.81 | 29.45 |
| 203Ile | 7.76 | 120.62 | 179.28 | 62.06 | 40.82 |
| 204Gly | 8.63 | 107.48 | 176.31 | 45.03 | None |
| 205Leu | 7.66 | 121.78 | 178.61 | 55.18 | 40.61 |
| 206Leu | 8.07 | 116.7 | 177.52 | 57.44 | 38.24 |
| 207 Tyr | 8.98 | 119.48 | 178.58 | 59 | 38.31 |
| 208GIn | 8.07 | 117.51 | 177.61 | 57.76 | 27.99 |
| 209Glu | 7.99 | 119.96 | 178.7 | 59.48 | 30.67 |
| 210Lys | 8.5 | 117.82 | 178.45 | 59.24 | 30.78 |
| 211GIn | 7.55 | 117.92 | 178.31 | 58.55 | 28.39 |
| 212Ala | 8.3 | 120.3 | 179.51 | 55.24 | 17.41 |
| 213Ile | 8.27 | 118.48 | 177.52 | 66.59 | 38.27 |
| 214Leu | 8.31 | 118.67 | 177.96 | 57.53 | 41.04 |
| 215Glu | 8.82 | 120.21 | 176.3 | 57.18 | 29.5 |
| 216Ala | 7.72 | 120.11 | 178.14 | 54.42 | 17.34 |
| 217lle | 8.18 | 117.62 | 177.64 | 66.73 | 38.47 |
| 218Arg | 8.35 | 121.51 | 175.76 | 59.91 | 30.64 |
| 219Glu | 8.46 | 119.36 | 179.11 | 55.43 | 29.09 |
| 220Gly | None | None | None | None | None |
| 2211 l | None | None | None | None | None |
| 222 Val | 8.62 | 121.58 | 173.86 | 59.83 | 31.29 |
| 223Ala | 8.95 | 127.37 | 176.55 | 49.74 | 22.67 |
| 224Ile | 8.87 | 111.03 | 176.82 | 58 | 41.78 |
| 225Asn | 8 | 119.48 | 179.6 | 55.19 | 41.01 |
| 226GIn | None | None | 176.69 | 58.47 | 27.82 |
| 227Glu | 7.56 | 116.39 | 177.07 | 55.9 | 28.95 |
| 228Gly | 8.44 | 107.02 | 173.58 | 45.1 | None |
| 229Thr | 7.92 | 118.47 | 174.63 | 61.57 | 69.48 |
| 23011 e | 8.32 | 124.32 | 176.77 | 62.56 | 37.26 |
| 231 Thr | 7.82 | 121.32 | None | None | None |
| 232Met | None | None | None | None | None |
| 233 Val | None | None | None | None | None |
| 234Asn | None | None | None | None | None |
| 235Gln | 8.8 | 119.57 | 177.22 | 58.41 | 30.93 |
| 236Thr | 7.87 | 115.37 | 176.67 | 66.4 | 68.04 |
| 237Ala | 7.86 | 121.8 | 176.03 | 55.23 | 17.43 |
| 238Leu | 8.48 | 117.44 | 177.95 | 57.59 | 40.55 |
| 239Lys | 8.59 | 118.2 | 179.68 | 59.19 | 30.96 |
| 240Leu | 8.35 | 118.81 | 178.52 | 55.43 | 40.16 |
| 241Leu | 7.9 | 116.4 | 176.88 | 56.13 | 40.61 |
| 242Gly | 8.36 | 106.73 | 172.75 | 45.08 | None |


| Residue | H | N | C | Ca | Cb |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 243Tyr | 7.6 | 120.37 | 176.58 | 58.09 | 40.66 |
| 244Asp | 8.47 | 117.89 | 178.03 | 54.79 | 41.73 |
| 245Asn | 7.65 | 115.66 | 178.9 | 55.74 | 38.72 |
| 246Glu | None | None | None | None | None |
| 247Arg | None | None | None | None | None |
| 248Asn | None | None | None | None | None |
| 249 Val | None | None | None | None | None |
| 250Leu | 7.48 | 120.7 | 178.03 | 57.08 | 40.67 |
| 251Gly | 8.92 | 109.6 | 173.81 | 44.85 | None |
| 252Thr | 7.83 | 118.64 | 176.41 | 62.24 | None |
| 253Pro | None | 124.58 | 179.54 | 62.59 | 31.81 |
| 254Ile | 8.99 | 127.21 | 175.92 | 63.63 | 34.17 |
| 255Leu | 8.42 | 119.28 | 178.53 | 54.64 | 39.75 |
| 256GIn | 7.57 | 114.76 | 176.44 | 57.43 | 28.38 |
| 257Leu | 7.91 | 117.72 | 177.57 | 57.99 | 40.05 |
| 258lle | 8.39 | 117.27 | 179.16 | 57.66 | 38.17 |
| 259Pro | None | None | 177.65 | 66.39 | 30.29 |
| 260His | 8.05 | 118.78 | 177.61 | 55.31 | 27.83 |
| 261Ser | None | None | None | 63.19 | None |
| 262Arg | 7.76 | 120.63 | 178.57 | 58.53 | 28.84 |
| 263Leu | 8.01 | 117.76 | 177.68 | 59.68 | 39.89 |
| 264Pro | None | None | 178.83 | 65.49 | 30.2 |
| 265Glu | 7.3 | 117.72 | 178.36 | 58.71 | 29.78 |
| 266 Val | 8.32 | 119.25 | 177.31 | 65.39 | 29.59 |
| 26711 e | 8.73 | 117.69 | 176.99 | 62.7 | 38.8 |
| 268Arg | 7.28 | 117.56 | 177.16 | 56.54 | 30.04 |
| 269Thr | 8.56 | 107.04 | 177.27 | 62.21 | 71.54 |
| 270Gly | 8.42 | 111.5 | 173.01 | 46.35 | None |
| 271GIn | 8.04 | 119.15 | 174.36 | 53.62 | 29.6 |
| 272Ala | 8.47 | 125.01 | 176.79 | 51.7 | 20.16 |
| 273Glu | 8.78 | 119.34 | 174.62 | 59.6 | 30.76 |
| 274Tyr | 8.57 | 119.76 | 177.52 | 56.16 | 40.85 |
| 275Asp | 8.86 | 118.85 | 174.95 | 54.79 | 40.62 |
| 276Asp | 8.06 | 120.54 | None | 54.88 | None |
| 277Glu | None | None | None | None | None |
| 278Met | None | None | None | None | None |
| 279 Val | None | None | None | None | None |
| 280Leu | None | None | 178.66 | 55.48 | None |
| 281Gly | 8.25 | 112.22 | 176.25 | 44.67 | None |
| 282Gly | 7.73 | 107.65 | 170.82 | 45.36 | None |
| 283Glu | 7.9 | 121.05 | 175.21 | 55.1 | 30.8 |
| 284 Thr | 8.01 | 118.96 | 176.85 | 61.46 | 68.82 |
| 285 Val | 7.47 | 121.37 | 176.07 | 58.95 | 35.65 |
| 286Ile | 7.79 | 117.79 | 175.59 | 59.42 | 40.25 |
| 287Ala | 9.26 | 130.53 | 176.6 | 49.97 | 21.73 |
| 288Asn | None | None | None | None | None |
| 289Arg | None | None | None | None | None |
| 29011 e | None | None | None | None | None |
| 291Pro | None | None | 174.9 | 62.78 | 30.69 |


| Residue | H | N | C | Ca | Cb |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 292Ile | 8.35 | 121.4 | 175.69 | 59.24 | 38.69 |
| 293Lys | 8.83 | 125.52 | 175.95 | 53.87 | 35.8 |
| 294Asn | 8.56 | 117.93 | 178.01 | 50.27 | 37.88 |
| 295Lys | 8.32 | 117.53 | 177.77 | 58.5 | 27.88 |
| 296Gln | 7.55 | 116.11 | 176.13 | 55.87 | 28.87 |
| 297Gly | 8.17 | 107.52 | 173.55 | 45.19 | None |
| 298Arg | 8.14 | 120.94 | 176.27 | 54.89 | 30.23 |
| 299Val | 8.86 | 124.73 | 176.62 | 62.95 | 30.34 |
| 300Ile | 8.86 | 120.02 | 175.55 | 60.18 | 38.52 |
| 301Gly | 7.94 | 107.43 | 170.67 | 45.37 | None |
| 302Ala | 8.56 | 119.68 | 173.93 | 51.76 | 21.81 |
| 303Val | 8.92 | 118.9 | None | 58.83 | None |
| 304Ser | None | None | None | None | None |
| 305Thr | None | None | None | None | None |
| 306Phe | None | None | None | None | None |
| 307Arg | None | None | None | None | None |
| 308Asn | None | None | None | None | None |
| 309Lys | None | None | None | None | None |

Table B.3: Predicted torsion angles from chemical shift of TM II in the free state

```
# Phi/Psi Angles From 'Strong' TALOS-N Predictions:
# error margins are set to conservative default values of double the
# deviation observed in TALOS-N capped at a minimum of +/-20 degree.
    3 VAL PHI -151.3 -75.7
    3 VAL PSI 111.5 158.4
    4 GLY PHI -171.1 -44.6
    4 GLY PSI 152.6 198.8
    5 ALA PHI -81.7 -41.7
    5 ALA PSI -55.7 -15.7
    6 VAL PHI -83.5 -43.5
    6 VAL PSI -63.3 -23.3
    7 ALA PHI -84.8 -44.8
    7 ALA PSI -60.9 -20.9
    8 ILE PHI -85.9 -45.9
    8 ILE PSI -63.3 -23.3
    9 ALA PHI -82.7 -42.7
    9 ALA PSI -62.4 -22.4
    10 LYS PHI -83.5 -43.5
    10 LYS PSI -60.4 -20.4
    11 ALA PHI -86.4 -46.4
    11 ALA PSI -60.3 -20.3
    12 VAL PHI -85.3 -45.3
    12 VAL PSI -65.7 -25.7
    13 LYS PHI -82.4 -42.4
    13 LYS PSI -56.7 -16.7
    14 LYS PHI -83.0 -43.0
    14 LYS PSI -50.4 -10.4
# Phi/Psi Angles From 'Generous' TALOS-N Predictions:
# error margins are set to default values of triple the standard
# deviation observed in TALOS-N capped at a minimum of +/-30 degree.
```

Table B.4: Predicted torsion angles from chemical shift of TM II in the bound state

```
# Phi/Psi Angles From 'Strong' TALOS-N Predictions:
# error margins are set to conservative default values of double the
# deviation observed in TALOS-N capped at a minimum of +/-20 degree.
    1 GLY PHI 58.7 98.7
    1 GLY PSI 
    3 VAL PHI -86.4 -46.4
    3 VAL PSI -58.7 -18.7
    5 ALA PHI -84.4 -44.4
    5 ALA PSI -59.5 -19.5
    6 VAL PHI -85.3 -45.3
    6 VAL PSI -61.7 -21.7
    7 ALA PHI -83.4 -43.4
    7 ALA PSI 
    8 ILE PHI -85.0 -45.0
    8 ILE PSI -64.5 -24.5
    9 ALA PHI -81.3 -41.3
    9 ALA PSI -61.7 -21.7
    10 LYS PHI -86.9 -46.9
    10 LYS PSI -56.9 -16.9
    11 ALA PHI -87.6 -47.6
    11 ALA PSI -51.7 -11.7
    12 VAL PHI -120.4 -69.1
    12 VAL PSI -17.5 22.5
# Phi/Psi Angles From 'Generous' TALOS-N Predictions:
# error margins are set to default values of triple the standard
# deviation observed in TALOS-N capped at a minimum of +/-30 degree.
    2 ALA PHI -92.4 -32.4
    2 ALA PSI -67.7 -7.7
    4 GLY PHI -93.0 -33.0
    4 GLY PSI -70.0 -10.0
    13 LYS PHI -139.2 19.7
    13 LYS PSI -70.0 19.5
```


## APPENDIX C

## Appendix: Chapter 3



Figure C.1: Kinase activity of the WT, V285A and N288D PASc-kin constructs by SPA ${ }^{33} \mathrm{P}$ assay. The WT (blue) and V285A (orange) mutant display parallel dimer in crystal, which have elevated rate of phosphorylation compared with the antiparallel mutant N288D (grey) PASc attached kinase (A). Data are provided by M.Stopp


Figure C.2: Consumption of ATP from ${ }^{31} \mathrm{P}$ NMR activity assay measure to 800 h .


Figure C.3: Dynamic light scattering (DLS) measurement of the WT (blue) and N288D mutant (orange) PASc-kin at a concentration of $140 \mathrm{uM}(\mathrm{A})$ and $70 \mathrm{uM}(\mathrm{B})$. The data is provided by M. Han

## C. 1 Derivation of reaction kinetics of ATP hydrolysis

CitA kinase converts ATP into ADP and free phosphate, there is reaction

$$
\begin{equation*}
A T P+C i t A \xrightarrow{k_{1}} C i t A-P i \xrightarrow{k_{2}} C i t A+P i \tag{C.1}
\end{equation*}
$$

$\mathrm{k}_{1}$ is the phosphorylation rate, while $\mathrm{k}_{2}$ is the hydrolysis rate, both reactions are so far considered to be non-reversible.In the beginning since the ATP concentration is much larger than that of the CitA, it can be considered a constant. The change of CitA-Pi concentration is:

$$
\begin{equation*}
\Delta[C i t A-P i]=[C i t A] \cdot k_{1}-[C i t A-P i] \cdot k_{2} \tag{C.2}
\end{equation*}
$$

Change in ATP concentration

$$
\begin{equation*}
\Delta[A T P]=-[C i t A] \cdot k_{1} \tag{C.3}
\end{equation*}
$$

Change in free phosphate concentration

$$
\begin{equation*}
\Delta[P i]=[C i t A-P i] \cdot k_{2} \tag{C.4}
\end{equation*}
$$

Since the enzyme is not consumed, the total citA concentration remains unchanged at:

$$
\begin{equation*}
[C i t A]_{\text {total }}=[C i t A-P i]+[C i t A] \tag{C.5}
\end{equation*}
$$

At steady state, the phophorylated CitA does not change,

$$
\begin{equation*}
\Delta[\text { CitA }-P i]=0=[\text { CitA }] \cdot k_{1}-[C i t A-P i] \cdot k_{2} \tag{C.6}
\end{equation*}
$$

with equation C.5,

$$
\begin{gather*}
{[\text { CitA }]=\frac{k_{2}}{k_{1}+k_{2}} \cdot[\text { Cit A }]_{\text {total }}}  \tag{C.7}\\
{[\text { CitA }-P i]=\frac{k_{1}}{k_{1}+k_{2}} \cdot[\text { CitA }]_{t o t a l}} \tag{C.8}
\end{gather*}
$$

With equation C. 3 and C. 4

$$
\begin{equation*}
\Delta[A T P]=-\frac{k_{2} \cdot k_{1}}{k_{1}+k_{2}} \cdot[C i t A]_{\text {total }} \tag{C.9}
\end{equation*}
$$

Change in free phosphate concentration

$$
\begin{equation*}
\Delta[P i]=\frac{k_{2} \cdot k_{1}}{k_{1}+k_{2}} \cdot[\text { CitA }]_{t o t a l} \tag{C.10}
\end{equation*}
$$

So in the beginning of the reaction, the consumption of ATP and the production of free phosphate follows a linear equation.

## APPENDIX D

## Appendix: Chapter 4



Figure D.1: DNP enhancement in CitA PASpc free sample is similar for proton one pulse (upper) and proton to fluorine CP (lower) experiment.

Table D.1: Intensity of the ${ }^{19}$ F CODEX experiment of the CF3-N308C CitA PASpc in the free state and the intensities from their respective reference experiments.

| Time [ms] | s | Error s | so | Error so | s/s0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 250 | $3.52 \mathrm{E}+08$ | $8.32 \mathrm{E}+06$ | $4.11 \mathrm{E}+08$ | $1.09 \mathrm{E}+07$ | 0.86 |
| 300 | $5.40 \mathrm{E}+08$ | $3.52 \mathrm{E}+07$ | $3.38 \mathrm{E}+08$ | $1.39 \mathrm{E}+07$ | 1.60 |
| 500 | $3.11 \mathrm{E}+08$ | $9.08 \mathrm{E}+06$ | $6.27 \mathrm{E}+08$ | $4.13 \mathrm{E}+07$ | 0.50 |



Figure D.2: (H)NH spectrum of CF3-N308C CitA PASpc liposome sample after incubation with citrate free buffer at $40^{\circ} \mathrm{C}$ for one week. The intensity for the citrate indication His96 side-chain (black square) indicates that there is only a very small portion (1D trace) of the citrate bound sample left.

Table D.2: Intensity of the ${ }^{19}$ F CODEX experiment of the CF3-N308C CitA PASpc in the citrate bound state and the intensities from their respective reference experiments.

| Time [ms] | s | Error s | so | Error so | s/so |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 20 | $3.94 \mathrm{E}+08$ | $5.95 \mathrm{E}+06$ | $4.19 \mathrm{E}+08$ | $1.80 \mathrm{E}+07$ | 0.94 |
| $\mathbf{5 0}$ | $5.70 \mathrm{E}+08$ | $2.90 \mathrm{E}+07$ | $5.54 \mathrm{E}+08$ | $3.26 \mathrm{E}+07$ | 1.03 |
| 100 | $3.10 \mathrm{E}+08$ | $1.11 \mathrm{E}+07$ | $3.42 \mathrm{E}+08$ | $3.04 \mathrm{E}+07$ | 0.91 |
| 250 | $2.70 \mathrm{E}+08$ | $2.10 \mathrm{E}+07$ | $4.50 \mathrm{E}+08$ | $2.98 \mathrm{E}+07$ | 0.60 |
| 275 | $3.93 \mathrm{E}+08$ | $6.16 \mathrm{E}+07$ | $5.85 \mathrm{E}+08$ | $1.92 \mathrm{E}+07$ | 0.67 |
| 300 | $4.25 \mathrm{E}+08$ | $4.81 \mathrm{E}+07$ | $5.85 \mathrm{E}+08$ | $2.55 \mathrm{E}+07$ | 0.73 |

## APPENDIX E

## Appendix: Chapter 5

## E. 1 Fitting of TREDOR curves



























































































































































* indicates potentially compromised fit quality due to spectral overlap

Table E.1: Relaxation rate Nitrogen T 2 from (H)NH vs. TREDOR relaxation rate

| Residue | hNH t2 [ms] TREDOR T2[ms] Residue | hNH t2[ms] TREDOR T2 [ms] |  |  |
| :--- | ---: | ---: | ---: | ---: |
| 7GluN | 19.55 | 3.87 34LeuN | 64.94 | 4.34 |
| 8LeuN | 68.45 | 4.51 35AsnN | 56.15 | 4.02 |
| 9ValN | 67.61 | 3.5237 ThrN | 70.08 | 5.82 |
| 10LeuN | 64.02 | 4.6838 AsnN | 69.74 | 4.46 |
| 11AlaN | 103.95 | 0.91 39LysN | 92.85 | 4.16 |
| 12LeuN | 78.37 | 3.9840 AspN | 49.85 | 5.12 |
| 13TyrN | 84.67 | 4.9341 TrpN | 64.31 | 3.27 |
| 14AspN | 109.89 | 4.7941 TrpNe | 53.30 | 4.73 |
| 15TyrN | 74.18 | 5.1742 TrpN | 72.10 | 9.68 |
| 16GInN | 136.61 | 5.3042 TrpNe 1 | 162.07 | 5.81 |
| 17GluN | 88.34 | 5.7243 LysN | 86.43 | 4.08 |
| 18LysN | 83.61 | 4.4244 ValN | 76.05 | 3.05 |
| 19SerN | 65.40 | 5.7245 GluN | 79.11 | 5.30 |
| 22GluN | 74.35 | 3.5749 ArgN | 52.88 | 6.50 |
| 23ValN | 101.01 | 4.0350 GlnN | 75.24 | 5.29 |
| 24ThrN | 118.62 | 4.8651 GlyN | 69.54 | 9.48 |
| 25MetN | 79.74 | $3.9052 P h e N$ | 104.60 | 4.98 |
| 26LysN | 108.70 | 4.2153 ValN | 77.04 | 3.50 |
| 27LysN | 106.27 | 3.7355 AlaN | 93.37 | 4.64 |
| 28GlyN | 70.32 | $6.4056 A l a N$ | 73.42 | 4.73 |
| 29AspN | 75.13 | 5.2357 TyrN | 85.84 | 3.94 |
| 30IleN | 91.49 | 3.5958 VaIN | 86.13 | 3.35 |
| 31LeuN | 70.18 | 3.8759 LysN | 60.28 | 3.14 |
| 32ThrN | 90.33 | 4.92 60LysN | 119.19 | 3.64 |
| 33LeuN | 98.91 | 4.46 61LeuN | 85.76 | 3.88 |

Table E.2: Upper and lower distance restraints used in the SH3 structure calculation. Ambiguous restraints are given in the CYANA format as putting them with $0 \AA$

| Contact |  |  | Upper limit [ $\AA$ ¢ $]$ | Lower limit [ $\AA$ ] |
| :---: | :---: | :---: | :---: | :---: |
| 8 LEU | N | 8 LEU CG | 3.44 | 2.82 |
| 8 LEU | N | 8 LEU CD1 | 3.91 | 3.2 |
| 8 LEU | N | 8 LEU CD2 | 0 | 0 |
| 8 LEU | N | 7 GLU CB | 3.78 | 3.09 |
| 9 VAL | N | 9 VAL CG1 | 3.44 | 2.81 |
| 9 VAL | N | 9 VAL CG2 | 3.31 | 2.71 |
| 10 LEU | N | 10 LEU CG | 3.92 | 3.21 |
| 10 LEU | N | 10 LEU CD1 | 0 | 0 |
| 10 LEU | N | 10 LEU CD2 | 0 | 0 |
| 10 LEU | N | 9 VAL CB | 3.77 | 3.09 |
| 10 LEU | N | 9 VAL CG2 | 4.3 | 3.52 |
| 10 LEU | N | 61 LEU CD1 | 4.73 | 3.87 |
| 10 LEU | N | 61 LEU CD2 | 0 | 0 |
| 11 ALA | N | 10 LEU CD1 | 3.51 | 2.87 |
| 11 ALA | N | 10 LEU CD2 | 0 | 0 |
| 12 LEU | N | 12 LEU CG | 3.6 | 2.94 |
| 12 LEU | N | 12 LEU CD1 | 0 | 0 |
| 12 LEU | N | 12 LEU CD2 | 0 | 0 |
| 12 LEU | N | 58 VAL CG1 | 4.28 | 3.51 |
| 13 TYR | N | 11 ALA CB | 4.54 | 3.71 |
| 13 TYR | N | 27 LYS CB | 4.77 | 3.9 |
| 14 ASP | N | 27 LYS CB | 4.53 | 3.7 |
| 15 TYR | N | 14 ASP CB | 4.77 | 3.24 |
| 15 TYR | $N$ | 25 MET CG | 4.45 | 3.64 |
| 15 TYR | N | 25 MET CE | 5.05 | 4.01 |
| 16 GLN | N | 16 GLN CG | 4.33 | 3.54 |
| 17 GLU | N | 17 GLU CG | 3.76 | 3.08 |
| 17 GLU | N | 16 GLN CB | 3.6 | 2.94 |
| 18 LYS | N | 18 LYS CG | 3.3 | 2.7 |
| 18 LYS | N | 17 GLU CB | 3.62 | 2.96 |
| 19 SER | N | 18 LYS CB | 3.82 | 3.12 |
| 19 SER | N | 17 GLU CB | 4.93 | 4.03 |
| 19 SER | N | 22 GLU CG | 4.78 | 3.91 |
| 19 SER | N | 18 LYS CG | 4.97 | 4.07 |
| 22 GLU | N | 22 GLU CG | 3.91 | 3.2 |
| 22 GLU | N | 21 ARG CG | 4.39 | 3.59 |
| 23 VAL | N | 23 VAL CG1 | 3.79 | 3.1 |
| 23 VAL | N | 22 GLU CB | 3.18 | 2.6 |
| 23 VAL | N | 17 GLU CB | 4.03 | 3.29 |
| 23 VAL | N | 23 VAL CG2 | 3.6 | 2.94 |
| 24 THR | N | 24 THR CG2 | 4.03 | 3.29 |
| 24 THR | N | 23 VAL CB | 3.49 | 2.86 |
| 24 THR | N | 23 VAL CG2 | 4.23 | 3.46 |


| 24 THR | N | 17 GLU CB | 4.34 | 3.55 |
| :---: | :---: | :---: | :---: | :---: |
| 25 MET | N | 25 MET CG | 3.44 | 2.82 |
| 25 MET | N | 24 THR CG2 | 4.34 | 3.55 |
| 26 LYS | N | 26 LYS CG | 4.02 | 3.29 |
| 26 LYS | N | 26 LYS CD | 4.7 | 3.85 |
| 26 LYS | N | 25 MET CB | 4.4 | 3.6 |
| 26 LYS | N | 25 MET CG | 4.09 | 3.35 |
| 27 LYS | N | 27 LYS CG | 4.02 | 3.29 |
| 27 LYS | N | 26 LYS CB | 3.79 | 3.1 |
| 27 LYS | N | 26 LYS CD | 4.69 | 3.83 |
| 28 GLY | N | 27 LYS CB | 3.79 | 3.1 |
| 28 GLY | N | 27 LYS CG | 3.79 | 3.1 |
| 28 GLY | N | 11 ALA CB | 4.59 | 3.75 |
| 29 ASP | N | 11 ALA CB | 4.7 | 3.85 |
| 30 ILE N | N | 30 ILE CG1 | 3.49 | 2.86 |
| 30 ILE | N | 30 ILE CD1 | 4.5 | 3.68 |
| 31 LEU | N | 30 ILE CG1 | 4.03 | 3.29 |
| 31 LEU | N | 30 ILE CB | 4.32 | 3.58 |
| 32 THR | N | 32 THR CG2 | 3.98 | 3.26 |
| 33 LEU | N | 33 LEU CD1 | 3.73 | 3.05 |
| 33 LEU | N | 33 LEU CD2 | 0 | 0 |
| 33 LEU | N | 33 LEU CG | 4.07 | 3.33 |
| 33 LEU | N | 44 VAL CG1 | 4.75 | 3.88 |
| 34 LEU | N | 34 LEU CD1 | 4.31 | 3.52 |
| 34 LEU | N | 34 LEU CD2 | 0 | 0 |
| 34 LEU | N | 34 LEU CD1 | 4.06 | 3.32 |
| 34 LEU | N | 34 LEU CD2 | 0 | 0 |
| 34 LEU | N | 34 LEU CG | 3.44 | 2.82 |
| 35 ASN | N | 43 LYS CB | 4.32 | 3.53 |
| 35 ASN | N | 34 LEU CG | 4.35 | 3.56 |
| 35 ASN | N | 33 LEU CD1 | 4.33 | 3.54 |
| 37 THR | N | 37 THR CG2 | 3.2 | 2.62 |
| 40 ASP | N | 39 LYS CB | 3.78 | 3.1 |
| 40 ASP | N | 39 LYS CG | 4.05 | 3.31 |
| 43 LYS | N | 43 LYS CG | 4.2 | 3.44 |
| 43 LYS | N | 42 TRP CB | 3.96 | 3.24 |
| 44 VAL | N | 44 VAL CG2 | 3.31 | 2.71 |
| 44 VAL | N | 44 VAL CG1 | 3.31 | 2.71 |
| 44 VAL | N | 43 LYS CB | 4.02 | 3.29 |
| 44 VAL | N | 43 LYS CG | 4.03 | 3.3 |
| 45 GLU | N | 44 VAL CG2 | 4.38 | 3.59 |
| 45 GLU | N | 44 VAL CG1 | 4.8 | 3.93 |
| 46 VAL | N | 46 VAL CG1 | 4.07 | 3.33 |
| 46 VAL | N | 50 GLN CB | 4.56 | 3.73 |
| 49 ARG | N | 49 ARG CG | 3.64 | 2.98 |
| 50 GLN | N | 50 GLN CG | 3.6 | 2.95 |
| 50 GLN | N | 49 ARG CG | 4.77 | 3.91 |


| 51 GLY N | 50 GLN CB | 3.36 | 2.75 |
| :---: | :---: | :---: | :---: |
| 51 GLY N | 43 LYS CG | 4.28 | 3.51 |
| 51 GLY N | 23 VAL CG1 | 4.03 | 3.29 |
| 51 GLY N | 23 VAL CG2 | 4.34 | 3.55 |
| 51 GLY N | 23 VAL CB | 4.46 | 3.65 |
| 53 VAL N | 53 VAL CG1 | 3.33 | 2.73 |
| 53 VAL N | 53 VAL CG2 | 3.44 | 2.81 |
| 55 ALA N | 54 PRO CB | 4.03 | 3.3 |
| 56 ALA N | 55 ALA CB | 3.79 | 3.1 |
| 57 TYR N | 56 ALA CB | 3.44 | 2.81 |
| 58 VAL N | 58 VAL CG1 | 3.45 | 2.83 |
| 58 VAL N | 58 VAL CG2 | 3.44 | 2.81 |
| 59 LYS N | 59 LYS CG | 3.79 | 3.1 |
| 59 LYS N | 58 VAL CG2 | 4.34 | 3.55 |
| 59 LYS N | 58 VAL CG1 | 4.78 | 3.91 |
| 60 LYS N | 60 LYS CG | 4.07 | 3.33 |
| 60 LYS N | 59 LYS CG | 4.11 | 3.36 |
| 60 LYS N | 9 VAL CG1 | 4.11 | 3.36 |
| 61 LEU N | 61 LEU CG | 3.44 | 2.82 |
| 61 LEU N | 60 LYS CB | 4.09 | 3.34 |
| 61 LEU N | 61 LEU CD1 | 4.16 | 3.4 |
| 61 LEU N | 61 LEU CD2 | 0 | 0 |
| 41 TRP NE1 | 41 TRP CB | 3.98 | 3.26 |
| 42 TRP NE1 | 42 TRP CB | 4.03 | 3.29 |
| 42 TRP NE1 | 55 ALA CB | 4.29 | 3.51 |
| 31 LEU N | 31 LEU CD2 | 3.44 | 2.82 |
| 31 LEU N | 31 LEU CG | 4 | 3.27 |
| 31 LEU N | 31 LEU CD1 | 0 | 0 |
| 31 LEU N | 31 LEU CD2 | 0 | 0 |
| 8 LEU H | 8 LEU C | 3.1 | 2.54 |
| 9 VAL H | 9 VAL C | 2.95 | 2.41 |
| 10 LEU H | 10 LEU C | 2.89 | 2.37 |
| 13 TYR H | 13 TYR C | 2.81 | 2.3 |
| 13 TYR H | 11 ALA C | 3.17 | 2.59 |
| 15 TYR H | 15 TYR C | 2.73 | 2.23 |
| 15 TYR H | 25 MET C | 3.09 | 2.53 |
| 16 GLN H | 16 GLN C | 2.65 | 2.17 |
| 17 GLU H | 17 GLU C | 3.56 | 2.92 |
| 19 SER H | 19 SER C | 2.66 | 2.18 |
| 23 VAL H | 23 VAL C | 2.88 | 2.36 |
| 23 VAL H | 51 GLY C | 3.8 | 3.11 |
| 24 THR H | 24 THR C | 3.25 | 2.66 |
| 25 MET H | 25 MET C | 2.76 | 2.26 |
| 25 MET H | 15 TYR C | 2.76 | 2.26 |
| 27 LYS H | 27 LYS C | 3.69 | 3.02 |
| 27 LYS H | 14 ASP C | 3.17 | 3.17 |
| 27 LYS H | 13 TYR C | 3.56 | 2.92 |


| 28 GLY H | 28 GLY C | 3.15 | 2.57 |
| :---: | :---: | :---: | :---: |
| 28 GLY H | 26 LYS C | 3.78 | 3.1 |
| 29 ASP H | 29 ASP C | 3.04 | 2.48 |
| 29 ASP H | 27 LYS C | 2.95 | 2.41 |
| 33 LEU H | 33 LEU C | 2.88 | 2.36 |
| 33 LEU H | 31 LEU C | 4.2 | 3.44 |
| 35 ASN H | 35 ASN C | 2.65 | 2.17 |
| 35 ASN H | 43 LYS C | 3.14 | 2.57 |
| 41 TRP H | 41 TRP C | 2.75 | 2.25 |
| 41 TRP H | 38 ASN C | 3.25 | 2.66 |
| 42 TRP H | 53 VAL C | 3.05 | 2.49 |
| 42 TRP HE1 | 39 LYS C | 4 | 3.28 |
| 42 TRP HE1 | 38 ASN C | 3.76 | 3.08 |
| 42 TRP HE1 | 36 SER C | 3.76 | 3.08 |
| 43 LYS H | 43 LYS C | 3.22 | 2.64 |
| 44 VAL H | 44 VAL C | 2.86 | 2.34 |
| 44 VAL H | 51 GLY C | 2.98 | 2.44 |
| 51 GLY H | 51 GLY C | 2.7 | 2.21 |
| 51 GLY H | 44 VAL C | 3.3 | 2.7 |
| 52 PHE H | 52 PHE C | 2.84 | 2.32 |
| 52 PHE H | 21 ARG C | 3.07 | 2.51 |
| 53 VAL H | 53 VAL C | 2.78 | 2.28 |
| 53 VAL H | 42 TRP C | 3.08 | 2.52 |
| 55 ALA H | 55 ALA C | 3.54 | 2.9 |
| 55 ALA H | 53 VAL C | 3.89 | 3.19 |
| 55 ALA H | 41 TRP C | 3.93 | 3.21 |
| 58 VAL H | 58 VAL C | 2.89 | 2.37 |
| 61 LEU H | 61 LEU C | 3.1 | 2.54 |
| 62 ASP H | 62 ASP C | 3.7 | 3.02 |
| 27 LYS H | 14 ASP CG | 3.17 | 2.59 |
| 24 THR H | 17 GLU CD | 4.27 | 3.49 |
| 18 LYS H | 22 GLU CD | 3.77 | 3.08 |
| 19 SER H | 22 GLU CD | 2.64 | 2.16 |
| 40 ASP H | 38 ASN CG | 2.94 | 2.41 |
| 41 TRP H | 38 ASN CG | 3.25 | 2.66 |
| 50 GLN HE21 | 45 GLU CD | 3.45 | 2.82 |

Table E.3: TALOS-N angle restrains

| Residue |  | Angle | Angle margin |  |
| :---: | :---: | :---: | :---: | :---: |
| 8 | LEU | PHI | -155.7 | -108 |
| 8 | LEU | PSI | 135.2 | 175.2 |
| 9 | VAL | PHI | -148.2 | -108.2 |
| 9 | VAL | PSI | 131.4 | 171.4 |
| 10 | LEU | PHI | -145.1 | -105.1 |
| 10 | LEU | PSI | 116.5 | 156.5 |
| 11 | ALA | PHI | -94.3 | -52.8 |
| 11 | ALA | PSI | 106.7 | 146.7 |
| 12 | LEU | PHI | -103.9 | -63.1 |
| 12 | LEU | PSI | -60.8 | -19.7 |
| 13 | TYR | PHI | -182.5 | -131.4 |
| 13 | TYR | PSI | 138 | 178 |
| 16 | GLN | PHI | -149.5 | -86.9 |
| 16 | GLN | PSI | 109.4 | 169.9 |
| 23 | VAL | PHI | -175.6 | -72.5 |
| 23 | VAL | PSI | 129.5 | 177.3 |
| 24 | THR | PHI | -132.1 | -83.3 |
| 24 | THR | PSI | 111.5 | 151.5 |
| 25 | MET | PHI | -151.5 | -89.7 |
| 25 | MET | PSI | 113.5 | 171.6 |
| 26 | LYS | PHI | -118 | -56.7 |
| 26 | LYS | PSI | 130.5 | 170.5 |
| 27 | LYS | PHI | -76.5 | -36.5 |
| 27 | LYS | PSI | 113.2 | 153.2 |
| 29 | ASP | PHI | -84.6 | -44.6 |
| 29 | ASP | PSI | 126.3 | 166.3 |
| 30 | ILE | PHI | -129.2 | -89.2 |
| 30 | ILE | PSI | 104.5 | 144.5 |
| 31 | LEU | PHI | -130 | -89.1 |
| 31 | LEU | PSI | 103.8 | 158.4 |
| 32 | THR | PHI | -97.3 | -52.6 |
| 32 | THR | PSI | 107.9 | 147.9 |
| 33 | LEU | PHI | -117.8 | -50.3 |
| 33 | LEU | PSI | 88.7 | 168.2 |
| 34 | LEU | PHI | -79.4 | -39.4 |
| 34 | LEU | PSI | -51.9 | -11.9 |
| 36 | SER | PHI | -88.8 | -48.8 |
| 36 | SER | PSI | -55.9 | -15.9 |
| 37 | THR | PHI | -85.9 | -45.9 |
| 37 | THR | PSI | -59.5 | -19.5 |
| 38 | ASN | PHI | -81.9 | -41.9 |
| 39 | LYS | PSI | -38.9 | 1.1 |
| 40 | ASP | PHI | -105.7 | -65.7 |
| 40 | ASP | PSI | -29.6 | 10.4 |
| 41 | TRP | PHI | -123.6 | -67.1 |
| 41 | TRP | PSI | 112.2 | 159.1 |


|  |  |  |  |  |
| :--- | :--- | :--- | :---: | :---: |
| 42 | TRP | PHI | -144.3 | -104.3 |
| 42 | TRP | PSI | 114.3 | 175.6 |
| 43 | LYS | PHI | -138.7 | -62.6 |
| 43 | LYS | PSI | 103.5 | 151 |
| 44 | VAL | PHI | -146.1 | -94.4 |
| 44 | VAL | PSI | 112.9 | 178.5 |
| 50 | GLN | PHI | -162.6 | -88.7 |
| 50 | GLN | PSI | 132.5 | 172.5 |
| 51 | GLY | PHI | 153.3 | 193.3 |
| 51 | GLY | PSI | -192.9 | -152.9 |
| 52 | PHE | PHI | -119.7 | -67 |
| 52 | PHE | PSI | 116.3 | 163.4 |
| 53 | VAL | PHI | -157.6 | -104 |
| 53 | VAL | PSI | 124.7 | 175.2 |
| 54 | PRO | PSI | 108.5 | 148.5 |
| 55 | ALA | PHI | -82.5 | -42.5 |
| 55 | ALA | PSI | -51.7 | -11.7 |
| 56 | ALA | PHI | -87.5 | -47.5 |
| 56 | ALA | PSI | -39.1 | 3.8 |
| 59 | LYS | PHI | -149.6 | -94.6 |
| 59 | LYS | PSI | 107.6 | 172.9 |
| 60 | LYS | PHI | -99.5 | -50.9 |
| 60 | LYS | PSI | 108.3 | 148.3 |
| 61 | LEU | PHI | -104 | -50.2 |
| 61 | LEU | PSI | 115.2 | 155.2 |

## E. 2 Simultaneous multi-curve TREDOR fitting

starting with Equation E.1. This result can be extended [101] to a set of $n_{i}$ equations, which is used to simultaneously fit the buildup curves of the individual carbon spins coupled to $\mathrm{N}_{1}$.

$$
n_{i}\left\{\begin{array}{l}
V_{11}\left(t_{m} i x\right)=\Lambda_{1}\left(1-\left[J_{0}\left(\sqrt{2} D_{11} t_{m i x}\right)\right]^{2}\right) \prod_{k=2}^{n_{i}}\left(1+\left[J_{0} \sqrt{2} D_{1 k} t_{m i x}\right]^{2}\right)  \tag{E.1}\\
V_{12}\left(t_{m} i x\right)=\Lambda_{1}\left(1-\left[J_{0}\left(\sqrt{2} D_{12} t_{m i x}\right)\right]^{2}\right) \prod_{k=1 \neq 2}^{n_{i}}\left(1+\left[J_{0} \sqrt{2} D_{1 k} t_{m i x}\right]^{2}\right) \\
\ldots \\
V_{1 i}\left(t_{m} i x\right)=\Lambda_{1}\left(1-\left[J_{0}\left(\sqrt{2} D_{1 i} t_{m i x}\right)\right]^{2}\right) \prod_{k=1 \neq i}^{n_{i}}\left(1+\left[J_{0} \sqrt{2} D_{1 k} t_{m i x}\right]^{2}\right)
\end{array}\right.
$$

Where $\Lambda_{1}$ is given as:

$$
\begin{equation*}
\Lambda_{1}=\frac{1}{2^{n_{i}}} V_{1}(0) \lambda_{1} \exp \left(-\Gamma_{1} t_{m i x}\right) \tag{E.2}
\end{equation*}
$$

The $\Gamma_{1}$ gives the coherence decay rate of spin coherence, which can be modeled as a single exponential. $\lambda_{1}$ is an amplitude scaling factor, which is typically fit freely since the starting signal is not recorded in a TEDOR measurement. So in a standard TEDOR fitting, to extract the dipolar couplings, one needs to fit the overall decay rate and an arbitrary scaling factor which are irrelevant to the parameter of concern. This consequently puts more demand on the data density, something that might be unachievable especially for samples with low sensitivity or short coherence times. In the pseudo-4D TREDOR experiment, we address this problem by recording the intensity of the untransferred part of the magnetization, so that the ratio $\zeta_{1 i}\left(t_{m i x}\right)$ can be formed between transferred and total magnetization

$$
\begin{align*}
\zeta_{1 i}\left(t_{m i x}\right) & =\frac{V_{1 i}\left(t_{m i x}\right)}{V_{1}\left(t_{m i x}\right)+\sum_{k=1}^{n_{i}} V_{1 k}\left(t_{m i x}\right)}  \tag{E.3}\\
& =\frac{V_{1 i}\left(t_{m i x}\right)}{V_{\text {total }}\left(t_{m i x}\right)} \tag{E.4}
\end{align*}
$$

Where $V_{1}\left(t_{\text {mix }}\right)$ is the intensity of the untransferred nitrogen signal, and the $V_{\text {total }}\left(t_{\text {mix }}\right)$ is the total signal at a certain mixing time. The untransferred signal $V_{1}\left(t_{m i x}\right)$ appears with the same scaling and typically also the same decay parameter, and hence the total signal also follows a
single exponential decay of the original signal intensity.

$$
\begin{equation*}
V_{\text {total }}\left(t_{m i x}\right)=V_{1}(0) \exp \left(-\Gamma_{1} t_{m i x}\right) \tag{E.5}
\end{equation*}
$$

Normalization by the total signal results in a coherence decay-free TEDOR curve, for which the parameters $\lambda_{1}$ and $V_{1}(0)$ no longer appear. Combining Equation E. 1 and Equation E.3, it is straightforward to show that we can fit the simultaneous buildup curve of several ${ }^{13} \mathrm{C}$ spins coupled to the same $\mathrm{N}_{1}$ as the following set of equations:

$$
n_{i}\left\{\begin{array}{l}
\zeta_{11}\left(t_{m i x}\right)=\frac{1}{2^{n_{i}}}\left(1-\left[J_{0}\left(\sqrt{2} D_{11} t_{m i x}\right)\right]^{2}\right) \prod_{k=2}^{n_{i}}\left(1+\left[J_{0} \sqrt{2} D_{1 k} t_{m i x}\right]^{2}\right)  \tag{E.6}\\
\zeta_{12}\left(t_{m i x}\right)=\frac{1}{2^{n_{i}}}\left(1-\left[J_{0}\left(\sqrt{2} D_{12} t_{m i x}\right)\right]^{2}\right) \prod_{k=1 \neq 2}^{n_{i}}\left(1+\left[J_{0} \sqrt{2} D_{1 k} t_{m i x}\right]^{2}\right) \\
\ldots \\
\zeta_{1 i}\left(t_{m i x}\right)=\frac{1}{2^{n_{i}}}\left(1-\left[J_{0}\left(\sqrt{2} D_{1 i} t_{m i x}\right)\right]^{2}\right) \prod_{k=1 \neq i}^{n_{i}}\left(1+\left[J_{0} \sqrt{2} D_{1 k} t_{m i x}\right]^{2}\right)
\end{array}\right.
$$



Figure E.1: Comparison of positions of multiple quantum artifacts in pseudo-3D H-CO TREDOR. With a shift of the offset from 193.7 ppm to 203.7 ppm , the artifacts changed chemical shifts on the $\mathrm{H}-\mathrm{CO}$ dimension each by 20 ppm , confirming the major artifacts left are only the leftover double quantum terms but not zero quantum terms. When the offset is placed at 203.7 ppm , the artifacts are placed away from the signal of interest enough for quantitative analysis.

Table E.4: CO T2 rho in SH 3 in ms with different hard pulse power in kHz and offsets in ppm

| Power | Offset | 53 ppm |
| :--- | :--- | :--- |
| 85 kHz | 11.1 ms | 64.7 ms |
| 100 kHz | 10.9 ms | 60.4 ms |

Table E.5: CA T2 rho in SH 3 in ms with different hard pulse power in kHz and offsets in ppm

| Power_offset | 53 ppm | 100 ppm |
| :--- | :--- | :--- |
| 85 kHz | 41.0 ms | 41.1 ms |
| 100 kHz | 47.5 ms | 48.5 ms |

## E. 3 TREDOR pulse programs

## E.3.1 hnCxNH TREDOR pulse program

```
; set F1 sweep width to 240 ppm and 13C offset to 60 ppm to place
;15N at correct freq.
; hnCANHtedor.mpibpc
; copy from 3D (H) CANH developed at CRMN in the group of G. Pintacuda
```

; Recent notes:
; this version does not require 13C axis inversion
; set inversion pulse bandwidth to 48 ppm
;Avance III version
; parameters:
;p1 : 1H 90 pulse duration
; p3 : 13C 90 pulse duration
;p7 : 15N 90 pulse duration
; p30 : water suppression time (30-200 ms)
; cnst21 : CO offset in Hz
; cnst22 : 60 ppm Carbon offset in Hz
; cnst23 : CA/CO offset in Hz
; d1 : recycle delay
; d5 : NOE mixing time
; dO : 15N initial evolution time
; d10 : 1/2 of 13CO initial evolution time
;in0 : increment for 15 N evolution
;in10 : 1/2 increment for 13CA evolution
; cpdprg1 : tppm (at pl13) or waltz (at pl13)
; cpdprg4 : cwY (at pl12)
; cpdprg5 : cwX (at pl12)

```
;pcpd1 : pulse length in decoupling sequence
;(2xtau_r for tppm, 25us for 10kHz waltz)
;pl1 : power level of 1H hard pulse
;pl12 : power level of decoupling (10-15 kHz)
;pl13 : power level for water suppression
; spnam1 : 1H shape for 1H->13CA CP (ramp 10-20%)
;spoal1 : N/A
;spoff1 : [ON/RES]
;sp1 : 1H power level during 1H->13CA CP
; spnam10: 1H shape for 15N->1H(N) CP (ramp 10-20%)
; spoal10 : N/A
;spoff10 : [ON/RES]
; sp10 : 1H power level during 15N->1H CP
; cpdprg2 : 15N decoupling pattern during acq (waltz-16)
;p17 : contact time 15N->1H(N) CP (300-700 us)
;pcpd2 : pulse length in 15N decoupling sequence (25 us)
;pl7 : power level for 15N hard pulse
;pl16 : power level for 15N decoupling (corr. to 10 kHz)
;pl2 : power level for 15N hard pulse
;pl20 : 15N power level for 15N->1H CP
; spnam2 : 15N shape for 13CA->15N CP (tan-c100-w10pct)
; sp2 : 15N power level for 13CA->15N CP
;spoal2 : N/A
;spoff2 : [ON/RES]
;p15 : contact time 1H->15N CP (short, 300 - 700us)
;p14 : contact time for 15N->13CA CP (10ms)
;p16 : contact time 13CA->15N CP (10 ms)
;p18 : Reburp Cx pulse duration
;pcpd3 : pulse length in 13C decoupling sequence (25 us)
; cpdprg3 : 13CO/CA decoupling pattern during 15N evol (waltz-16)
```

```
;pl3 : power level of 13C hard pulse [REFERENCE]
;pl17 : power level for 13CO/CA decoupling (10 kHz)
;spnam9 : 13C shape for 13CA->15N CP (rectangle)
;sp9: 13C power for 13CA->15N CP
; spoal9 : N/A
; spoff9 : [ON/RES CO]
;spnam18 : Reburp
;spoff18 : [ON/RES CO]
; spnam19 : 13CA selective pulse shape (Q3)
; spoal19 : N/A
;spoff19 : [ON/RES CA]
; spnam29 : 13C shape for 1H->13CO CP (rectangle)
;sp29: 13C power level for 1H->13CO CP
;spoal29 : N/A
;spoff29 : [ON/RES CO]
;zgoptns : -Dfslg, -Dlacq, or blank
;l1 : to set mixing time
;l8 : z-filter time (number or rotor periods
;19 : fraction of rotation rate for t1 increment, about 20 for 55 kHz
;d23 : indirect dim incrementation
; $COMMENT=Inverse Cp with INEPT CBCA mixing
; $CLASS=Solids
; $DIM=3D
; $TYPE=H detect
; $SUBTYPE=Heteronuclear
; $OWNER=CRMN
#include <Avancesolids.incl>
```

```
; Start evolutions from exactly 0
"d0=0.0"
"d10=0.0"
"d20=0.0"
;"tautotal=5.96*d10"
```

; 1 H settings
"spoall=0.5" ; default value (irrelevant)
"spoff1=0.0" ; on-resonance
"spoal10=0.5" ; default value (irrelevant)
"spoff10=0.0" ; on-resonance
; 15N settings
"pcpd2=25" $\quad$; does not work!
"plw2=plw7"
"plw16=plw2*(pow (p7/25,2))" ; 15N waltz 10kHz decoupling power level
"spoal2=0.5" ; default value (irrelevant)
"spoff2=0.0" ; on-resonance
; 13C settings
"plw17=plw3*(pow(p3/25,2))" ; 13C waltz 10kHz decoupling power level
"cnst20 $=($ sfo3-bf3)*1000000/bf3" ; 40 ppm C frequency offset (ppm)
"cnst22 = cnst20-12" ; 28 ppm, CB frequency offset (ppm)
"cnst23 $=$ cnst20+(113.7-40)" ; the offset half-way CO and CA (ppm)
"cnst21 = cnst20+(113.7)" ; CO frequency offset (ppm)

```
"p18=5.81/(48.0*bf3/1000000)" ; 5 to 53 ppm bandwidth (safe)
;"spw18=plw3*pow((0.5/(p18*0.1515))/(0.25/p3),2)" ; Q3 power level
"spw18=plw3*pow((0.5/(p18*0.07981))/(0.25/p3),2)" ; Reburp power level
"spoal18=0.5" ; default value (irrelevant)
"spoff18=bf3*((-12)/1000000)" ;on res with
CB, CG, etc
```

| "p19 ${ }^{\text {c }}$. $412 /(105.0 *$ bf3/1000000) " |  |
| :---: | :---: |
| "spw19=plw3*pow ( $0.5 /(\mathrm{p} 19 * 0.1515) \mathrm{l} /(0.25 / \mathrm{p} 3), 2) \mathrm{c}$; Q3 power level |  |
| "spoal19=0.5" | ; default value (irrelevant) |
| "spoff19=0.0" | ; CA frequency |
| "spoal9=0.5" | ; default value (irrelevant) |
| "spoff $9=0.0$ " | ; on-resonance |
| "spoal29=0.5" | ; default value (irrelevant) |
| "spoff29=0.0" | ; on-resonance CA |

;"acqt0=1u*cnst11" ??
;"in0=inf1"
;"in10=inf2/2"

```
"d25=0.25s/cnst 31-1u"
"d26=0.25s/cnst31-(p3)" ; one-quarter rotor cycle ...
"d27=0.25s/cnst31-larger((p7),(p3))"
;the 0.5u compensates for if statement in
```

```
;indirect acq. dim.
"d28=0.25s/cnst31-p7"
;"d29=0.25s/cnst31-p7"
"d23=1s*19/cnst31"
"121=p18/(2*(1s/cnst31))+0.25s/cnst 31+1"
"d29=(121+20)*1.0s/cnst31-p18/2-0.25/cnst31"
"d30=d29-p3*2"
;d29=0.75s/cnst31-(p3/2)" =p18/2+0.25rotor
;rounded up to even rotor period -p18/2 -0.25rotor
"d31=1s/cnst31"
;define pulse tauz
;"tauz=l8*1s/cnst31-p3"
;"l10=1"
;"l11=110 %l9"
define delay t1incr
"l22=((p18+p19+p18)/(1.0s/cnst31)+1)/2"
"d24=122*2*1.0s/cnst31-p18-p19-p18"
;"d2=(18+1) *1s/cnst31-p3-p7-d
"d2=1s/cnst31-p3-p7" ;d2
;if not using selective pulses for J dec in 13C evolution
"t1incr=(1s*19)/(cnst31)"
"in0=tlincr"
"in10=(in0/2.48152)/2"
"inf1=in10*2"
"in20=inf2"
```

```
define delay mix
"mix=4*2*11/cnst31"
    tlincr
    d23
    mix
I ze
2 d1 do:f2
#include <p15_prot.incl>
#include <aq_prot.incl>
        1u fq= cnst22(bf ppm):f3
        (p1 pl1 ph4):f1
; 1u cpds2:f2 cpds3:f3
; d20
; (p1 pl1 pho):f1 (1u do):f2 (1u do):f3
;3 d5
; lu fq=cnst22(bf ppm):f3
; (p1 pl1 ph4):f1 ;check phase
; HN cp
    (p15:sp0 ph17):f1 (p15 pl20 ph14):f2
; NCa
    1u cpds1:f1
```

```
    d25 pl7:f2 pl3:f3 ; tppm decoupling at pl12 if synchronized
    ; with TPPM use special decoupling sequence
5 d26 ; several F3 pulses ...
    (p3*2 ph8^):f3 ; ... at intervals of ...
    d26 ; ... one-half rotor cycle
    d26
    (p3*2 ph8^):f3 ; ... at intervals of ...
    d26 ; F1 pulse
    d26 ; several F3 pulses ...
    (p3*2 ph8^):f3 ; ... at intervals of ...
    d26 ; ... at intervals of ...
    d26 ; ... one-half rotor cycle
    (p3*2 ph8^):f3 ; ... at intervals of ...
    d26 ; F1 pulse
lo to 5 times l1
    d29
    (center (p7*2 ph15):f2 (p18:sp18 ph15):f3)
    ;CO selective Pi to NOT REDOR
    (p3*2 pl3 ph18):f3
    d30 ; Hahn echo refocussing pulse on F1
6 d26 pl3:f3 ; several F3 pulses ...
    (p3*2 ph9^):f3 ; ... at intervals of ...
    d26 ; ... at intervals of ...
    d26 ; ... one-half rotor cycle
    (p3*2 ph9^):f3 ; ... at intervals of ...
    d26 ;
    d26 ; several F3 pulses ...
    (p3*2 ph9^):f3 ; ... at intervals of ...
    d26 ; ... at intervals of ...
```

```
        d26 ; ... one-half rotor cycle
    (p3*2 ph9^):f3 ; ... at intervals of ...
    d26 ; F1 pulse
lo to 6 times l1
    d27 fq= cnst20(bf ppm):f3
    (ralign (p7 ph12):f2 (p3 pl3 ph3):f3) ; end of integer rotor period
    ;(tauz pll4 phO):f1 ;Z-filter integer rotor period
    ; (p3 pl3 ph0):f3 ; begin rotor period at beginning of pulse
;;;;;; d0 cpds3:f2
; (rotor pi rotor d0):f2 (rotor pi rotor d10 d10 p3 pl3 ph0):f3
    ;if "d0==0" goto 7
; 0.5u
    ;(d0) (d10 d10 p3 pl3 ph0):f3
    ;(p7 pl7 ph0):f2
    ;if "d0>0" goto 8
; INP,0.5u
    if "d0 == 0"
    {
        (p7 pl7 ph20):f2 (p3 pl3 ph19):f3
    }
    if "d0 > 0"
    {
        (d0) (d10 d10 p3 pl3 ph19):f3
        (p7 pl7 ph20):f2
    }
```

```
;OLDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDD
; (d0) (d10 d10 p3 pl3 ph3):f3
; (p7 pl7 ph0):f2 ; rotor period done at end of p1!
; OLDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDD
; LAP, 0.5u
8 d28 pl7:f2 pl3:f3 ; tppm decoupling at pl12
9 d26 fq= cnst22(bf ppm):f3 ; several F3 pulses ...
    (p3*2 ph10^):f3 ; ... at intervals of ...
    d26 ; ... one-half rotor cycle
    d26
    (p3*2 ph10^):f3 ; ... at intervals of ...
        d26
        d26 ; several F3 pulses ...
        (p3*2 ph10^):f3 ; ... at intervals of ...
        d26 ; ... one-half rotor cycle
        d26
    (p3*2 ph10^):f3 ; ... at intervals of ...
        d26
lo to 9 times l1
    d29
    (center (p7*2 ph0):f2 (p18:sp18 ph0):f3)
    ; Hahn echo refocussing pulse
    (p3*2 pl3 ph18):f3
    d30
10 d26 pl3:f3 ; several F3 pulses ...
    (p3*2 ph11^):f3 ; ... at intervals of ...
    d26 ; ... one-half rotor cycle
    d26
```

```
        (p3*2 ph11^):f3 ; ... at intervals of ...
        d26
        d26 ; several F3 pulses ...
        (p3*2 ph11^):f3 ; ... at intervals of ...
        d26 ; ... one-half rotor cycle
        d26
        (p3*2 ph11^):f3 ; ... at intervals of ...
        d26
lo to 10 times l1
        d28 fq = cnst23(bf ppm):f3 ; Hahn echo occurs about now
        (p7 ph16):f2 (1u do):f1
    ; (tauz pl14 ph0):f1
        (p30*0.125 pl13 ph0):f1
        (p30*0.125 pl13 ph1):f1
        (p30*0.125 pl13 ph0):f1
        (p30*0.125 pl13 ph1):f1
        (p7 ph2):f2 (1u cpds1):f1 (1u cpds3):f3
    ; (p16:sp9 ph10):f3 (p16:sp2 ph2):f2
    d20 ; fq= 0 (bf ppm):f2
    ;0.5u fq= 75 (bf ppm):f2
; 1u do:f1 do:f3
        (p7 pl7 ph5):f2 (1u do):f1 (1u do):f3
        ;water suppression
        (p30*0.125 pl13 ph0):f1
        (p30*0.125 pl13 ph1):f1
        (p30*0.125 pl13 ph0):f1
        (p30*0.125 pl13 ph1):f1
; end water suppression
```

```
(p7 pl7 ph6):f2
(p17 pl20 ph7):f2 (p17:sp10 ph13):f1
```

1u cpds2:f2
go=2 ph31
1 m do:f2

10m mc \#0 to 2
F1PH(calph(ph3, -90) \& calph(ph12, -90) \& calph(ph14, -90), caldel(d0, +in0) \&caldel(d10, +in10))
; F1PH (calph(ph14, -90) \& calph(ph12, -90), caldel(d0, +in0))
F2PH(calph(ph2, +90), caldel(d20, +in20)) ;15N
;F3PH(calph(ph4, +90), caldel(d20, +in20)) ;1H

```
HaltAcqu, 1m ;jump address for protection files
exit ;quit
ph0 = 0
ph1 = 1
ph3 = 2 2 0 0 ;was0 ;up after 13C evolution
ph4 = 2 ; proton flip down (FIRST PULSE)
; edge artifacts in 1H dimension without this phase cycle
ph2 = 0 0 2 2 ; down before 15N evolution
ph5 = 0
ph6 = 0 0 2 2
ph7 = 1
ph12 = 0 0 2 2;(float, 120.0) 0
ph14 = 0 0 2 2 ;(float, 120.0) 0
ph15 = 0 1
```

```
ph16 = 1 1 3 3
ph17 = 1 1 1 3 3 3 3 3 1 1
ph8= 0
ph9= 0 1 0 1 1 0 1 0 2 3 2 2 3 3 2 2 3 2
ph10= 0 1 0 1 1 1 0 1 0 2 3 2 2 3 3
ph11= 0 1 0 1 1 0
ph13 = 1
ph18 = 0 0 2 2 0 0 2 2
ph19 = 0 0 2 2 0 0 2 2 ; 13CA(all aliph) selective pulse
ph20 = 0 0 2 2
ph31 = 0 2 2 0 2 0 0 2 ; receiver phase for joint phase cycling
```


## E.3.2 hNhCOH TREDOR pulse program

```
;reduced the extra time int he echo on 2020-12-4 land
;modification of hnCONHtedor_nozf.xifo.5 for H-C TREDOR
;TREDOR CO hNhCOHtredor.land
;alons lends version
;set F1 sweep width to 240 ppm and 13C offset to 60 ppm
;to place 15N at correct freq.
; hnCANHtedor.mpibpc
; copy from 3D (H) CANH developed at CRMN in the group of G. Pintacuda
```

; Recent notes:
; this version does not require 13C axis inversion
; set inversion pulse bandwidth to 48 ppm

```
;Avance III version
;parameters:
;p1 : 1H 90 pulse duration
;p3 : 13C 90 pulse duration
;p7 : 15N 90 pulse duration
;p30 : water suppression time (30-200 ms)
;cnst21 : CO offset in Hz
;cnst22 : 60 ppm Carbon offset in Hz
;cnst23 : CA/CO offset in Hz
;d1 : recycle delay
;d5 : NOE mixing time
;dO : 15N initial evolution time
;d10 : 1/2 of 13CO initial evolution time
;in0 : increment for 15N evolution
;in10 : 1/2 increment for 13CA evolution
;cpdprg1 : tppm (at pl13) or waltz (at pl13)
;cpdprg4 : cwY (at pl12)
;cpdprg5 : cwX (at pl12)
;pcpd1 : pulse length in decoupling sequence
;(2xtau_r for tppm, 25us for 10kHz waltz)
;pl1 : power level of 1H hard pulse
;pl12 : power level of decoupling (10-15 kHz)
;pl13 : power level for water suppression
;spnam1 : 1H shape for 1H->13CA CP (ramp 10-20%)
;spoal1 : N/A
;spoff1 : [ON/RES]
;sp1 : 1H power level during 1H->13CA CP
;spnam10 : 1H shape for 15N->1H(N) CP (ramp 10-20%)
;spoal10 : N/A
;spoff10 : [ON/RES]
```

```
;sp10 : 1H power level during 15N->1H CP
;cpdprg2 : 15N decoupling pattern during acq (waltz-16)
;p17 : contact time 15N->1H(N) CP (300-700 us)
;pcpd2 : pulse length in 15N decoupling sequence (25 us)
;pl7 : power level for 15N hard pulse
;pl16 : power level for 15N decoupling (corr. to 10 kHz)
;pl2 : power level for 15N hard pulse
;pl20 : 15N power level for 15N->1H CP
;spnam2 : 15N shape for 13CA->15N CP (tan-c100-w10pct)
;sp2 : 15N power level for 13CA->15N CP
;spoal2 : N/A
;spoff2 : [ON/RES]
;p15 : contact time 1H->15N CP (short, 300 - 700us)
;p14 : contact time for 15N->13CA CP (10ms)
;p16 : contact time 13CA->15N CP (10 ms)
;p18 : Reburp Cx pulse duration
;pcpd3 : pulse length in 13C decoupling sequence (25 us)
;cpdprg3 : 13CO/CA decoupling pattern during 15N evol (waltz-16)
;pl3 : power level of 13C hard pulse [REFERENCE]
;pl17 : power level for 13CO/CA decoupling (10 kHz)
;spnam9 : 13C shape for 13CA->15N CP (rectangle)
;sp9 : 13C power for 13CA->15N CP
;spoal9 : N/A
;spoff9 : [ON/RES CO]
;spnam18 : Reburp
;spoff18 : [ON/RES CO]
;spnam19 : 13CA selective pulse shape (Q3)
;spoal19 : N/A
;spoff19 : [ON/RES CA]
;spnam29 : 13C shape for 1H->13CO CP (rectangle)
```

```
;sp29 : 13C power level for 1H->13CO CP
;spoal29: N/A
;spoff29 : [ON/RES CO]
;zgoptns : -Dfslg, -Dlacq, or blank
;l1 : to set mixing time
;l8 : z-filter time (number or rotor periods
;19 : fraction of rotation rate for t1 increment, about 4 for 55 kHz
;d23 : indirect dim incrementation
; $COMMENT=Inverse Cp with INEPT CBCA mixing
; $CLASS=Solids
; $DIM=3D
; $TYPE=H detect
; $SUBTYPE=Heteronuclear
; $OWNER=CRMN
#include <Avancesolids.incl>
; Start evolutions from exactly 0
"d0=0.0"
"d10=0.0"
"d20=0.0"
;"tautotal=5.96*d10"
; 1H settings
    "spoall=0.5" ; default value (irrelevant)
    "spoff1=0.0" ; on-resonance
    "spoal10=0.5" ; default value (irrelevant)
    "spoff10=0.0" ; on-resonance
```

```
"pcpd2=25" ;does not work!
"plw2=plw7"
"plw16=plw2*(pow(p7/25,2))" ; 15N waltz 10kHz decoupling power level
"spoal2=0.5" ; default value (irrelevant)
"spoff2=0.0" ; on-resonance
```

; 13C settings
"plw17=plw3*(pow(p3/25,2))" ; 13C waltz $10 k H z$ decoupling power level
;"cnst20 $=($ sfo3-bf3)*1000000/bf3" ; 40 ppm C frequency offset (ppm)
;"cnst22 = cnst20-12" ; 28 ppm, CB frequency offset (ppm)
;"cnst23 = cnst20+(113.7-40)" ; the offset half-way CO and CA (ppm)
;"cnst21 = cnst20+(113.7)" ; CO frequency offset (ppm)
"cnst21 $=($ sfo3-bf3)*1000000/bf3-20" ; CO frequency offset (ppm)
"cnst20 $=($ sfo3-bf3)*1000000/bf3" ; 183.7 ppm C frequency offset (ppm)
"cnst23 $=$ cnst $20+(113.7-173.7) " \quad$; the offset half-way CO and CA (ppm)
"cnst22 = cnst20-12-133.7" ; 28 ppm, CB frequency offset (ppm)
"p18=5.81/(100*bf3/1000000)" ; 100 ppm bandwidth (safe)
;"spw18=plw3*pow((0.5/(p18*0.1515))/(0.25/p3),2)" ; Q3 power level
"spw18=plw3*pow ( $0.5 /(p 18 * 0.07981)) /(0.25 / p 3), 2) " ;$ Reburp power level
"spoal18=0.5" ; default value (irrelevant)
;"spoff18=bf3*((-30)/1000000)" ; on res bf3*((-10)/1000000)" ;on res with C
"spoff18=0.0"
;"p19=3.412/(105.0*bf3/1000000)" ; 105 ppm bandwidth (safe)
;"spw19=plw3*pow((0.5/(p19*0.1515))/(0.25/p3),2)" ; Q3 power level

```
;"spoal19=0.5" ; default value (irrelevant)
;"spoff19=0.0"
; CA frequency
\begin{tabular}{ll} 
"spoal9 \(=0.5\) " & ; default value (irrelevant) \\
"spoff \(9=0.0 "\) & \(;\) on-resonance
\end{tabular}
"spoal29=0.5"
"spoff29=0.0"
;"acqt0=1u*cnst11" ??
;"in0=inf1"
;"in10=inf2/2"
```

"d25=0.25s/cnst $31-1 u "$
"d26=0.25s/cnst31-(p3)" ; one-quarter rotor cycle...
"d27=0.25s/cnst31-larger((p1), (p3))" ; the $0.5 u$ compensates for if statemen
"d22=0.25s/cnst31-p1"
"d28=0.25s/cnst31-1u"
;"d29=0.25s/cnst31-p7"
"d23=1s*19/cnst31"
$" 121=\mathrm{p} 18 /(2 *(1 \mathrm{~s} / \mathrm{cnst} 31))+0.25 \mathrm{~s} / \mathrm{cnst} 31+1 "$
"d29 $=(121+1) * 1.0 s / c n s t 31-p 18 / 2-0.25 / c n s t 31 "$
$" d 30=d 29-p 3 * 2 "$
; d29 $=0.75 \mathrm{~s} / \mathrm{cnst} 31-(\mathrm{p} 3 / 2) "=\mathrm{p} 18 / 2+0.25 r o t o r$ rounded up to even rotor period
"d31=1s/cnst31"
; define pulse tauz

```
;"tauz=18*1s/cnst31-p3"
;"110=1"
;"l11=110 %19"
define delay tlincr
"122=((p18+p18)/(1.0s/cnst31)+1)/2"
"d24=122*2*1.0s/cnst31-p18-p18"
;"d2=(18+1)*1s/cnst31-p3-p7-d
"d2=1s/cnst31-p3-p7" ; d2 if not using selective pulses for J dec in 13C evo.
"t1incr=(1s*l9)/(cnst31)"
"in0=t1incr"
;"in10=(in0/2.48152)/2"
;"in10=in0*3.976735/2"
"in10=in0/2"
```

"inf1=in10*2"
"in20=inf2"
define delay mix
"mix $=4 * 2 * 11 / \mathrm{cnst} 31$ "
t1incr
d23
mix
1 ze
2 d1 do:f2
\#include <p15_prot.incl>
\#include <aq_prot.incl>

1u fq= cnst21(bf ppm):f3

```
(p1 pl1 ph4):f1
```

```
; 1u cpds2:f2 cpds3:f3
; d20
; (p1 pl1 ph0):f1 (1u do):f2 (1u do):f3
;3 d5
; 1u fq=cnst22(bf ppm):f3
```

; (p1 pl1 ph4):f1 ; check phase
; HN cp
(p15:sp0 ph17):f1 (p15 pl20 ph14):f2
; NCa
; (p7 ph16):f2 (1u do):f1
; ( $\mathrm{p} 30 * 0.125 \mathrm{pl} 13 \mathrm{ph} 0): f 1$
; (p30*0.125 pl13 ph1):f1
; ( $\mathrm{p} 30 * 0.125 \mathrm{pl13} \mathrm{ph} 0): f 1$
; (p30*0.125 pl13 ph1):f1
; (p7 ph2):f2 (1u cpds1):f1 (1u cpds3):f3
(0.5u cpds1):f1 (0.5u cpds3):f3
d20
; fq= 0 (bf ppm):f2
; 0.5 u fq= 75 (bf ppm): f 2

```
; lu do:f1 do:f3
    (p7 pl7 ph5):f2 (1u do):f1 (1u do):f3
    ;water suppression
    (p30*0.25 pl13 ph0):f1
    (p30*0.25 pl13 ph1):f1
    (p30*0.25 pl13 ph0):f1
    (p30*0.25 pl13 ph1):f1
;end water suppression
    (p7 pl7 ph6):f2
    (p17 pl20 ph7):f2 (p17:sp10 ph13):f1
;past in, change channel for H-C TREDOR
    1u ;cpds1:f1
    d25 pl7:f2 pl3:f3
    ; tppm decoupling at pl12 if synchronized with TPPM use special
    ; decoupling sequence
5 d26 ; several F3 pulses ...
    (p3*2 ph8^):f3 ; ... at intervals of ...
    d26 ; ... one-half rotor cycle
    d26
    (p3*2 ph8^):f3 ; ... at intervals of ...
    d26 ; F1 pulse
    d26 ; several F3 pulses ...
    (p3*2 ph8^):f3 ; ... at intervals of ...
    d26 ; ... at intervals of ...
    d26 ; ... one-half rotor cycle
    (p3*2 ph8^):f3 ; ... at intervals of ...
    d26 ; F1 pulse
lo to 5 times l1
```

d2 9

```
    (center (p1*2 pl1 ph15):f1 (p18:sp18 ph15):f3) ;; ... at intervals of ..
    (p3*2 pl3 ph18):f3
    d30 ; Hahn echo refocussing pulse on F1
6 d26 pl3:f3 ; several F3 pulses ...
    (p3*2 ph9^):f3 ; ... at intervals of ...
        d26 ; ... at intervals of ...
        d26 ; ... one-half rotor cycle
    (p3*2 ph9^):f3 ; ... at intervals of ...
        d26 ;
        d26 ; several F3 pulses ...
        (p3*2 ph9^):f3 ; ... at intervals of ...
        d26 ; ... at intervals of ...
        d26 ; ... one-half rotor cycle
        (p3*2 ph9^):f3 ; ... at intervals of ...
    d26 ; F1 pulse
lo to 6 times l1
    d27 fq= cnst20(bf ppm):f3
    (ralign (p1 ph12):f1 (p3 pl3 ph3):f3 (1u cpds2):f2)
    ; end of integer rotor period
    ;(tauz pl14 ph0):f1 ;(1u fq=cnst22(bf ppm)):f3
    ;Z-filter integer rotor period
    ; (p3 pl3 ph0):f3 ; begin rotor period at beginning of pulse
```

    d10 ; decouple CA?
    d10
    (p1 pl1 ph18):f1 (p3 pl3 ph19):f3 (1u do):f2
    ```
; if "d0 == 0"
; {
; (p1 pl1 ph18):f1 (p3 pl3 ph19):f3
; }
; if "dO > 0"
; {
; (d0 pl pl1 ph18):f1 (d10 d10) ; switched which delay is shorter
; (p3 pl3 ph19):f3
; }
```

; OLDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDD
; (d0) (d10 d10 p3 pl3 ph3):f3
; (p7 pl7 pho):f2 ; rotor period done at end of p1!
; OLDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDD
; LAP, $0.5 u$
8 d27 pl7:f2 pl3:f3 ; tppm decoupling at pl12
9 d26 fq= cnst21 (bf ppm): f3 ; several F3 pulses ...
(p3*2 ph10^):f3 ; ... at intervals of ...
d26 ; ... one-half rotor cycle
d2 6
(p3*2 ph10^):f3 ; ... at intervals of ...
d2 6
d26 ; several F3 pulses ...
$(p 3 * 2$ ph10^):f3 ; ... at intervals of ...
d26 ; ... one-half rotor cycle
d2 6
$(p 3 \star 2$ ph10^):f3 ; ... at intervals of ...
d26
lo to 9 times 11

```
    d29
    (center (p1*2 pl1 ph0):f1 (p18:sp18 ph0):f3)
    ; Hahn echo refocussing pulse
    (p3*2 pl3 ph18):f3
    d30
10 d26 pl3:f3 ; several F3 pulses ...
    (p3*2 ph11^):f3 ; ... at intervals of ...
    d26 ; ... one-half rotor cycle
    d26
    (p3*2 ph11^):f3 ; ... at intervals of ...
    d26
    d26 ; several F3 pulses ...
    (p3*2 ph11^):f3 ; ... at intervals of ...
    d26 ; ... one-half rotor cycle
    d26
    (p3*2 ph11^):f3 ; ... at intervals of ...
    d26
lo to 10 times l1
    d28 fq = cnst21(bf ppm):f3 ; Hahn echo occurs about now
; (p7 ph16):f2 (1u do):f1
```

    1u cpds2:f2
    go=2 ph31
    1 m do: \(£ 2\)
    \(10 \mathrm{~m} \mathrm{mc} \# 0\) to 2
    F1PH (calph (ph3, -90) \& calph(ph12, -90) \& calph(ph13, -90),
    caldel(d0, +in0) \& caldel(d10, +in10))
    ```
;F1PH(calph(ph14, -90) & calph(ph12, -90), caldel(d0, +in0))
F2PH(calph(ph14, +90), caldel(d20, +in20)) ;15N
;F3PH(calph(ph4, +90), caldel(d20, +in20)) ;1H
```

HaltAcqu, 1m ;jump address for protection files
exit ;quit
pho $=0$
ph1 = 1
ph3 = 2200 ;was0 ; up after 13C evolution
ph4 = 2 ;edge artifacts in 1 H dimension without this phase cycle
;ph2 = 0022 ; down before 15 N evolution
ph5 = 1
ph6 = 0022 ; Remove this phase cycle?
ph7 = 1
ph12 = 002 2; (float, 120.0) 0
ph14 = 0022 ; (float, 120.0) 0
ph15 = 01
;ph16 = 1133
ph17 = 11333311 ; WHY THIS CYCLE? REMOVE?
ph8 $=0 \begin{array}{lllllllllllllllll}0 & 1 & 0 & 1 & 1 & 0 & 1 & 0 & 2 & 3 & 2 & 3 & 3 & 2 & 3 & 2 & \text {; xy }\end{array} 6$
ph9= 0 1 $10 \begin{array}{lllllllllllll} & 1 & 1 & 1 & 0 & 2 & 3 & 2 & 3 & 3 & 2 & 3 & 2\end{array}$
ph10 $=0 \begin{array}{llllllllllllllll}0 & 1 & 0 & 1 & 1 & 0 & 1 & 0 & 2 & 3 & 2 & 3 & 3 & 2 & 3 & 2\end{array}$
ph11= 0 1 $0011 \begin{array}{lllllllllll} & 1 & 1 & 2 & 3 & 2 & 3 & 3 & 2 & 3 & 2\end{array}$
ph13 = 2
ph18 = 00220022
ph19 = 00220022 ; 13CA(all aliph) selective pulse

```
ph31 = 0 2 2 0 2 0 0 2 ; receiver phase for joint phase cycling
```


## E. 4 TREDOR curve fitting script

```
    clear
res = 'leu12';
raw=readtable([res,'.txt']);
title = raw.Properties.VariableNames
timepts = raw{:,2}';
nitrogen = raw(:,3);
carbon1 = raw(:,4);
carbon2 = raw(:,5);
carbon3 = raw(:,7);
noise = raw{:,9}';
for i=1:height(nitrogen)
    V_total(i)=nitrogen{i,1}+carbon1{i,1};%+carbon2{i,1}+carbon3{i,1};
    curve1(i) = carbon1{i,1}/V_total(i);
    %curve2(i) = carbon2{i,1}/V_total(i);
    curve2(i) = 0
    %curve3(i) = carbon3{i,1}/V_total(i);
    curve3(i) = 0
end
jc1=0 ;% enter the j couplings here
lamsamp=[1];
%lamsamp=(1:10)/10;
%lamsamp=(1:3)/1; %for testing purposes
gamma2samp=(0)*30;%per second ~1/T2 to ~2/T2
%gamma2samp=0;
%gamma2samp=(3:5)*10; %for testing purposes
```

```
Dsamp=(0:30)*10;
```

montynumber=100; \%number of monty carlo noise additions
\%END DATA INPUT

```
%*************************************************************
jcoup1=(cos(3.14.*jc1.*timepts./2)).^2 ;%j coupling curve
```

c1noise=zeros(montynumber+1,length(noise));
for $k=1: l e n g t h(n o i s e)$
c1noise(:,k)=[0; noise(k) *randn(montynumber,1)];
end
\%the fit function value corresponding to the pH grid
chi2grid=zeros(length(Dsamp), length(gamma2samp), length(lamsamp),
(montynumber+1));
\%
$\%$
\%
\%
for l=1:length(Dsamp)
1
[c1]=tedorcurve1full_scaled(Dsamp(l),timepts);
c1j=c1.*jcoup1;
for o=1:length(gamma2samp)

```
        tmp=exp (-gamma2samp (o).*timepts);
        clg=tmp.*clj;
        for p=1:length(lamsamp)
        clglam=clg.*lamsamp (p);
        for q=1:(montynumber+1)
                chi2grid(l,o,p,q)=sum(((clglam-curvel+clnoise(q, :))./noise)
        end
        end
    end
end
fitD1s=zeros(montynumber+1,1);
fitgamma2s=zeros(montynumber+1,1);
fitlams=zeros(montynumber+1,1);
fitcurvesl=zeros(montynumber+1,length(timepts));
for o=1:(montynumber+1)
    sqchi2grid=squeeze(chi2grid(:, :, :,O));
    [a,b, c]=ind2sub(size(sqchi2grid),find(sqchi2grid==min(sqchi2grid(:))));
    fitD1s(o)=Dsamp(a);
    fitgamma2s(o)=gamma2samp (b);
    fitlams(o)=lamsamp(c);
```

    [fitcurvesl(o, :)]=tedorcurvelfull_scaled (Dsamp (a) ,timepts);
    ```
end
fitD1s;
fitgamma2s;
fitlams;
fitr1s=(3061.41./fitD1s).^0.33333333;
timesmooth = (0:700)/50000;
[asmooth] = tedorcurvelfull_scaled(Dsamp(a),timesmooth);
mean_D1 = mean(fitD1s)
erro_D1 = std(fitD1s)
```

